New scattering mechanism of electrons in the partial density-wave state in magnetic field

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Main message:

In the density-wave state coexisting with metallic conductivity the magnetoresistance (MR) studies must take into account the new scattering mechanism of conducting electrons, coming from the non-uniform magnetic breakdown.
It leads to the increase of longitudinal MR and (sometimes in quasi-2D materials) to the phase inversion of MQO.
This mechanism can be much stronger than impurities.

ECRYS-2014

Collaborators

Experiment and motivation:

Mark Kartsovnik

Walther-Meißner-Institute, Garching, Germany

Vladimir Zverev

(ISSP, Chernogolovka, Russia)

Theory: with Revaz Ramazashvili

(Laboratoire de Physique Théorique, Toulouse)

Publication: M.V. Kartsovnik, V.N. Zverev, D.Andres, W.Biberacher, T.Helm, P.D. Grigoriev, R.Ramazashvili, N.D. Kushch, H.Muller, "Magnetic quantum oscillations in the charge-density-wave state of the organic metals α-(BEDT-TTF)$_2$MHg(SCN)$_4$ with M = K and Tl", Low Temp. Phys., 40(4), 377 (2014) [FNT 40(4), 484]; arXiv:1311.5744.

2

Why magnetoresistance studies are important?

There are only few methods to study electronic dispersion *E(p)* and Fermi surface (FS) geometry in metals, including strongly-correlated systems with competing orders.

These methods include:

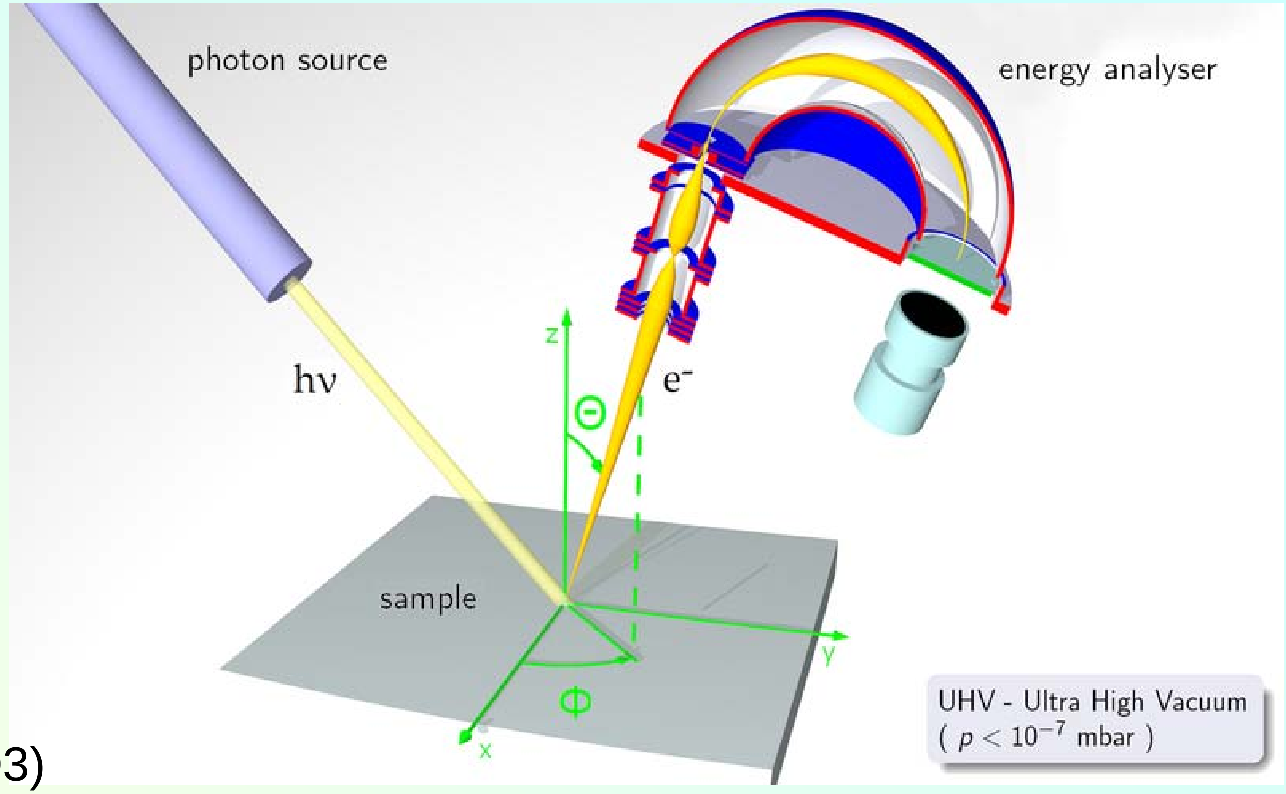
1. **Conductivity tensor** $\sigma_{ij} \propto e^2 \tau \left\langle v_i v_j \right\rangle_{FS} = \sigma_{ij}(T)$ **gives only general information about anisotropy of *E(p)* and about phase transitions with lowering temperature.**
2. **Band-structure calculations** (rough, not always reliable)
3. **ARPES (Angle resolved photoemission spectroscopy)** **Drawbacks: (i) Not always available; (ii) Only surface electrons participate; (iii) low resolution >10meV.**
4. **Magnetotransport: angular and field dependence of MR, including magnetic quantum oscillations (powerful tool, useful both alone or as complementary to ARPES).**

ARPES (Angle resolved photoemission spectroscopy)

Main idea:

$$E = \hbar\omega - E_k - \phi$$

E_k = kinetic energy of the outgoing electron — can be measured.
$\hbar\omega =$ incoming photon energy - known from experiment, φ = known electron work function.
Angle resolution of photoemitted electrons gives their momentum.



Rev.Mod.Phys. 75, 473 (2003)

The photocurrent intensity is proportional to a one-particle spectral function multiplied by the Fermi function:

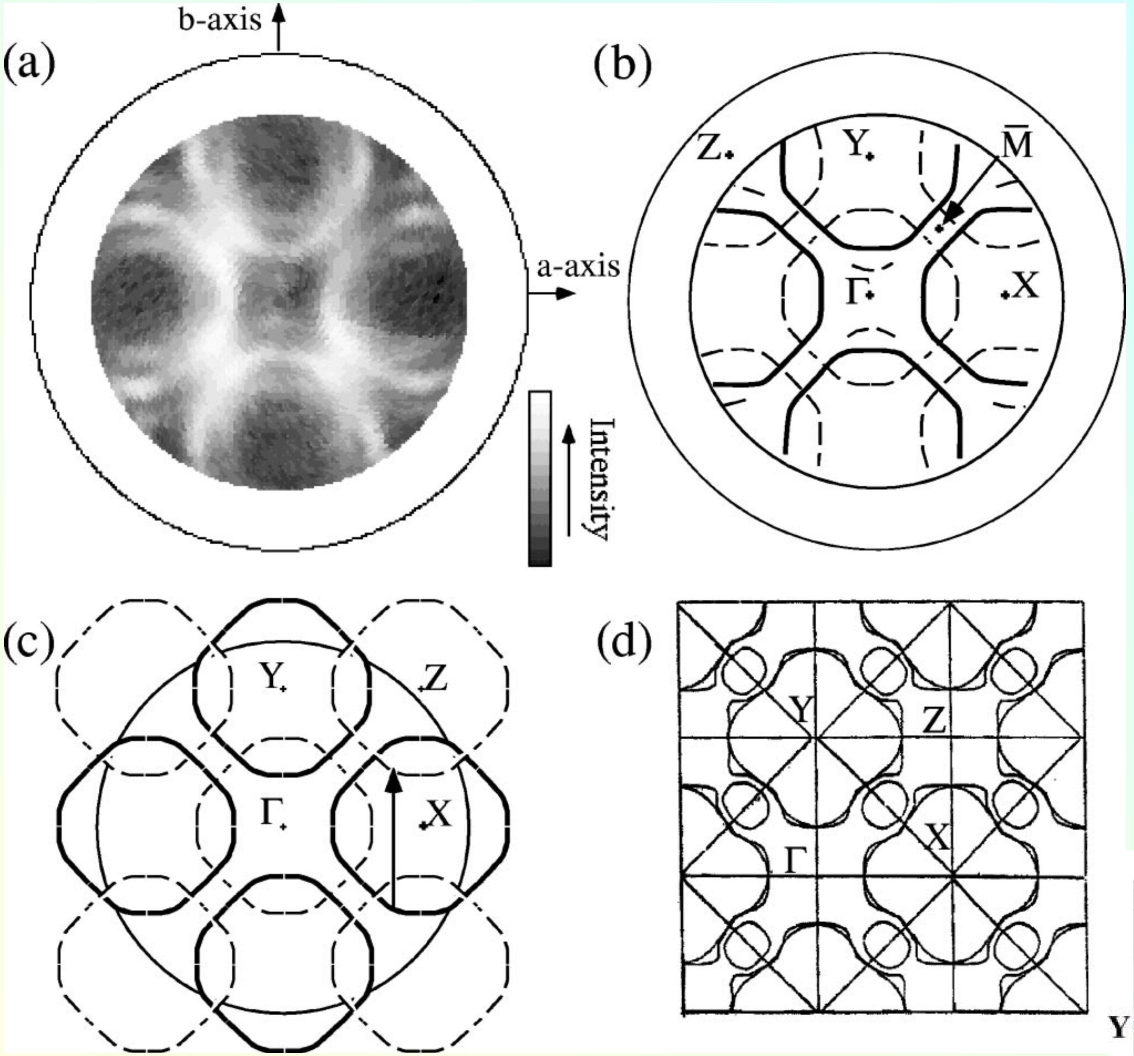
$$I(\mathbf{k},\omega) = A(\mathbf{k},\omega) f(\omega)$$

$$A(\omega,\mathbf{k}) = -\frac{1}{\pi}\frac{\Sigma''(\omega)}{(\omega - \varepsilon(\mathbf{k}) - \Sigma'(\omega))^2 + \Sigma''(\omega)^2}.$$

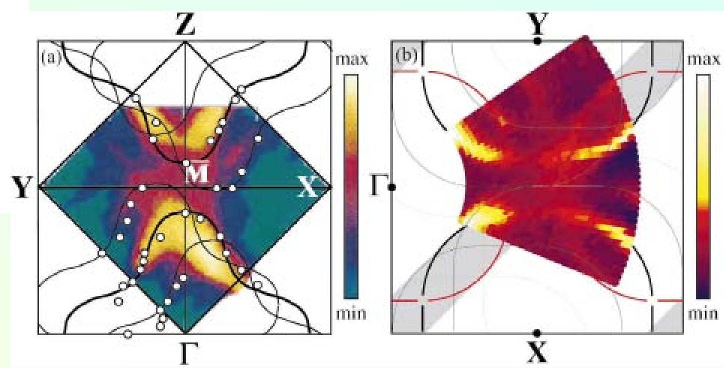
Therefore can find out information about *E(k)*

Drawbacks: 1) Often unavailable; 2) Only surface electrons participate.

