

# Moire-Wigner-Mott Freezing in TMD Heterobilayers

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Florida State University



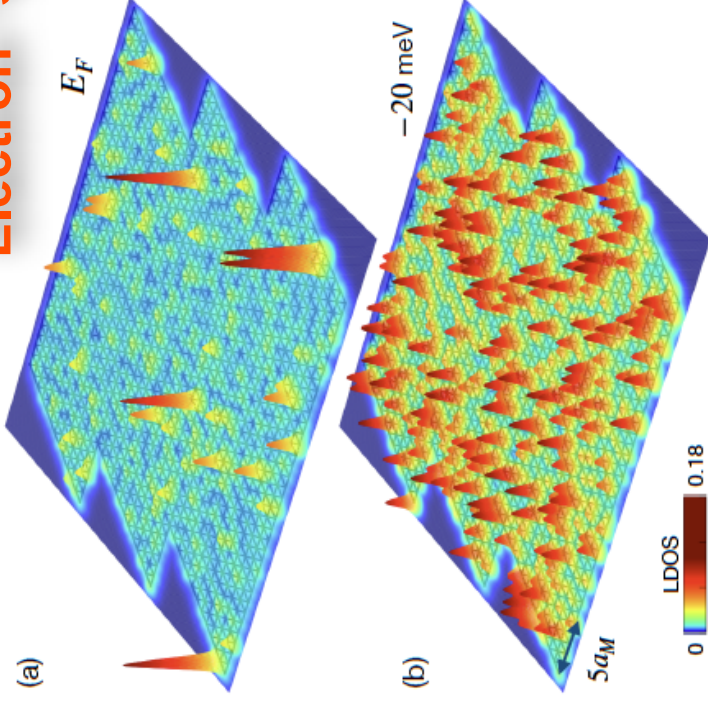
Collaborators:

**Yuting Tan** (FSU)

**Pak-Ki (Henry) Tsang** (FSU)

**Louk Rademaker** (Geneva)

**Electron “slush”**



Funding:

**NSF grants:**

**DMR-1822258**

**DMR-1410132**

...



# Mechanisms for Localization?

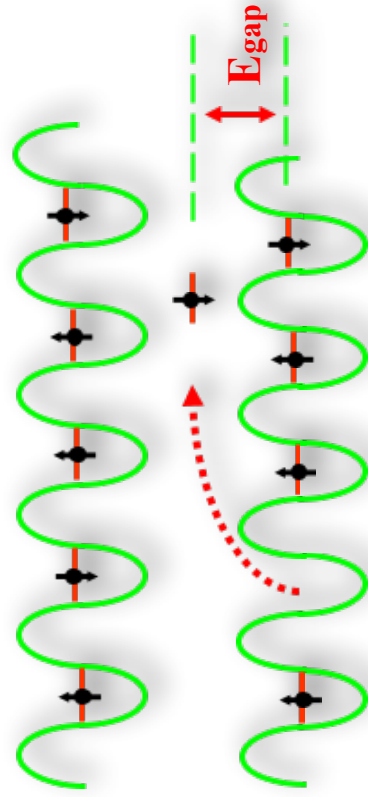


Sir Neville Mott:  
**interaction**

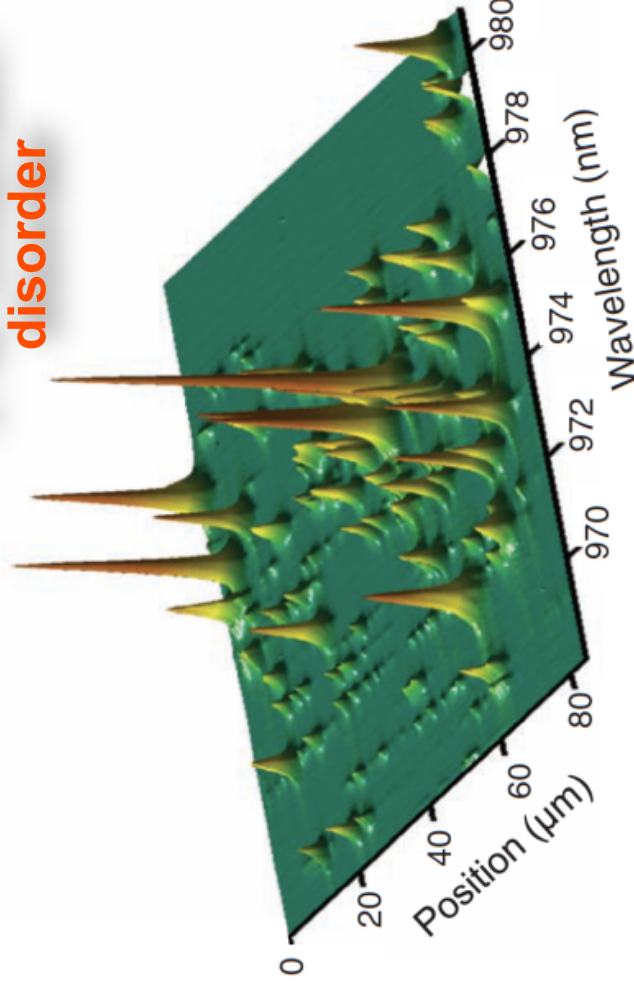
## Friend or Foe???



P. W. Anderson:  
**disorder**



Do correlations increase or weaken  
**(screen) disorder?**

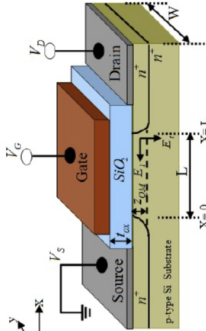




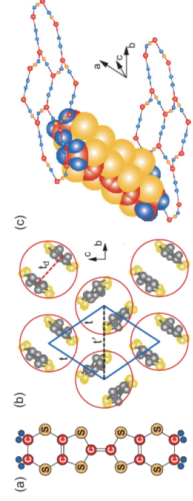
# Model Mott systems

(Strong interactions - half-filled narrow bands)

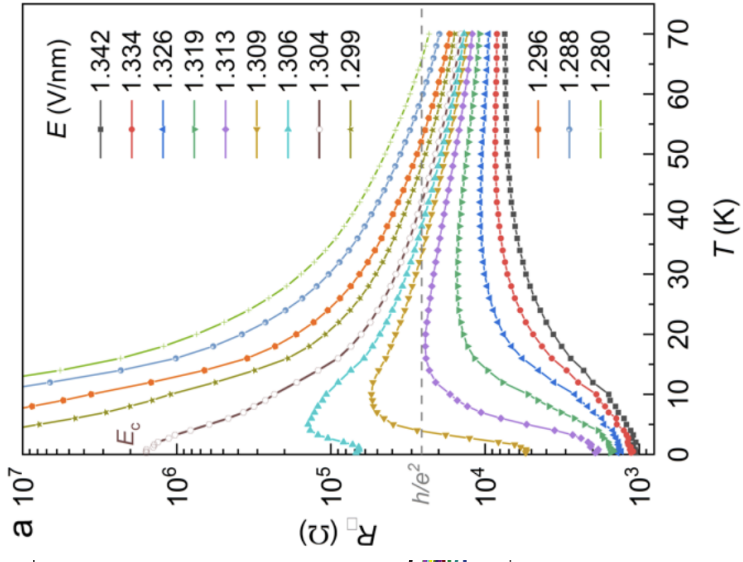
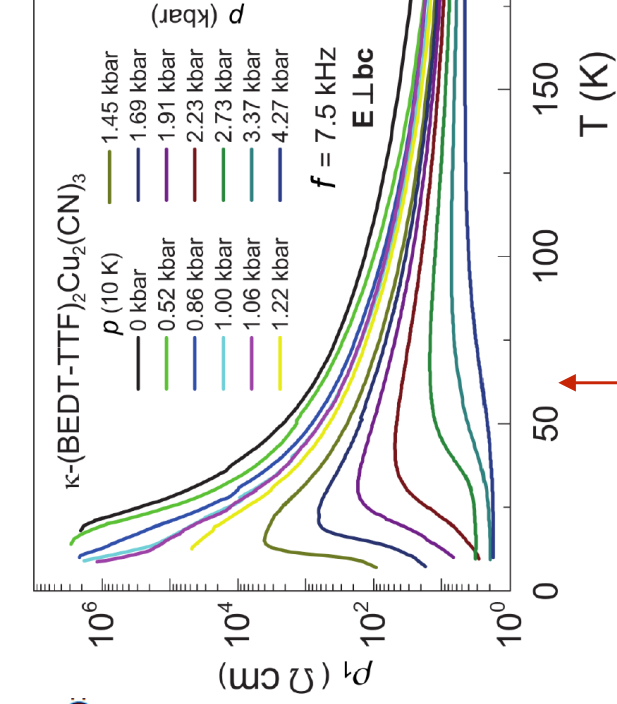
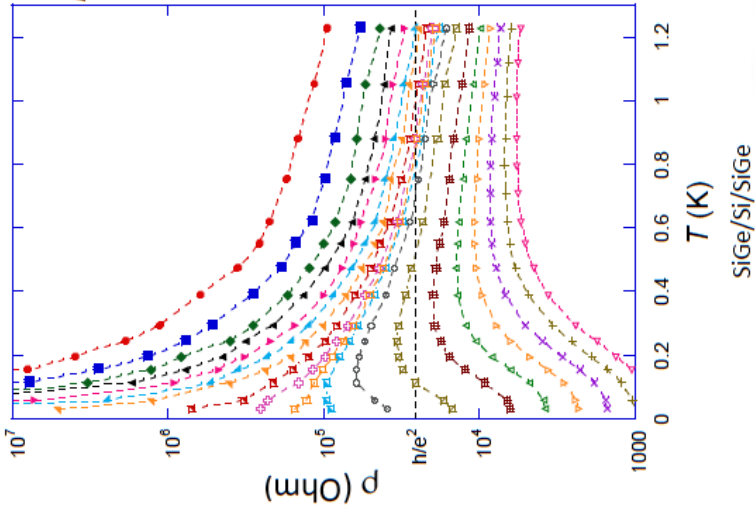
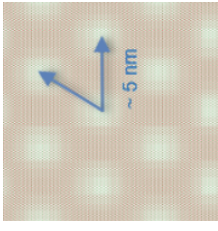
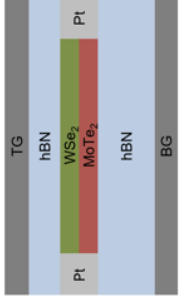
**2DEG in Si/SiGe**  
(Kravchenko, 1995-2021)



**Mott organics**  
(Kanoda, 2005)



**Moire TMDs**  
(Shan, Mak, 2021)



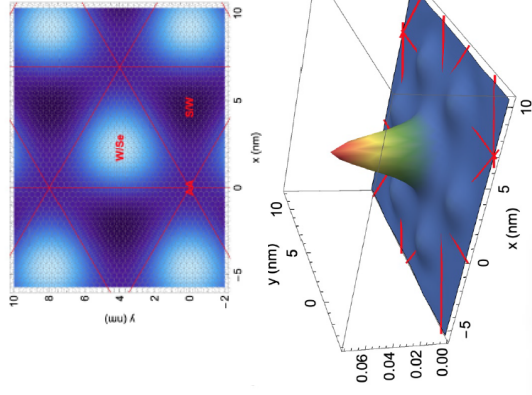
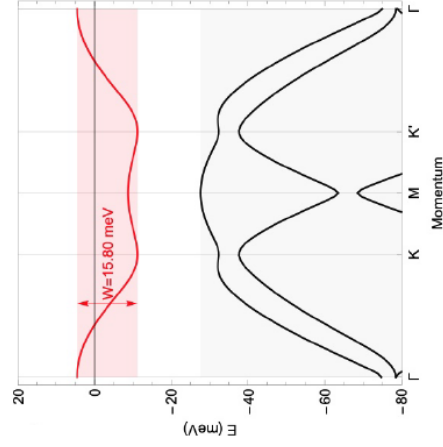
**Almost the same!**

See: Y. Tan, V. D., L. Rademaker, Crystals 2022, 12(7) 932; arXiv:2206.02055

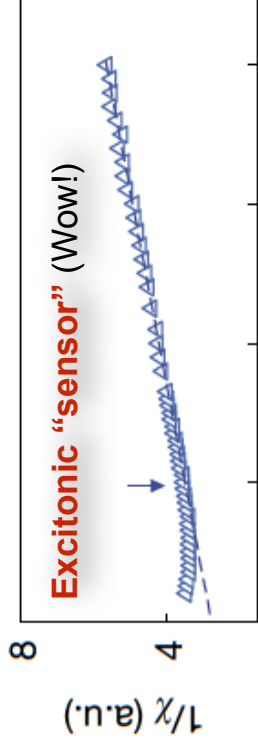
# TMD moire bilayers: Mott and beyond!