ARPES data and Fermi-surface shape



The Fermi surface of near optimally doped $Bi_2Sr_2CaCu_2O_{8+\delta}$ (a) integrated intensity map (10-meV window centered at *EF*) for Bi2212 at 300 K obtained with 21.2-eV photons (HeI line); (b),(c) superposition of the main Fermi surface (thick lines) and of its (p,p) translation (thin dashed lines) due to backfolded shadow bands; (d) Fermi surface calculated by Massidda *et al.* (1988).

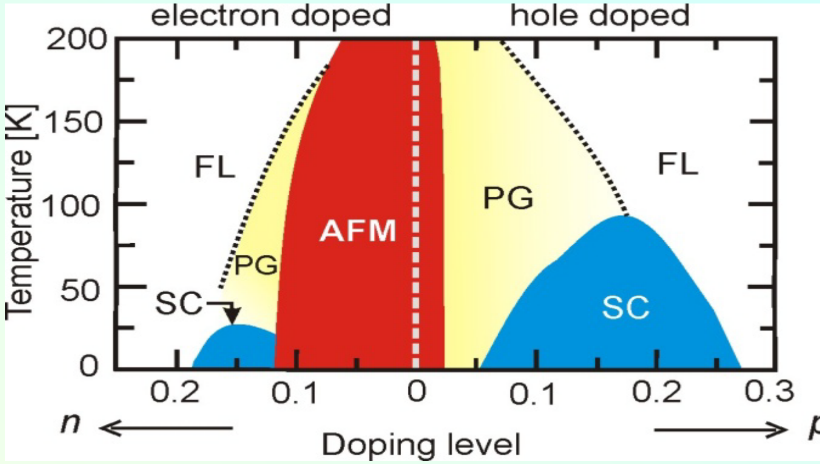


Drawback 3: Low resolution
=> ambiguous interpretation

Phase diagram of high-Tc cuprate SC. Importance of magnetoresistance studies.

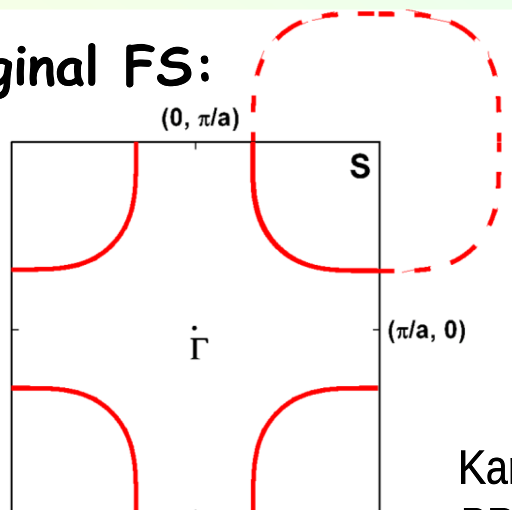
$Nd_{2-x}Ce_xCuO_4$

(NCCO)



Theory predicts shift of the QPT point in SC phase? How strong is this shift?

Original FS:

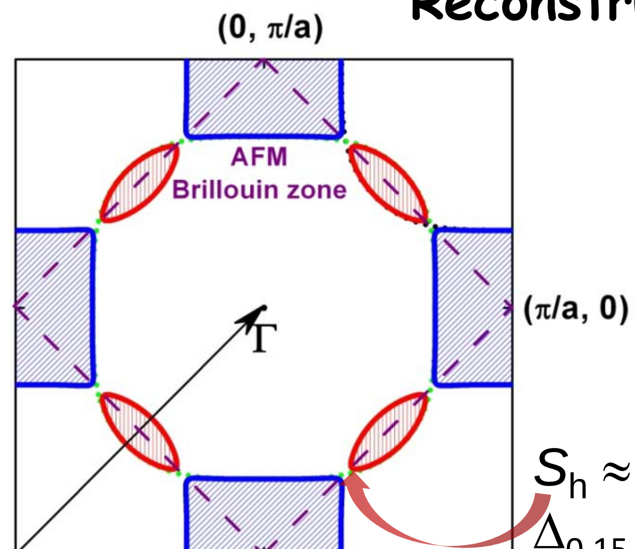


$\underline{n = 0.17}$

S_h = 41.5% of S_{BZ}

T. Helm, M. Kartsovnik et al., PRL 103, 157002 (2009)

Reconstructed FS:



$\underline{n = 0.15 \text{ and } 0.16}$

$S_h \approx 1.1\%$ of S_{BZ};

$\Delta_{0.15} \approx 64$ meV;

$\Delta_{0.16} \approx 36$ meV

Angular dependence of background magnetoresistance

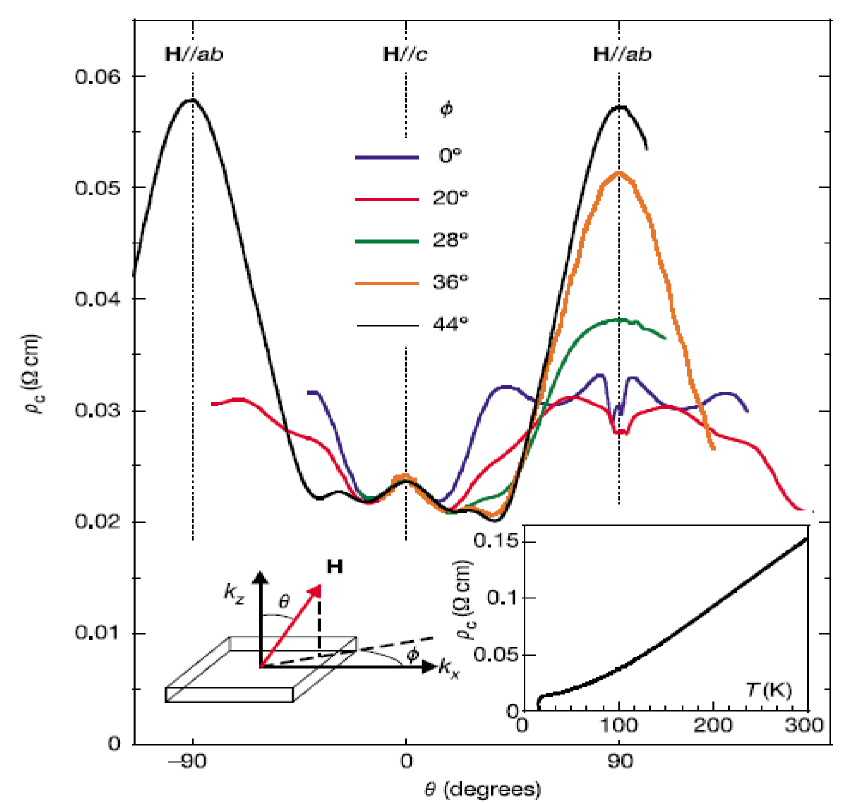
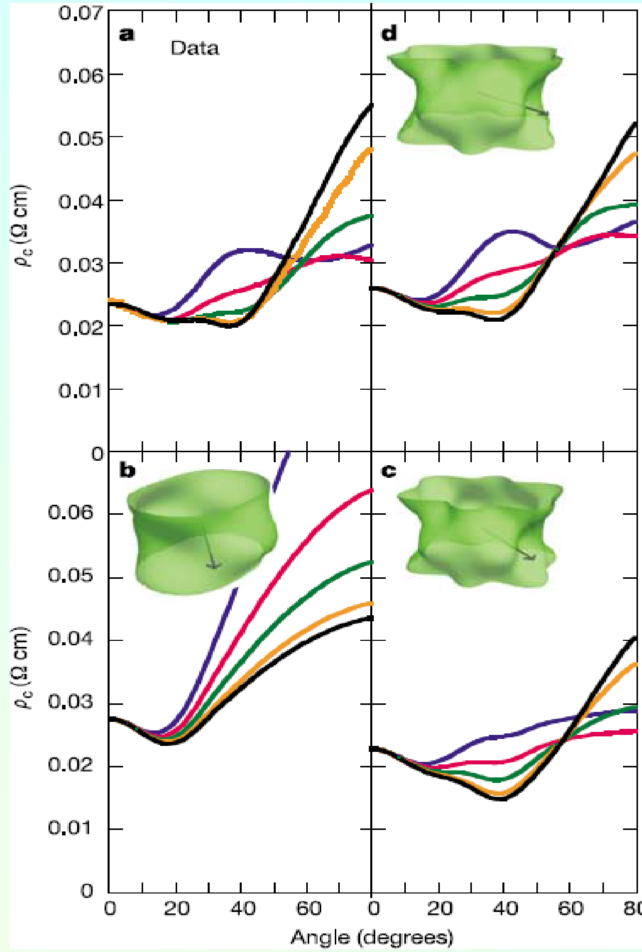


Figure 1 Polar AMRO sweeps in an overdoped Tl2201 single crystal ($T_c \approx 20$ K). The data were taken at $T = 4.2$ K and $H = 45$ T. The different azimuthal orientations (±4°) of each polar sweep are stated relative to the Cu–O–Cu bond direction. The key features of the data are as follows: (1) a sharp dip in $\rho_\perp$ at $\theta = 90°$ for low values of ϕ, which we attribute to the onset of superconductivity at angles where $H_{c2}(\phi, \theta)$ is maximal, (2) a broad peak around **H**||*ab* ($\theta = 90°$) that is maximal for $\phi \approx 45°$, consistent with previous azimuthal AMRO studies in overdoped Tl2201 (ref. 16), (3) a small peak at **H**||*c* ($\theta = 0°$), and (4) a second peak in the range $25° < \theta < 45°$ whose position and intensity vary strongly with ϕ. These last two features are the most critical for our analysis. Similar



Reconstruction of the FS in $Tl_2Ba_2CuO_{6+d}$ from polar AMRO data.

N. E. Hussey et al., "A coherent 3D Fermi surface in a high-Tc superconductor" Nature 425, 814 (2003)

AMRO experiment proved (for the first time) the existence of Fermi surface in cuprate high-Tc superconductors

Magnetoresistance studies of organic metals

There are very many papers on the study of electronic properties of organic metals using magnetoresistance measurements.

Some books:

1. J. Wosnitza, *Fermi Surfaces of Low-Dimensional Organic Metals and Superconductors* (Springer-Verlag, Berlin, 1996).
2. T. Ishiguro, K. Yamaji, and G. Saito, *Organic Superconductors*, 2nd ed. (Springer-Verlag, Berlin, 1998).
3. A.G. Lebed (ed.), *The Physics of Organic Superconductors and Conductors*, (Springer Series in Materials Science, 2009).

Some review papers:

1. **D. Jérome and H.J. Schulz, Adv. Phys. 31, 299 (1982).**
2. **J. Singleton, Rep. Prog. Phys. 63, 1111 (2000).**
3. **M.V. Kartsovnik, *High Magnetic Fields: A Tool for Studying Electronic Properties of Layered Organic Metals*, Chem. Rev. 104, 5737 (2004).**
4. **M.V. Kartsovnik , V.G. Peschansky, *Galvanomagnetic Phenomena in Layered Organic Conductors*, FNT 31, 249 (2005) [LTP 31, 185].**

Strong and weak points of magnetoresistance as a tool to study electronic properties

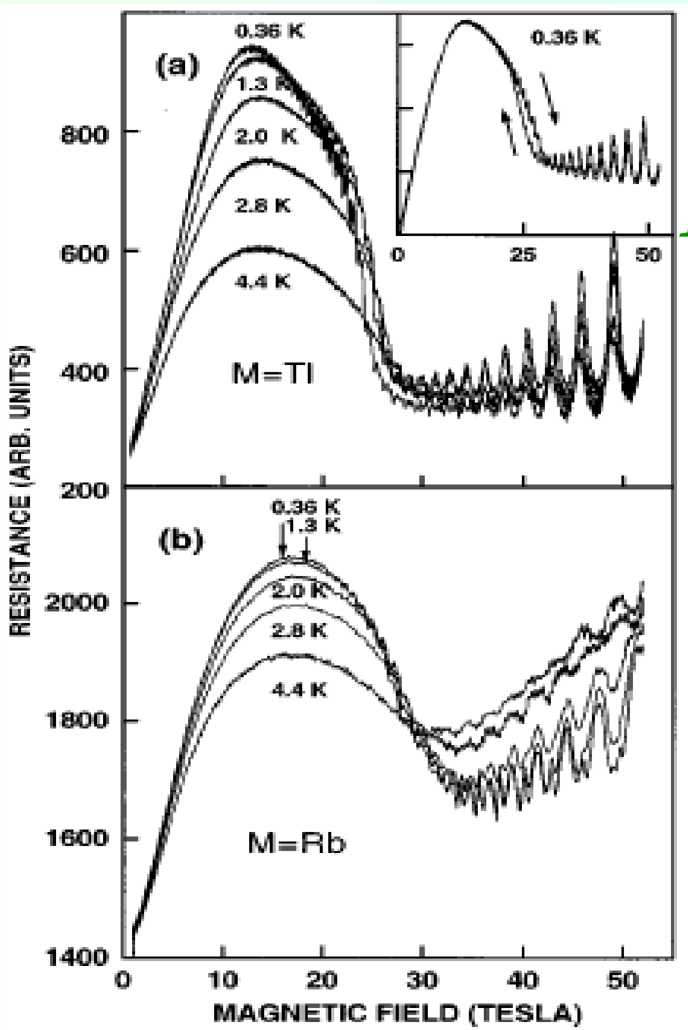
Strong point: high precision and availability

Weak point: requires reliable theoretical description

Therefore, any unusual/unexpected qualitative feature must be analyzed and understood

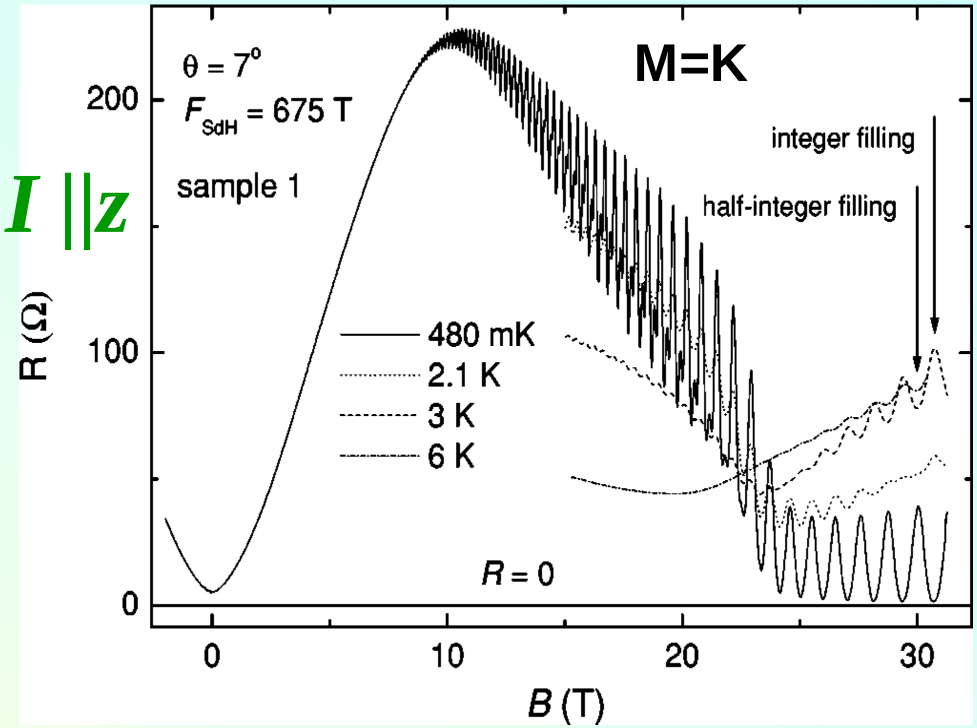
Experimental facts and motivation

Magnetoresistance in layered organic metal α-(BEDT-TTF)$_2$MHg(SCN)$_4$, (M=K,Tl,Rb,..)



R.H. McKenzie et al., PRB 54, R8289 (1996)

$B \parallel I \parallel z$



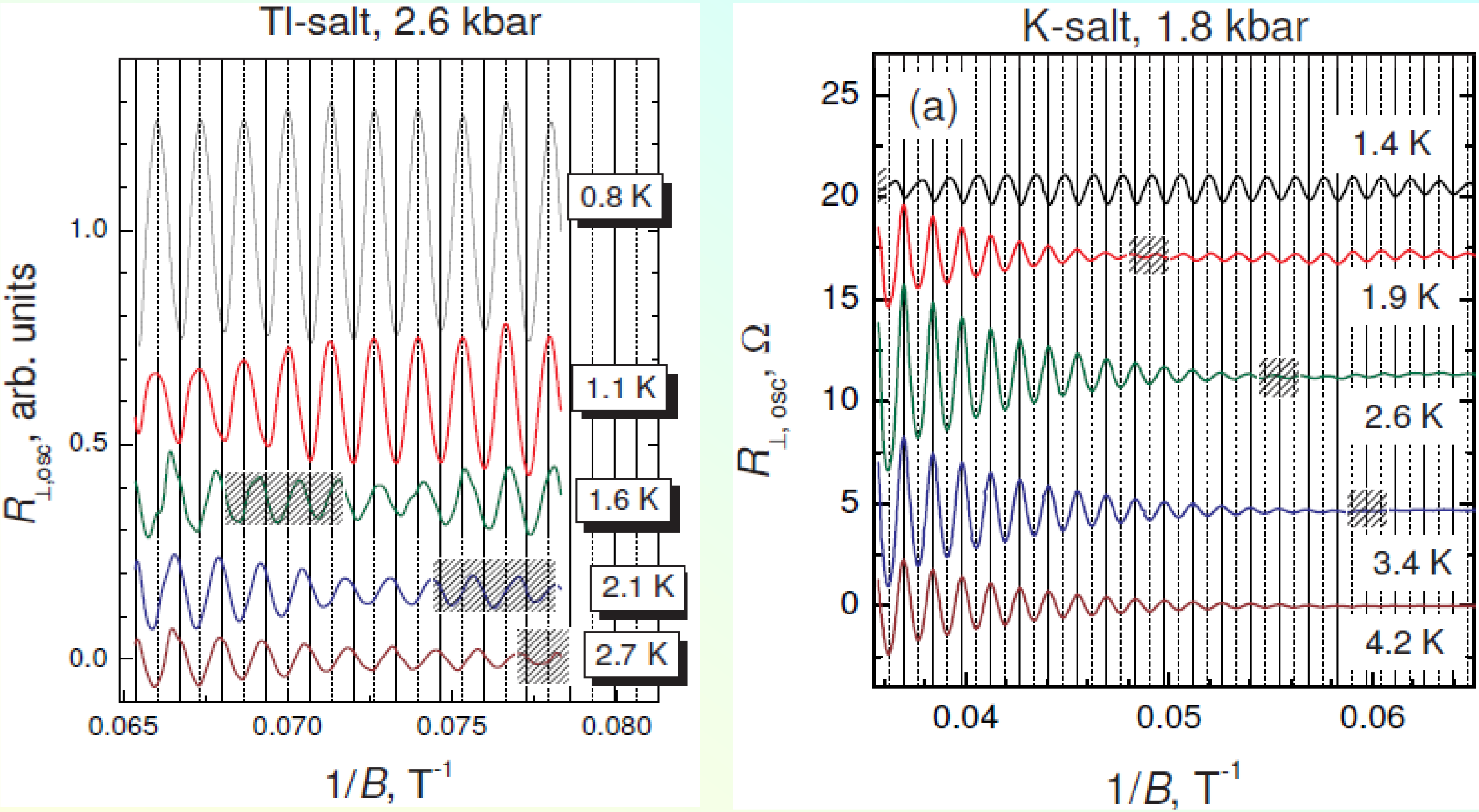
N. Harrison et al., PRB 62, 14 212 (2000)

Importnant experimental facts:

1. Hump on MR at B~12T
2. Phase inversion of Shubnikov - de Haas oscillations in CDW

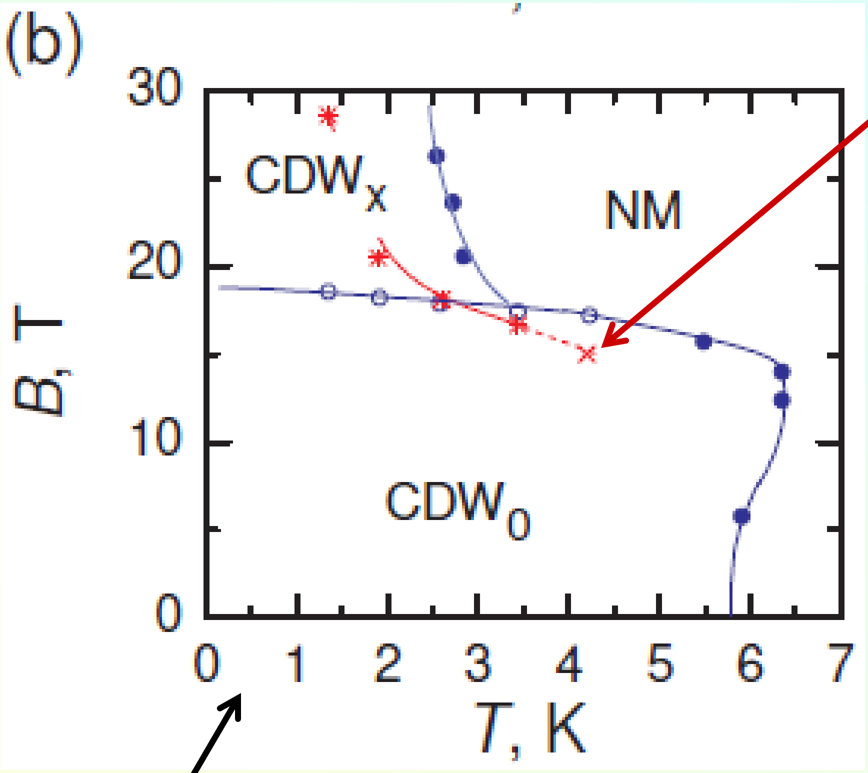
Phase inversion of Shubnikov –de Haas oscillations