- tuning of bandwidth and band filling -

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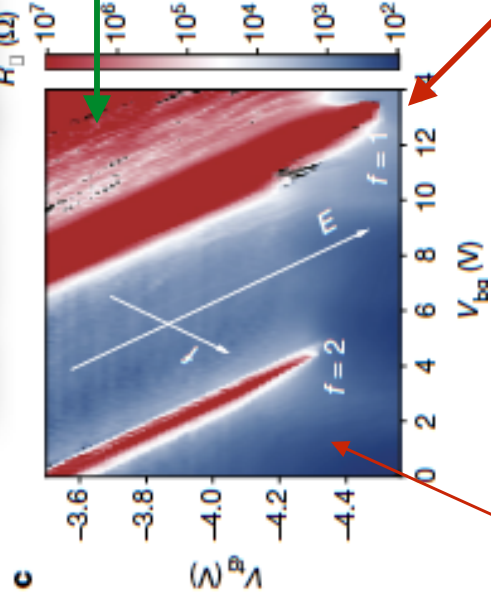
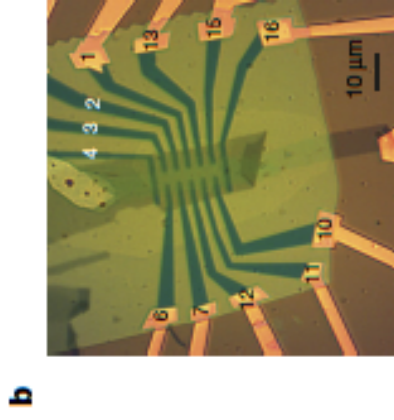
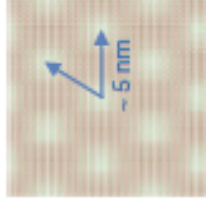
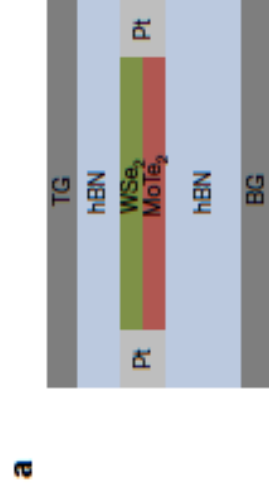


(Shan & Mak, Cornell)



## Tuning band width via electric field

Local moment magnetism at  $f=1$  (half filling)



Wigner-Mott?  
( $0 < f < 1$ )

Mott insulator  
( $f = 1$ )

Band insulator  
( $f = 2$ )

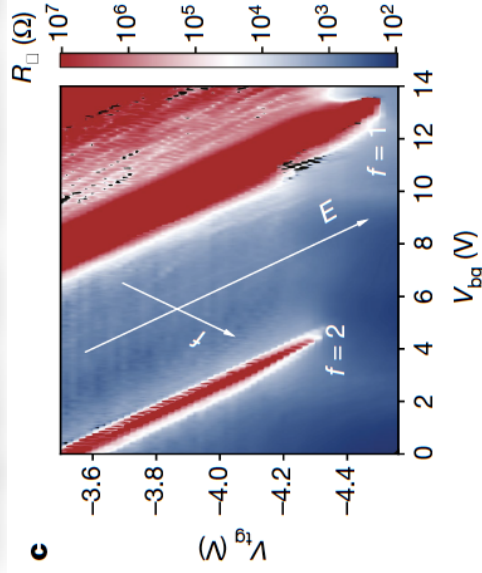
# CPA+DMFT theory: quantum critical scaling for disorder-driven MIT in moire devices (f=2)



Yuting Tan

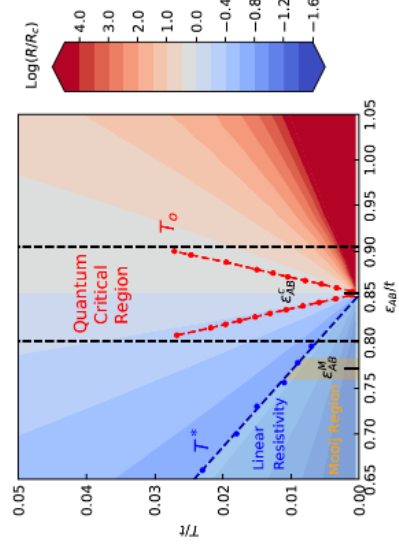
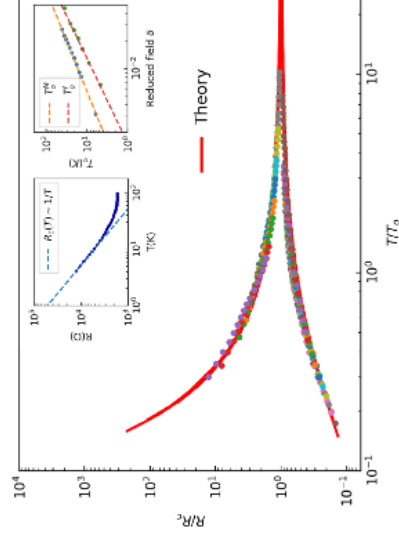
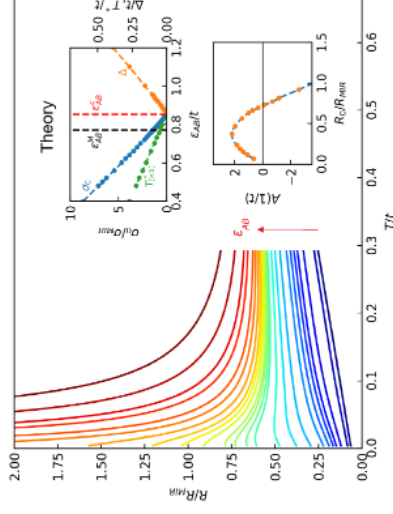
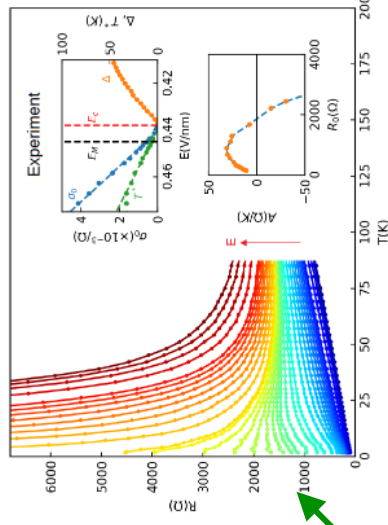
(arXiv:2112.11522)

Tuning band width via electric field at  $f = 2$



Slope A  
changes sign  
("Moijj correlation")

$$\sigma_0 = 1/R_0 \sim (E - E_c)$$



Continuous, disorder-dominated MIT!

All experimental trends captured by theory!

quantum criticality, scaling!!



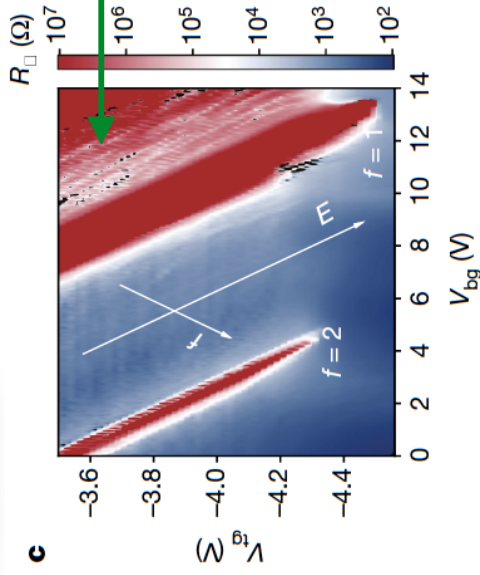
Louk Rademaker



Wigner

ECRYS: Mottness beyond half-filling!