Experimental data. The phase inversion is in the dashed region of B-T



Low Temp. Phys., 40(4), 377-383 (2014) [**arXiv:1311.5744**]

Phase diagram of α-(BEDT-TTF)$_2$KHg(SCN)$_4$ and the line of phase inversion of MQO



The phase inversion points * follow the CDW transition line

This suggest that the phase inversion of MQO is related to CDW transition, to CDW energy gap or to FS reconstruction

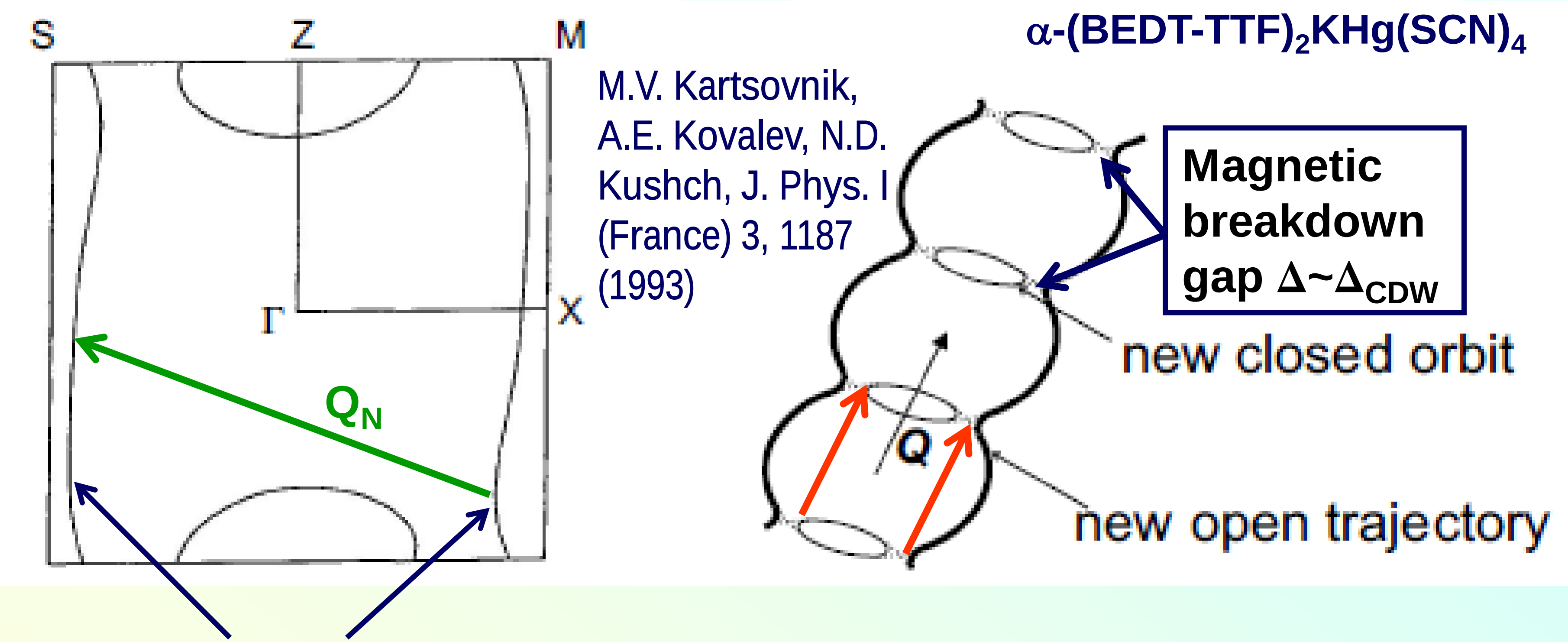
However, this phase inversion remained puzzling for decades

Ref: M.V. Kartsovnik, V.N. Zverev, D.Andres, W.Biberacher, T.Helm, P.D. Grigoriev, R.Ramazashvili, N.D. Kushch, H.Muller, Low Temp. Phys. 40(4), 377 (2014) [FNT 40(4), 484]; arXiv:1311.5744.

Fermi surface reconstruction by CDW

Original in-plane Fermi surface

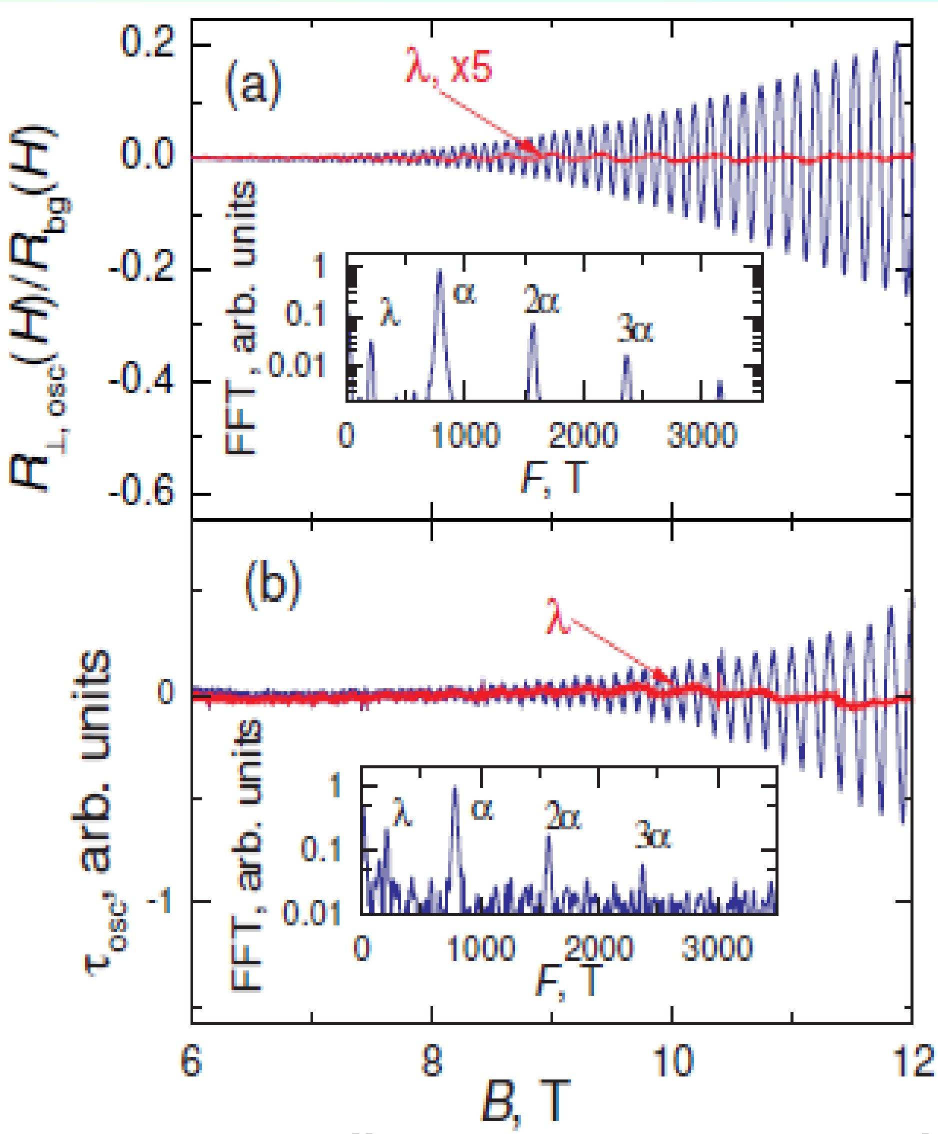
Reconstructed Fermi surface



The quasi-1D FS parts possess nesting property with vector Q and become gapped in the CDW state. The CDW creates periodic potential and the new Brillouin zone. The quasi-2D FS pockets then overlap and form reconstructed FS with new quasi-1D sheets and small 2D pockets.

Even 2D FS pockets, having no nesting property, become reconstructed by CDW on 1D parts!

The observed MQO support this FS reconstruction



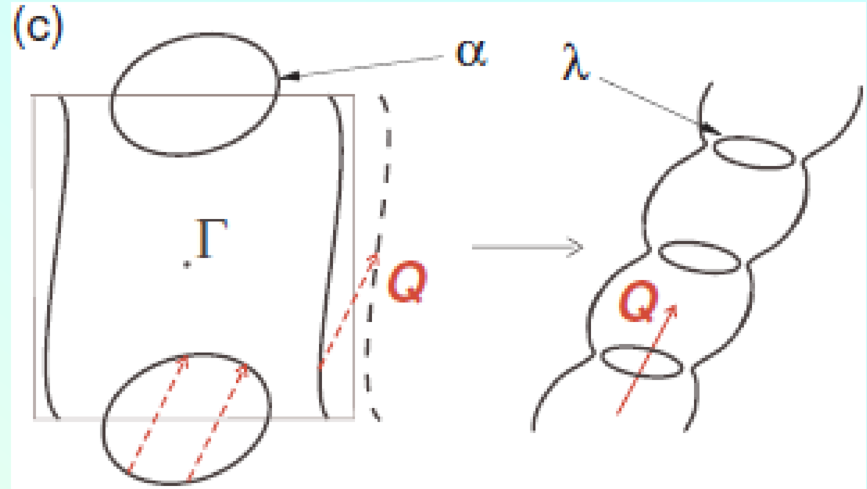
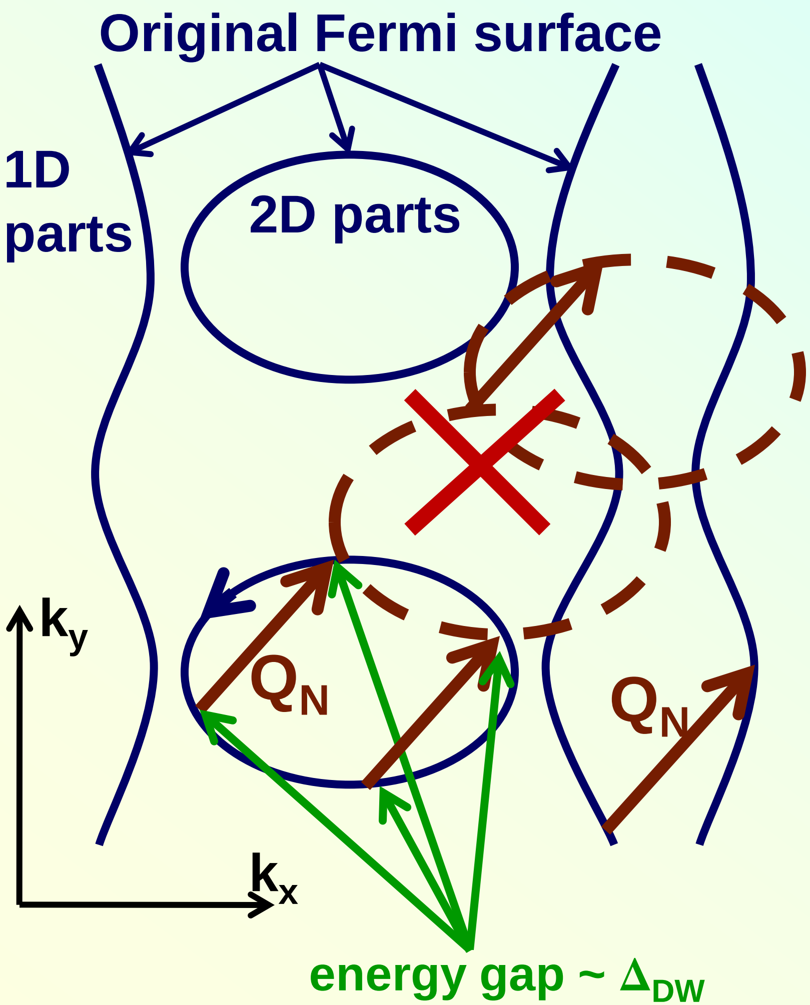


Figure 2. Oscillating components of the magnetoresistance (a) and magnetic torque (b) of the K-salt at $T = 0.45\,\mathrm{K}$, $\theta = 31.5°$. The red curves are obtained by filtering out the α-oscillations and demonstrate the behavior of the slow oscillations with frequency $F_\lambda = 210\,\mathrm{T}$. In (a) the λ-oscillations are magnified by a factor of 5, for a better visibility. The insets in (a) and (b) show the corresponding fast Fourier spectra. (c) Schematic 2D view of the Fermi surface reconstruction due to the CDW potential with the wave vector Q. The original Fermi surface (left panel) consists of a pair of open sheets and a cylinder. The CDW, introducing a new periodicity with the wave vector Q, opens a gap at the Fermi level in the whole q1D band as well as in the q2D band at the states separated by Q (right panel).

M.V. Kartsovnik, V.N. Zverev, .. , P.D. Grigoriev, R.Ramazashvili, N.D. Kushch, H.Muller, Low Temp. Phys., 40(4), 377 (2014) [FNT 40(4), 484]; arXiv:1311.5744

Reconstruction of FS is weak, but the electron trajectories strongly change in the momentum space



No additional parts of FS are created by density wave!

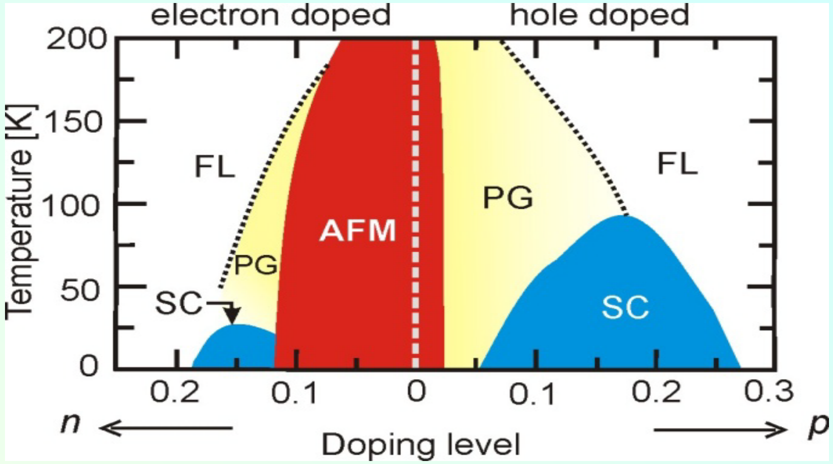
Only small energy gap is formed at the boundaries of new Brillouin zone However, this gap strongly changes the electron trajectories, e.g., from closed (2D) to open (1D).
The electrons just scatter by Q_N to the same FS part.

Even electron trajectories from 2D FS pockets, having no nesting property, become reconstructed by CDW to open 1D trajectories!

FS reconstruction in high-Tc cuprates (just another example)

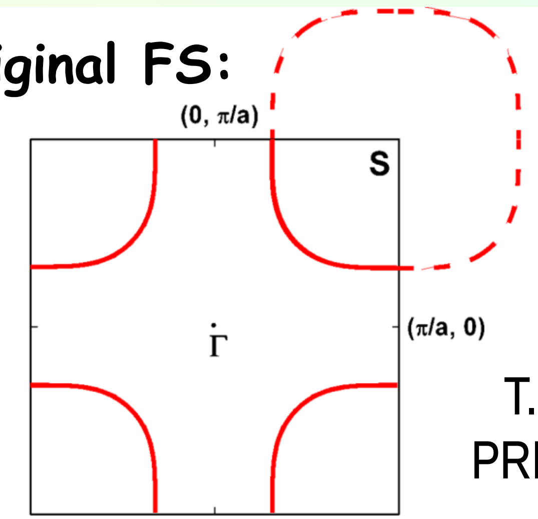
$Nd_{2-x}Ce_xCuO_4$

(NCCO)



! The Fermi-surface reconstruction is <u>very common</u> and can be easily seen by MQO

Original FS:

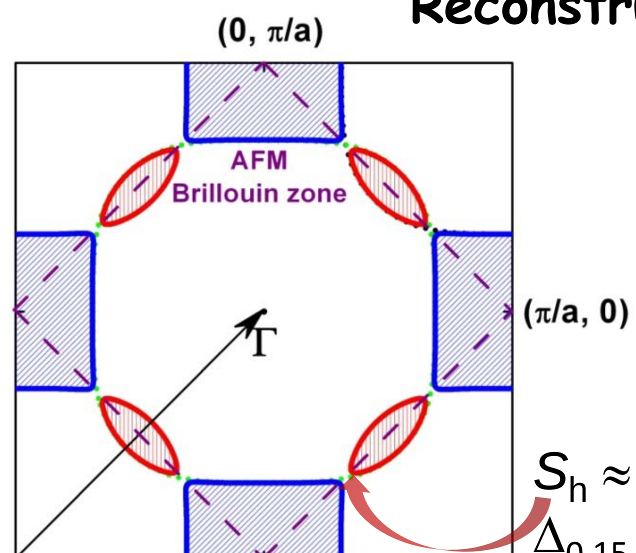


<u>n = 0.17</u>

S_h = 41.5% of S_{BZ}

T. Helm et al., PRL 103, 157002 (2009)

Reconstructed FS:



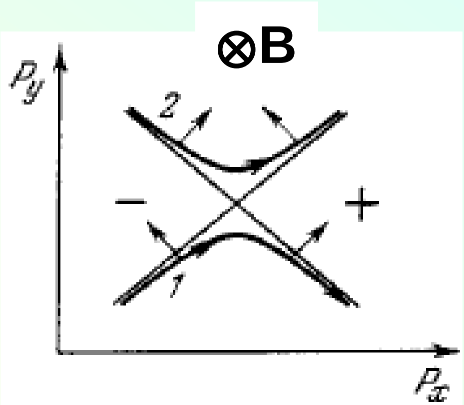
<u>n = 0.15 and 0.16</u>

$S_h \approx$ 1.1% of S_{BZ};

$\Delta_{0.15} \approx$ 64 meV;

$\Delta_{0.16} \approx$ 36 meV

Theory of magnetic breakdown (MB)



The 2D scattering matrix between the states 1 and 2

$$\hat{S} = \begin{pmatrix} \sqrt{1-W}\,e^{i\Lambda}, & -\sqrt{W} \\ \sqrt{W}, & \sqrt{1-W}\,e^{-i\Lambda} \end{pmatrix}$$

where the MB probability $W = \exp\{-H_0/H\}$

the MB field $H_0 \sim \Delta^2/E_F$ is much smaller than gap!

$(B_{MB} \sim \Delta^2 m_c/\hbar e E_F)$ The MB phase $\Lambda = \dfrac{\pi}{4} + \dfrac{H_0}{\pi H} - \dfrac{H_0}{\pi H}\ln\dfrac{H_0}{\pi H} + \arg\Gamma\left(i\dfrac{H_0}{\pi H}\right)$

Remark: the MB field H_0 can be calculated with coefficient:

If one takes the electron dispersion at the MB point in a general form as

$$\varepsilon_{1,2}(p) = \varepsilon_M + v_M\,\delta p_n + \sqrt{\Delta^2/4 + (v_{1,2}^M\,\delta p_n)^2},$$

$$\varepsilon_M = \tfrac{1}{2}[\varepsilon_1(p_M) + \varepsilon_2(p_m)], \quad \delta p_n = n_M(p - p_M)$$

$$v_M = \tfrac{1}{2}(v_{11}^M + v_{22}^M), \quad \Delta = \Delta(p_M) = \varepsilon_1(p_M) - \varepsilon_2(p_M);$$

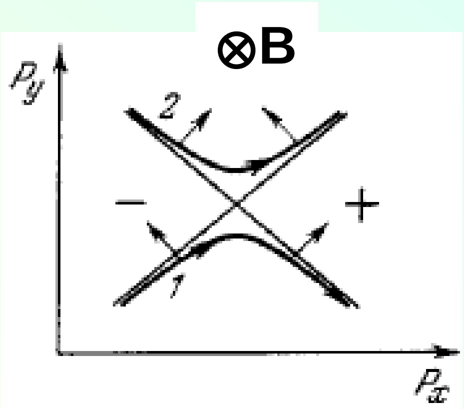
The MB field H_0 then

$$H_0 = \frac{c\pi\Delta^2}{e\hbar\,|v_x v_{12}\cos\theta|}$$

M.I. Kaganov, A.A. Slutskin, Phys. Reports 98, 189 (1983)

Idea:

Origin of MB scattering mechanism



The 2D scattering matrix between the states 1 and 2

$$\hat{S} = \begin{pmatrix} \sqrt{1-W}\, e^{i\Lambda}, & -\sqrt{W} \\ \sqrt{W}, & \sqrt{1-W}\, e^{-i\Lambda} \end{pmatrix}$$

where the MB probability $W = \exp\{-H_0/H\}$

the MB field $H_0 \propto \Delta^2/E_F$ is << DW gap!

Uniform MB, though strongly scatters conducting electrons, does not lead to the momentum relaxation along field because does not break the spatial uniformity (which gives momentum conservation).

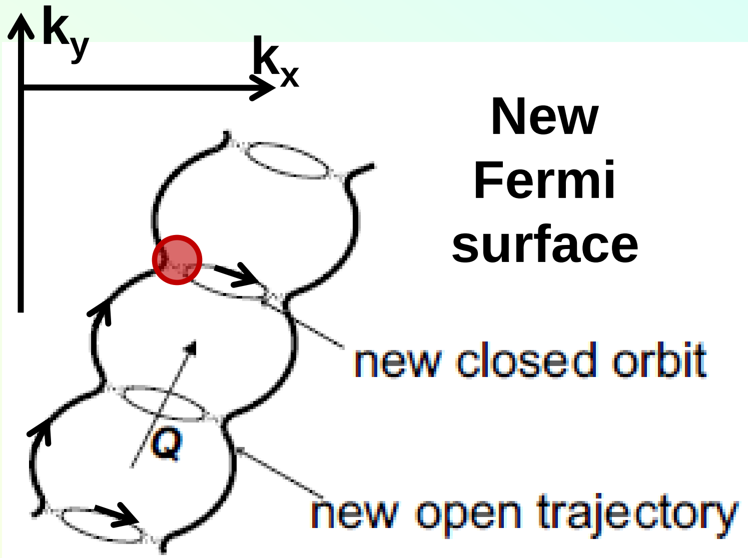
Idea: non-uniform MB may give the electron momentum relaxation!