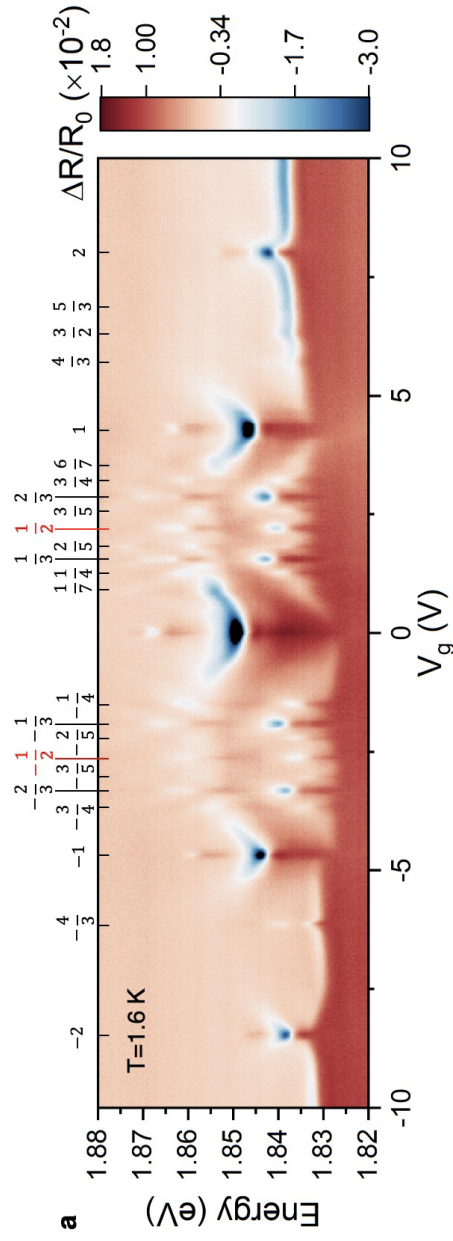
(soon on arXiv)



*Nature Physics* 4, 932 - 935 (2008)

Coulomb correlations and the Wigner–Mott transition

A. Camjayi, K. Haule, V. Dobrosavljevic & G. Kotliar



**Experiment:** Shan & Mak, *Nature*, 2020, **excitonic sensor!**

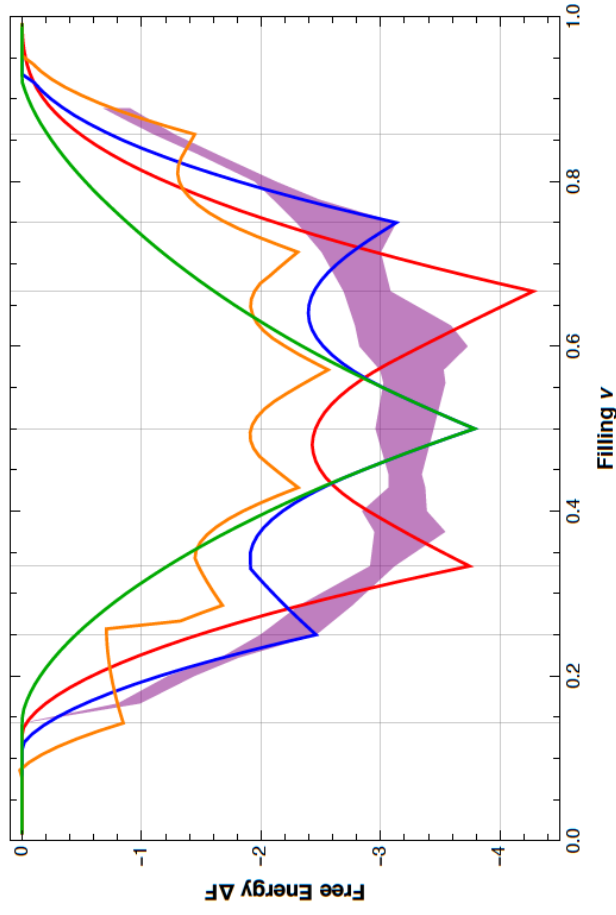
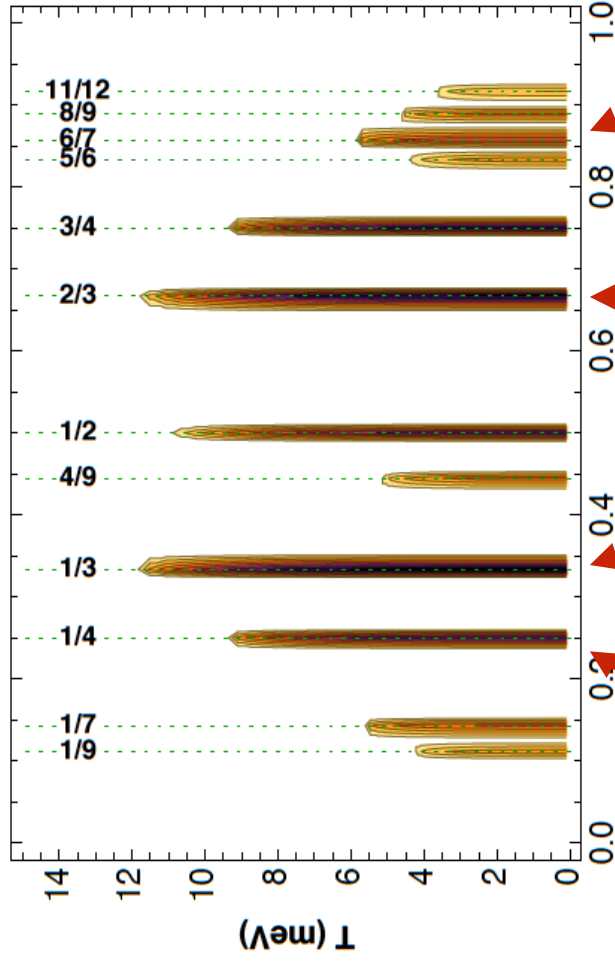
# ECRYS: Mottness beyond half-filling!



Wigner

Competing charge orders!