If a local MB defect scatters an electron differently from uniform MB, it also changes electron momentum along magnetic field => new scattering mechanism

The weak spatial fluctuations of CDW gap Δ (CDW defects or solitons) result to strong fluctuations of the MB probability (due to FS reconstruction).

MB defects are not scattering potential, but variations of scattering matrix. They are strong because corresponding change of MB probability is ~1

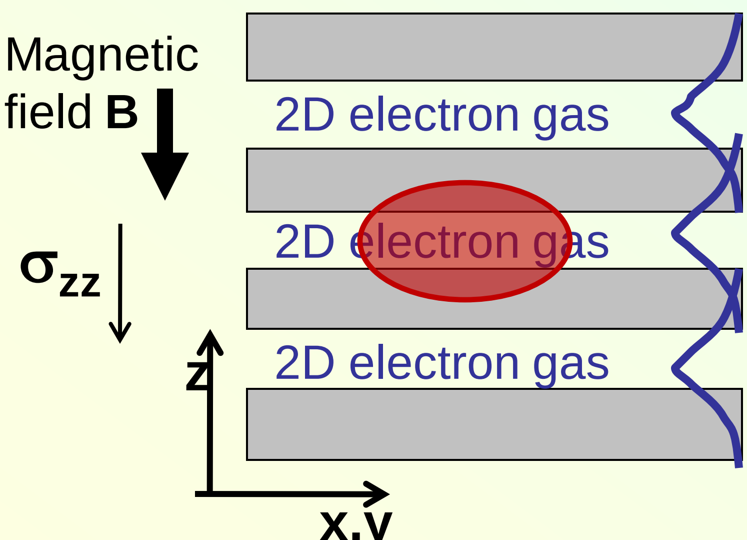
Local change of MB probability as a scattering center for conducting electrons



New electron spectrum contains two types of electron states or 2 bands:

1) non-quantized quasi-1D states
2) 2D states, giving Landau levels

The scattering from normal impurities to all states at the same energy is $\propto \rho_{tot}$



Assume the MB probability W≅0 everywhere except the MB defect spots (red), where W≅1. And these defects are localized in z-direction, so that they scatter to any p_z. Then they act as scattering centers!

The MB defects scatter electrons between the two bands 1D ↔ 2D

Phase inversion of Shubnikov –de Haas oscillations

The phase inversion comes because the MB scattering is non-diagonal between the FS parts (or, the electron spectrum parts). The defects, increasing the MB amplitude (local reduction of the DW gap), scatter mainly to 2D parts (quantized electron spectrum): $1/\tau_{\mathrm{MB}} \propto \rho_{2D}\left(E_{\mathrm{F}}\right)$

In τ–approximation electron conductivity

$$\sigma_{zz} = 2e^2\tau_{tot}\sum_{\boldsymbol{k}} v_z^2\left(\boldsymbol{k}\right)\left(-n_F'\left[\varepsilon_{1D}\left(\boldsymbol{k}\right)\right]\right)$$

where the total scattering rate is a sum of MB and impurity contributions:

$$1/\tau_{tot} = 1/\tau_{\mathrm{MB}} + 1/\tau_i$$

When both 1D and 2D parts

$$\sigma_{zz} \propto \frac{\langle v_{z1D}^2\rangle\,\rho_{1D}\left(E_{\mathrm{F}}\right) + \langle v_{z2D}^2\rangle\,\rho_{2D}\left(E_{\mathrm{F}}\right)}{\rho_{2D}\left(E_{\mathrm{F}}\right)}.$$

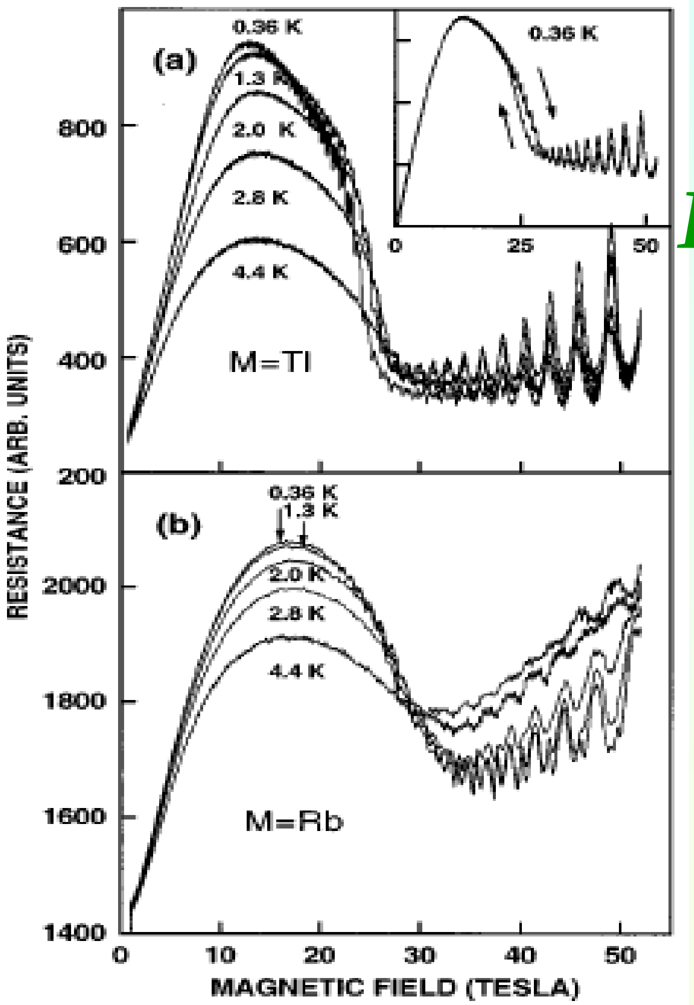
$$\left\langle v_{z\,2D}^2\right\rangle\left(\epsilon\right) \approx \left\langle v_{z\,1D}^2\right\rangle\left[1 - 2\alpha R_D\cos\left(2\pi\epsilon/\hbar\omega_c\right)\right], \quad \left\langle v_{z\,1D}^2\right\rangle \approx 2t_\perp^2 d^2/\hbar^2$$

The conductivity

$$\boxed{\sigma_{zz} \propto const + \left(\frac{\rho_{1D0}}{\rho_{2D0}} - \alpha\right)2R_D\cos\left(2\pi F/B\right)}$$

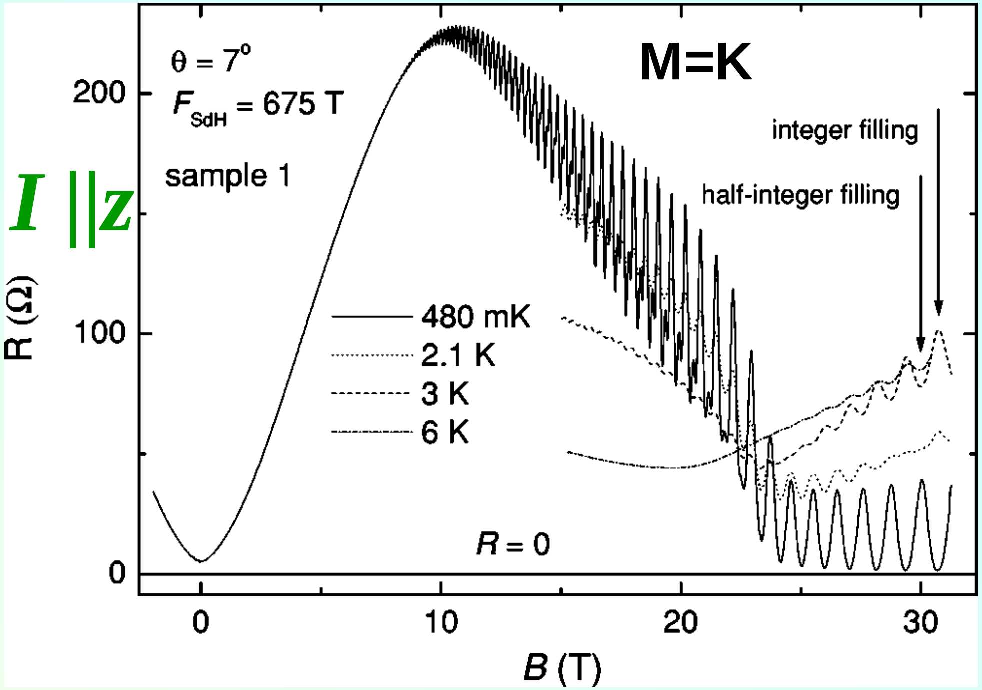
The MQO amplitude changes sign !

Magnetoresistance in layered organic metal α-(BEDT-TTF)$_2$MHg(SCN)$_4$, (M=K,Tl,Rb,..)



R.H. McKenzie et al., PRB 54, R8289 (1996)

$B \parallel I \parallel z$



N. Harrison et al., PRB 62, 14 212 (2000)

The observed increase of MR at B~5-20T~H_0 may be due to this new scattering mechanism on MB defects

This mechanism is rather general !

Increased resistivity at MB field H_0 shows the CDW defects

Conclusions

The magnetoresistance studies in the density-wave state must take into account additional scattering mechanism from non-uniform MB, which is rather general and depends on DW non-uniformities/defects. This mechanism explains the phase inversion of MQO and MR hump observed in organic metal α-(BEDT-TTF)$_2$MHg(SCN)$_4$

<u>Brief description of this scattering mechanism</u>:

Density wave (DW) with imperfect nesting leads to Fermi-surface (FS) reconstruction.
The DW energy gap $\mathbf{\Delta << E_F}$ separates close electron trajectories in momentum space. Hence, the magnetic-breakdown (MB) field $\mathbf{B_{MB} \propto \Delta^2/E_F}$ is easily achieved, which leads to the electron jumps between close classical trajectories

In the crossover regime $\mathbf{B \sim B_{MB}}$, weak spatial non-uniformities of $\mathbf{\Delta}$ strongly change the local MB amplitude, producing additional scattering of conducting electrons.
This leads to magnetoresistance (MR) maximum at $\mathbf{B \sim B_{MB}}$ even at $\mathbf{B || J}$, and sometimes to phase inversion of the Shubnikov-de Haas oscillations, e.g. as in α-(BEDT-TTF)$_2$MHg(SCN)$_4$.
The cleaner sample is, the stronger is this MR increase due to new scattering mechanism.

Thank you for attention !