Louk Rademaker



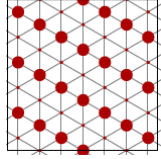
$$H = - \sum_{i,j,\sigma} t_{ij} c_{i,\sigma}^\dagger c_{j,\sigma} + \sum_i U n_{i,\uparrow} n_{i,\downarrow} + \sum_{i,j \neq i, \sigma_1, \sigma_2} V_{ij} n_{i,\sigma_1} n_{j,\sigma_2}$$

Charge-order: Hartree theory

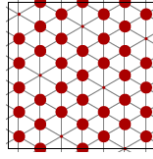
$$\sum_{i,j \neq i, \sigma_1, \sigma_2} V_{ij} n_{i,\sigma_1} n_{j,\sigma_2} \rightarrow \sum_{i,\sigma_1} n_{i,\sigma_1} \left( \sum_{j \neq i, \sigma_2} V_{ij} \langle n_j \rangle \right)$$

4-subl. Wigner

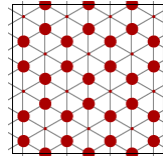
$$\text{Effective site energy } \varepsilon_i \equiv \sum_{j \neq i, \sigma_2} V_{ij} \langle n_j \rangle$$



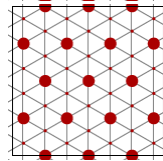
Stripes



7-subl. Wigner



3-subl. Wigner



4-subl. Wigner



Yuting Tan

ECRYS: Mottness beyond half-filling!

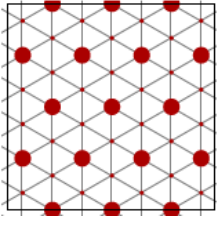
Effective site energy

$$\varepsilon_i \equiv \sum_{j \neq i, \sigma_2} V_{ij} \langle n_j \rangle$$

$$H_{\text{eff}} = - \sum_{ij, \sigma} t_{ij} c_{i, \sigma}^\dagger c_{j, \sigma} + \sum_{i, \sigma} n_{i, \sigma} \varepsilon_i + \sum_i U n_{i, \uparrow} n_{i, \downarrow}$$

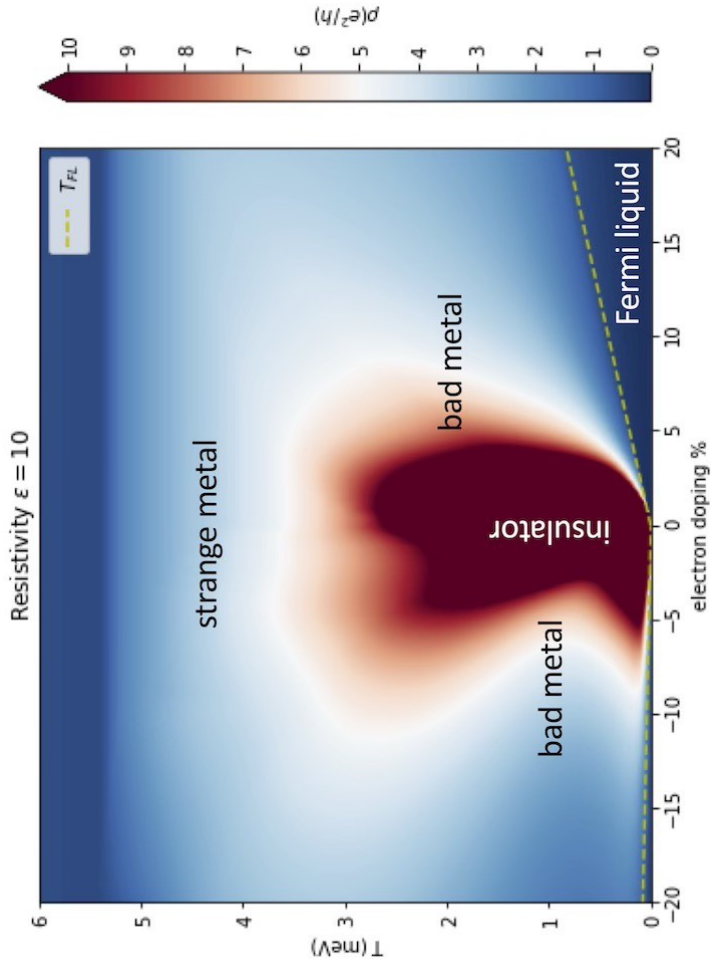
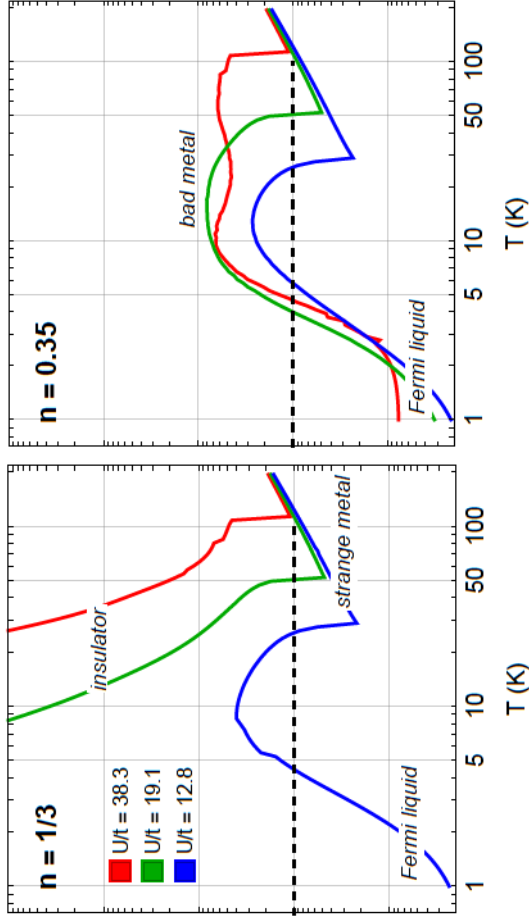