Shubnikov – de Haas oscillations in 3D and 2D metals

MQO of conductivity in 3D metals mainly come from the oscillations of electron mean free time $\tau \sim 1/\rho(E_F)$. The DoS $\rho(E_F)$ oscillates because of Landau level quantization.

$$\sigma_{zz}^{3D} = e^2 \tau \sum_{FS} v_z^2,$$

where in the Born approximation the scattering rate is given by golden Fermi rule:

$$1/\tau = \frac{2\pi}{\hbar} n_i |v|^2 \boxed{\int dp_z \sum_n \delta(\varepsilon(n, p_z) - \mu) \frac{eH/c}{(2\pi\hbar)^2}}.$$

DoS

So, in 3D conductivity is inversely proportional to the DoS,

because oscillations of scattering rate $1/\tau$ dominate oscillations of mean square electron velocity averaged over FS.

In 2D maxima of conductivity coincide with DoS maxima,

because between the LLs there is no electron states to conduct =>

the phase of Shubnikov-de Haas oscillations in 2D and 3D differs by π

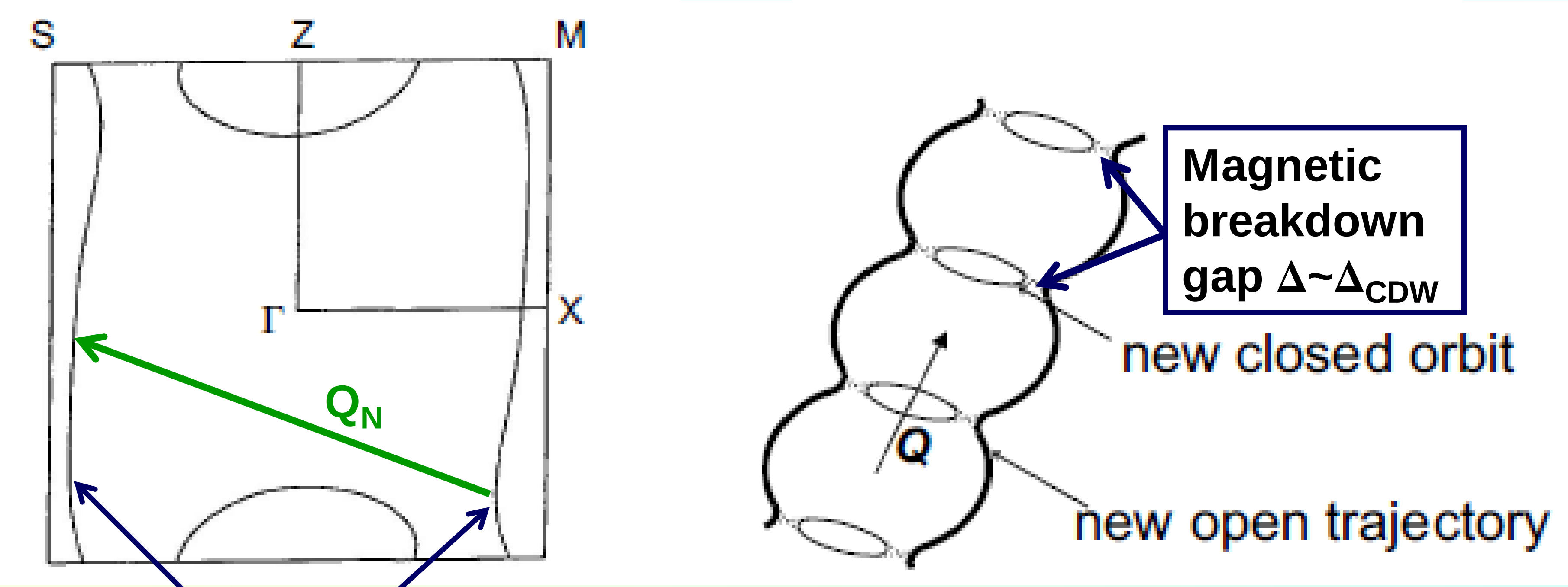
$\Rightarrow$ 2D and 3D cases are not described by the same formula!

$\Rightarrow$ There is a phase inversion as we go from 3D to 2D case.

Fermi surface reconstruction by CDW

Original in-plane Fermi surface

Reconstructed Fermi surface



The quasi-1D FS parts possess nesting property with vector Q and become gapped in the CDW state. The CDW creates periodic potential and the new Brillouin zone. The quasi-2D FS pockets then overlap and form reconstructed FS with new quasi-1D sheets and small pockets

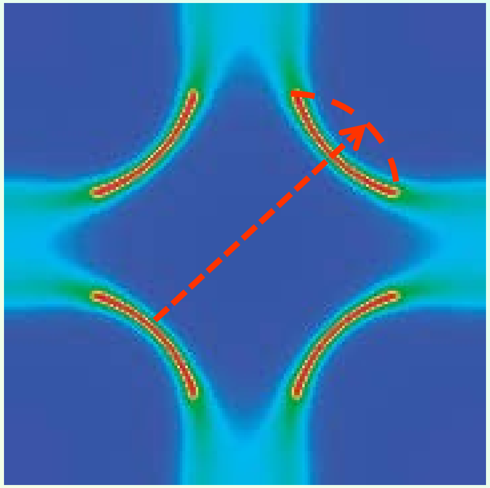
For α-(BEDT-TTF)$_2$KHg(SCN)$_4$ this FS reconstruction was first proposed in
M.V. Kartsovnik, A.E. Kovalev, N.D. Kushch, J. Phys. I (France) 3, 1187 (1993)

Difficulty:

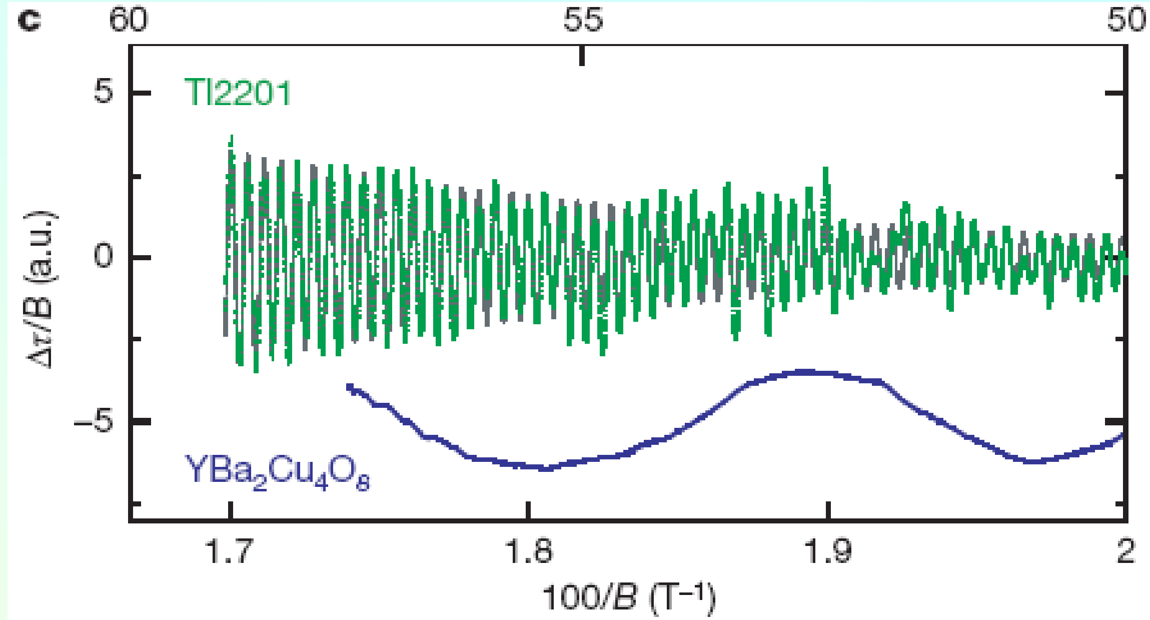
Spatially uniform magnetic breakdown does not lead to electron momentum relaxation along B and to longitudinal MR,
because the spatial uniformity is not broken, giving momentum conservation.

Hence, it does not increase R_{zz} !

Quantum oscillations from Fermi arcs



ARPES image plot



T. Pereg-Barne et al., Nature Physics 6, 44 - 49 (2009)

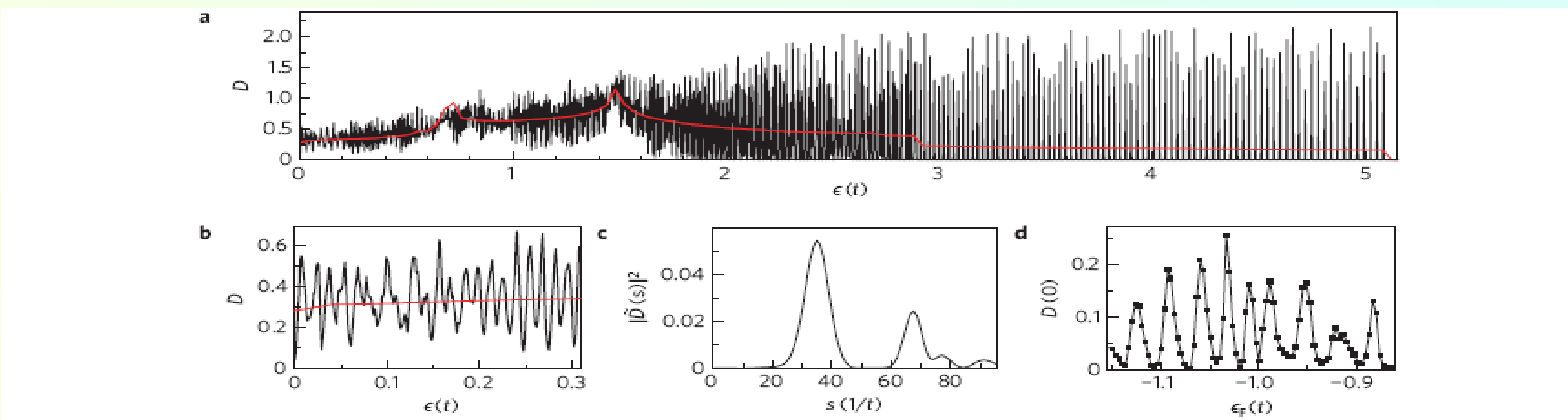


Figure 4 | Exact diagonalization of the lattice model. a, DOS as a function of energy in the FAM in zero (red) and non-zero (black) magnetic field corresponding to two vortices in a 20 × 20 magnetic unit cell. In YBCO with lattice constant $a_0 \simeq 4$Å this corresponds to the physical field of about 64 T. The parameters used are as follows: $\Delta_0/t = 1$, $\epsilon_F/t = -1.3$, $\nu = 0.6$ and $\tau = 0.1$. **b**, The low-energy DOS for the same parameters, in detail. **c**, The power spectrum of the low-energy DOS showing dominant frequency of oscillations $34t^{-1}$ and its second harmonic. **d**, DOS at the Fermi level as a function of ϵ_F.