Wigner



3-subl. Wigner

Onsite Coulomb correlations, transport: DMFT



Quantum effects: particle-hole asymmetry

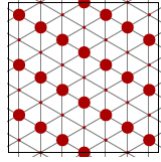


# ECRYS+: self-generated Wigner-Mott glasses!



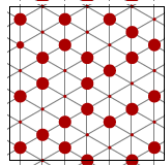
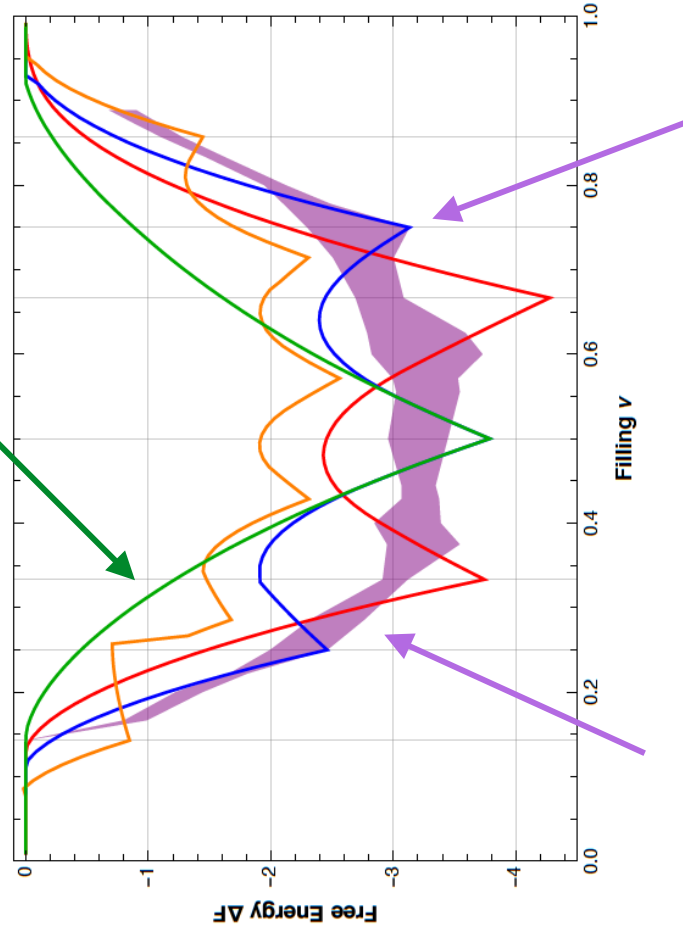
**Louk Rademaker**

Stripes

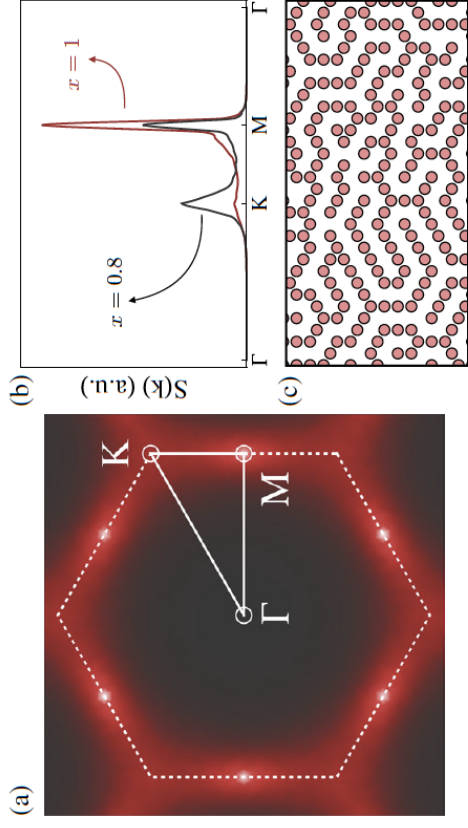
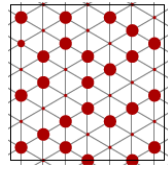


## Glassy Dynamics in Geometrically Frustrated Coulomb Liquids without Disorder

Samiyeh Mahmoudian,<sup>1</sup> Louk Rademaker,<sup>2</sup> Arnaud Ralko,<sup>3</sup> Simone Fratini,<sup>3</sup> and Vladimir Dobrosavljević<sup>1</sup>

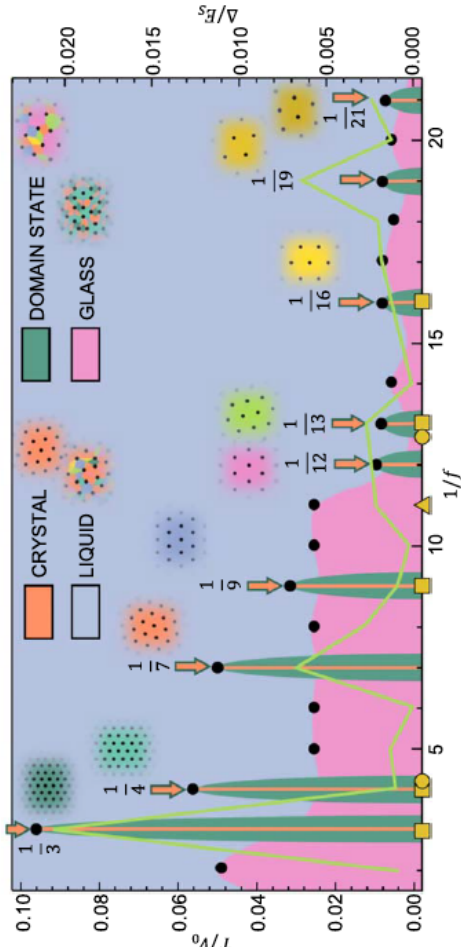
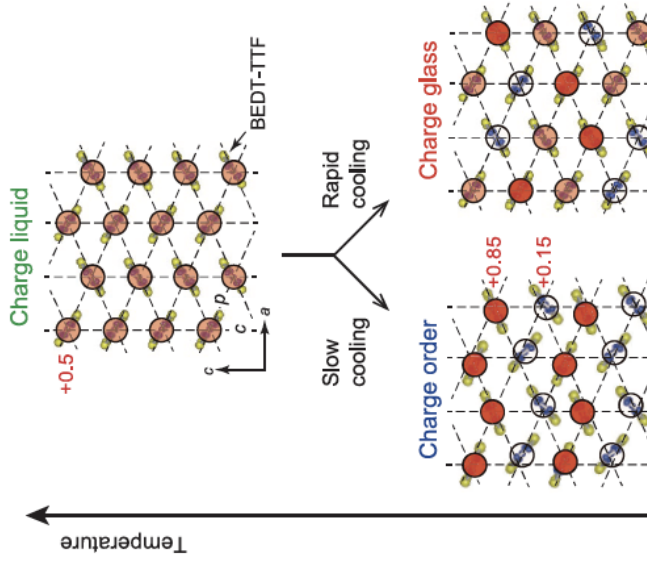


Amorphous states



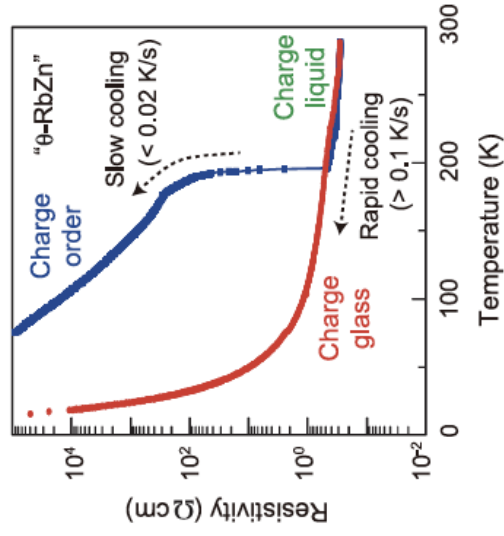
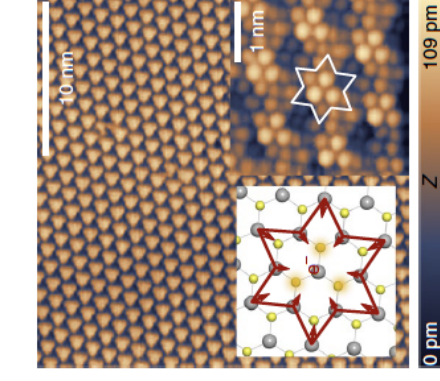
Competing charge orders - glassiness?