PRL 101, 216402 (2008) PHYSICAL REVIEW LETTERS week ending 21 NOVEMBER 2008

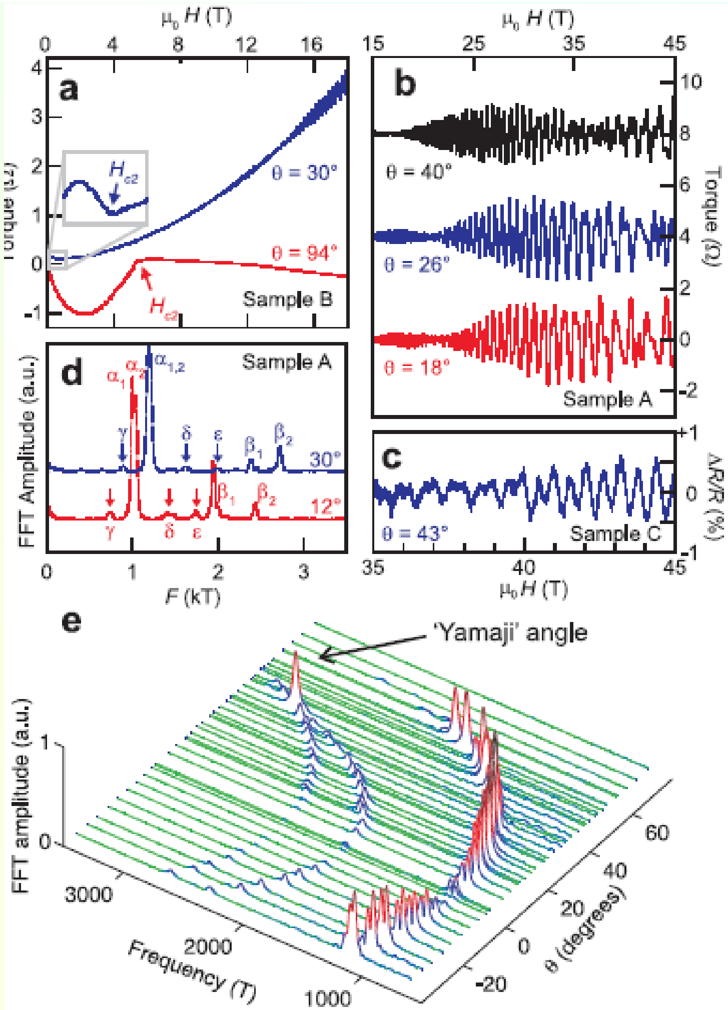
Motivation

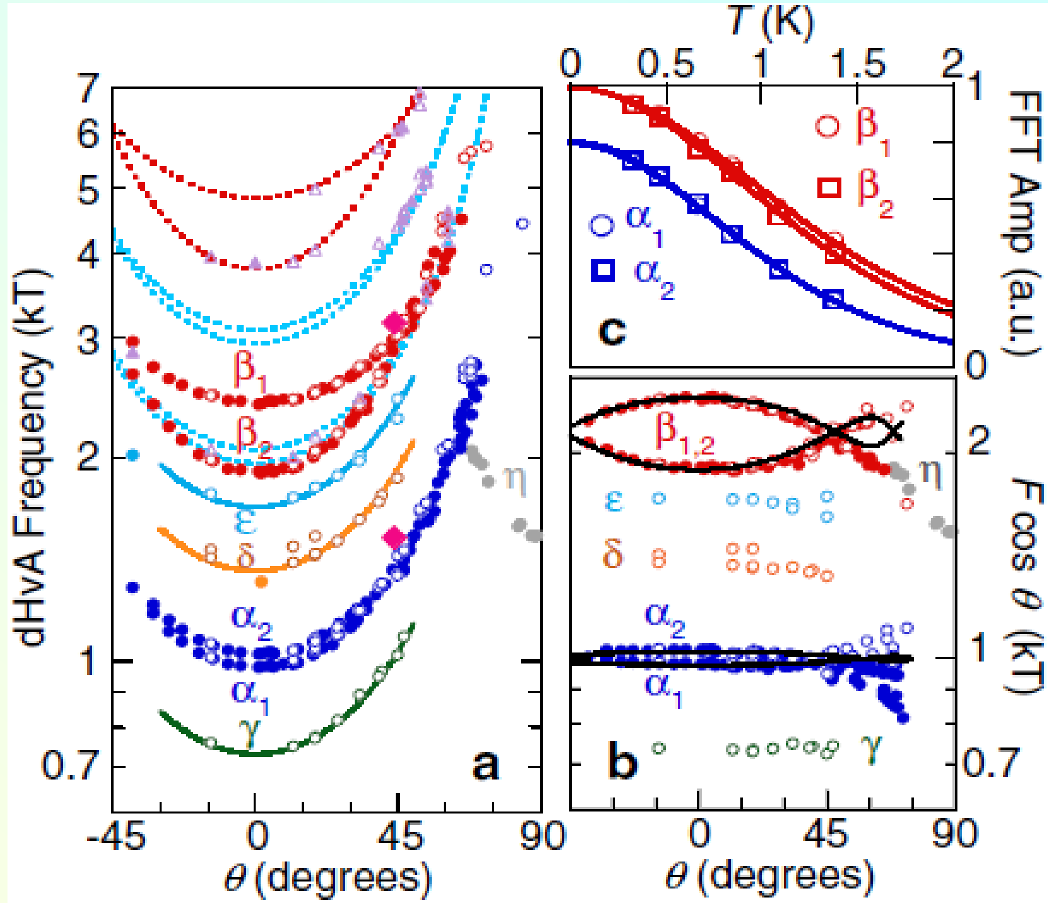
Fermi Surface of Superconducting LaFePO Determined from Quantum Oscillations

A. I. Coldea,[1] J. D. Fletcher,[1] A. Carrington,[1] J. G. Analytis,[2] A. F. Bangura,[1] J.-H. Chu,[2] A. S. Erickson,[2] I. R. Fisher,[2] N. E. Hussey,[1] and R. D. McDonald[3]

M8

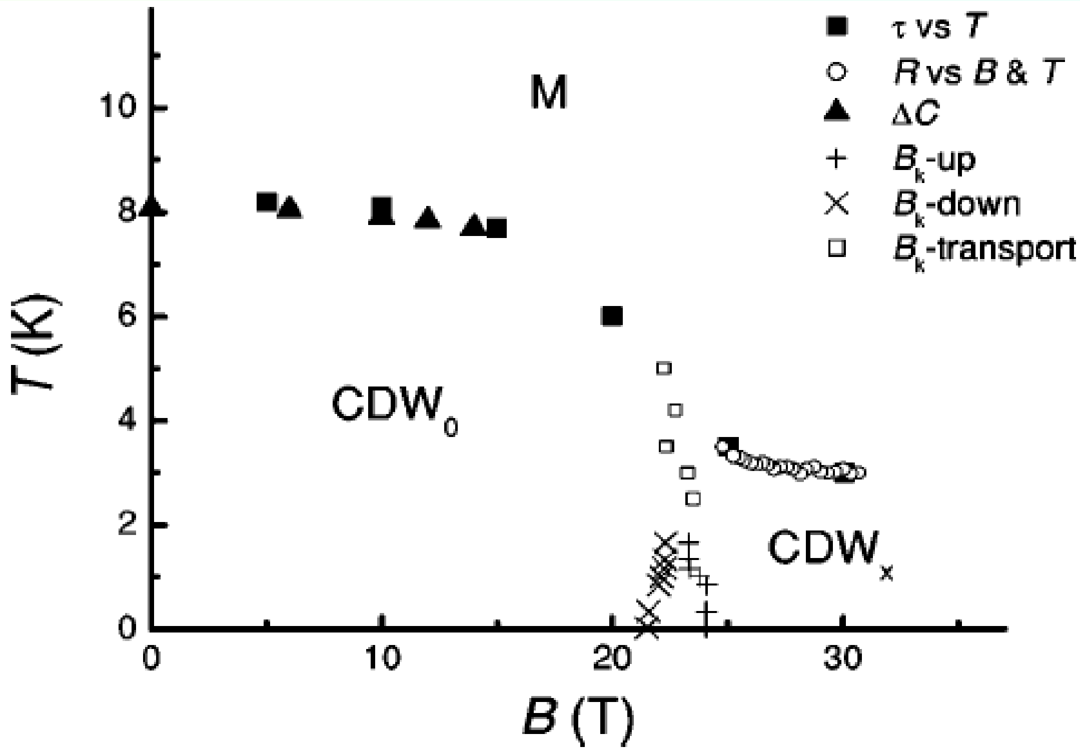
Experiments on MQO in high-Tc





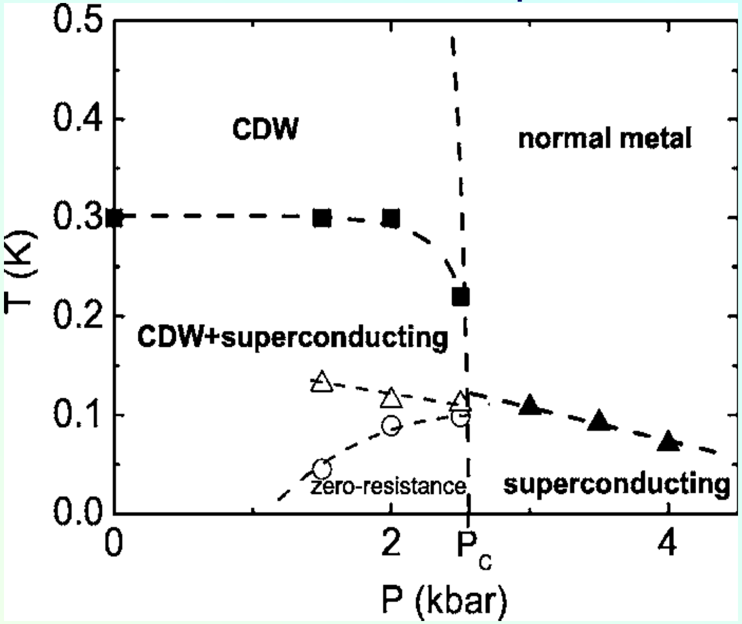
Phase diagram of α-$(BEDT\text{-}TTF)_2KHg(SCN)_4$

High magnetic field destroys CDW_0 by the Zeeman splitting and the non-uniform CDW_x is formed at $B>B_c$ with lower T_c :



N. Harrison et al., PRB 62, 14212 (2000)

Pressure also damps CDW:



D. Andres et al., PRB 72, 174513 (2005)

Conclusions

1. The magnetoresistance studies in the density-wave state must take into account additional scattering mechanism from non-uniform MB, which is rather general and depends on DW non-uniformities/defects.

2. MR measurements can reveal the defects of DW order parameter. These defects lead to the increase of longitudinal MR at field $B{\sim}H_0$. The cleaner sample is, the stronger is this MR increase. Such increase of MR at is very general and may appear in other DW and even in AFM ordered systems: heavy fermion and high-Tc superconducting materials.

3. In quasi-2D layered compounds DW defects may also lead to the phase inversion of MQO of conductivity.

Thank you for attention !