# How common are Wigner-Mott glasses?



System	$f$	Phase
2H-Fe <sub>0.95</sub> TaS <sub>2</sub> [105]	1/3	Crystal
1T-TiSe <sub>2</sub>	1/4	Crystal
N <sub>2</sub> H <sub>4</sub> /1T-TaS <sub>2</sub> [58]	1/4	Crystal
N <sub>2</sub> H <sub>4</sub> /2H-TaS <sub>2</sub> [58]	1/4	Crystal
1T-Cu <sub>0.08</sub> TiSe <sub>2</sub> [54]	1/4.2	Domain state
2H-Fe <sub>0.33</sub> TaSe <sub>2</sub> [105]	1/4	Crystal
2H-Fe <sub>0.33</sub> NbSe <sub>2</sub> [105]	1/4	Crystal
Alkali/1T-TaS <sub>2</sub> [56, 57]	~1/8	Glass
N <sub>2</sub> H <sub>4</sub> /1T-TaS <sub>2</sub> [58]	~1/8	Glass
2H-TaS <sub>2</sub> [106]	1/9	Crystal
2H-TaSe <sub>2</sub> [106]	1/9	Crystal
2H-NiSe <sub>2</sub> [59]	~1/9	Domain state
Cu/1T-TaS <sub>2</sub> [107]	1/9	Crystal
Alkali/1T-TaS <sub>2</sub> [108]	1/9	Crystal
N <sub>2</sub> H <sub>4</sub> /1T-TaS <sub>2</sub> [58]	1/9	Crystal
PD 1T-TaS <sub>2</sub>	1/11	Glass
1T-Nb <sub>0.1</sub> TaS <sub>2</sub> [51]	~1/11	Possible glass
PD 1T-TaS <sub>2</sub>	1/12.6	Domain state
1T-TaSeS	1/12.6	Domain state
1T-Ta <sub>0.99</sub> Fe <sub>0.01</sub> S <sub>2</sub>	1/12.6	Domain state
1T-Ta <sub>0.97</sub> Ta <sub>0.99</sub> Se <sub>2</sub> [52]	1/12.6	Domain state
1T-Nb <sub>0.04</sub> TaS <sub>2</sub> [51]	~1/13	Domain state
1T-Nb <sub>0.07</sub> TaS <sub>2</sub> [51]	~1/13	Domain state
1T-TaS <sub>2</sub>	1/13	Crystal
4Hb-TaS <sub>2</sub> [106]	1/13	Crystal
1T-TaSe <sub>2</sub>	1/13	Crystal
4Hb-TaSe <sub>2</sub> [106]	1/13	Crystal
1T-NbSe <sub>2</sub> [106]	1/13	Crystal
1T-VSe <sub>2</sub> [106]	1/16	Crystal

## 1T-TaS<sub>2</sub>



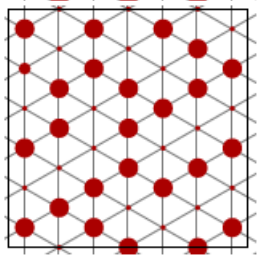
D. Mihailovic et al.

P. Monceau, K. Kanoda, ...

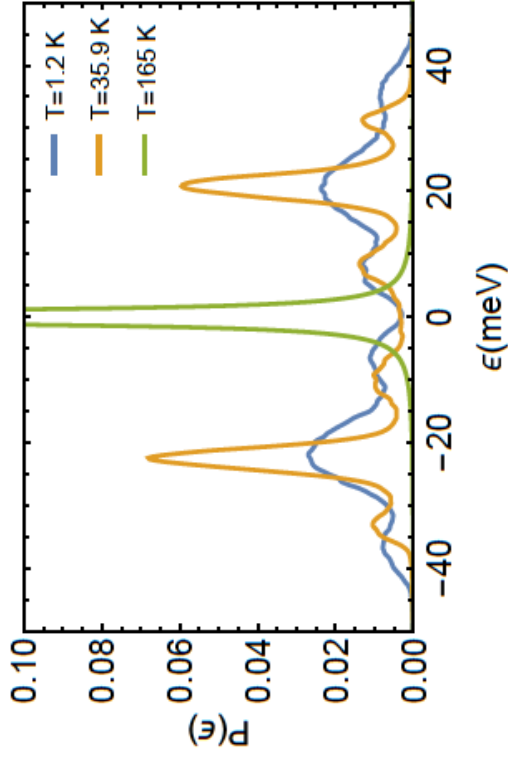


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Amorphous states

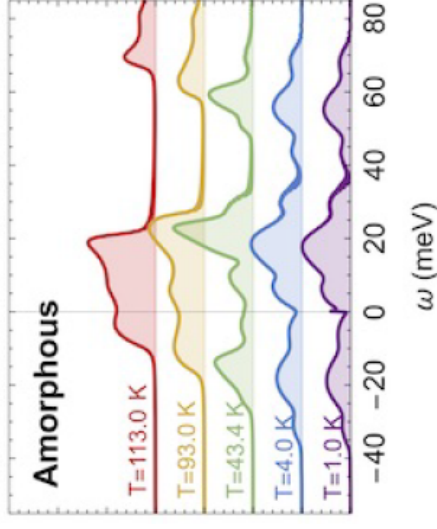
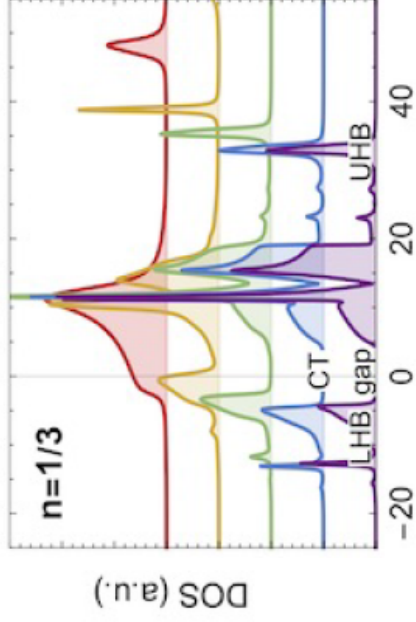


Effective site energy  $\epsilon_i \equiv \sum_{j \neq i, \sigma_j} V_{ij} \langle n_j \rangle$

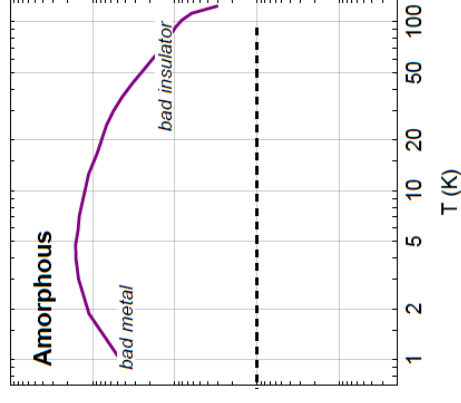
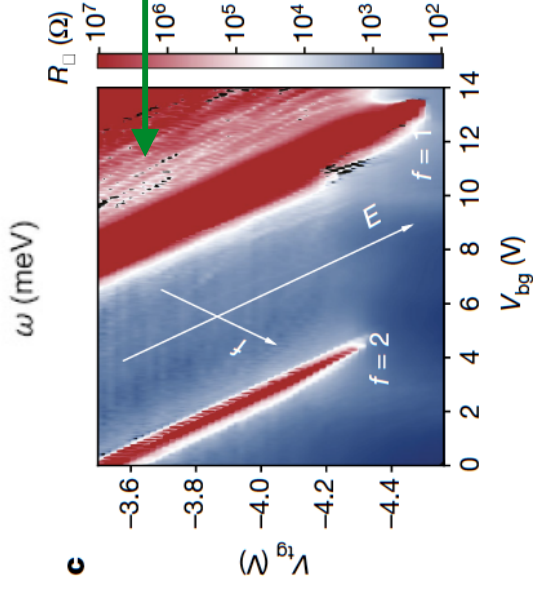


Histogram for amorphous state at  $T = 1.2K, 35.9K, 165K$ .

“Electron slush”: transport in Wigner-Mott glasses!



Wigner-Mott?  
( $0 < f < 1$ )

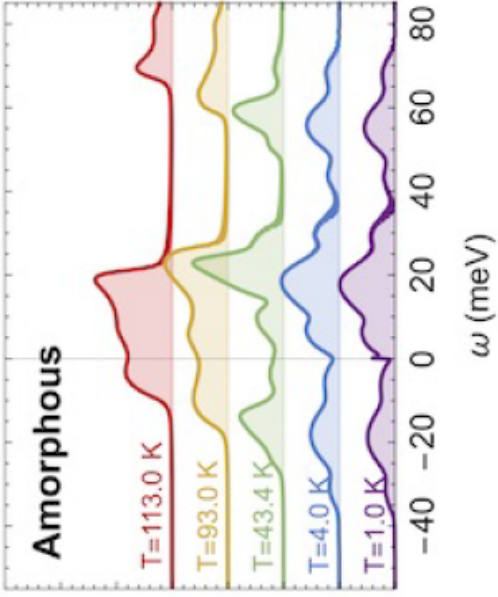
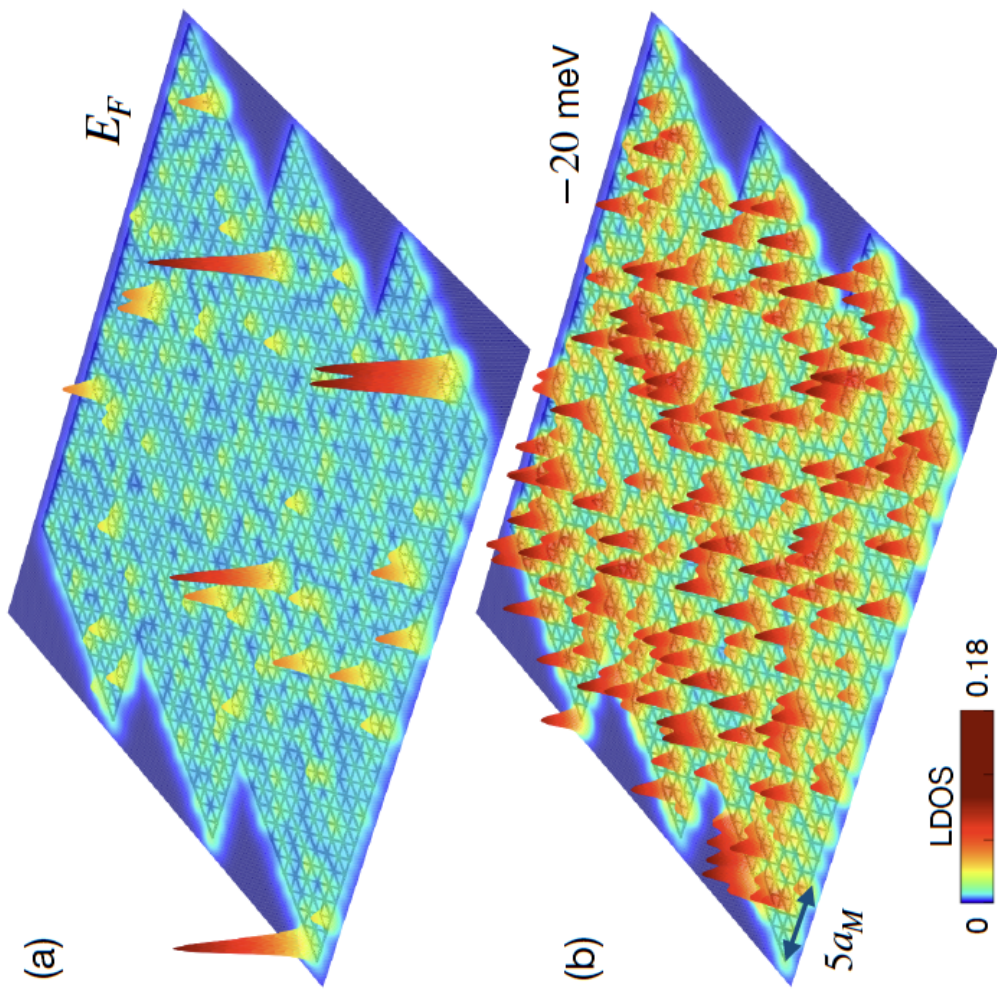


“Pseudogap transport”: weakly insulating?



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# “Electron slush”: STM signatures?

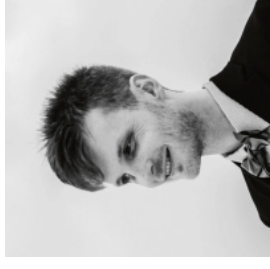


**Amorphous electronic states depleted near the Fermi energy**



Yuting Tan

## Perspectives and challenges



Louk Rademaker

- TMD Moire bilayers as **ideal realizations** of many MIT universality classes
- Mott, Wigner-Mott, and **disorder-driven** transitions + more...
- **DMFT describes surprisingly well** not only Mott but also **disorder-driven MIT**
- **Open questions:**
  - A. Can onset of charge order be separated from MIT (probably yes)?
  - B. Wigner-Mott crystal vs. **Wigner-Mott glass MITs?** Polarons, localization?
  - C. Glassy and other **non-equilibrium** effects (weak thermalization, MBL)?