

Signatures of a Pair Density Wave at High Magnetic Fields in Stripe-Ordered Cuprates

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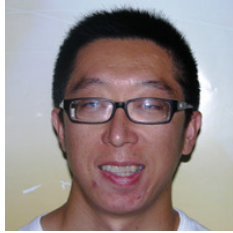
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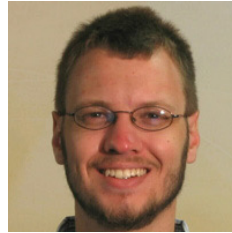
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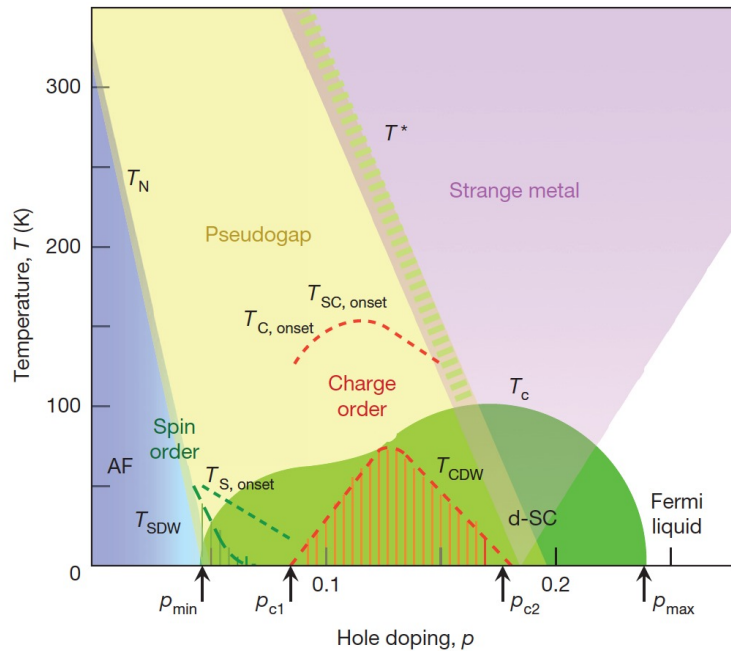


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LSCO, LESCO, LNSCO crystals



Copper-oxide high-temperature superconductors: Questions that we address

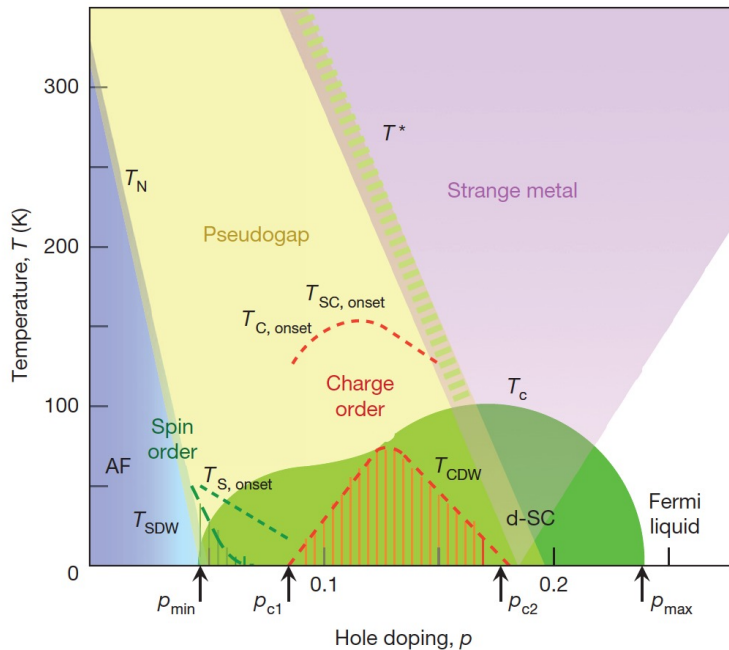


- Nature of the **ground state** (if superconductivity is removed)?
- Interplay of **charge and spin orders** with cuprate superconductivity?
- Origin of the **pseudogap** regime?
- Role of the **pair-density wave (PDW) superconductivity** in cuprate physics?

[Keimer *et al.*, Nature 518, 179 (2015)]



Copper-oxide high-temperature superconductors



[Keimer *et al.*, Nature 518, 179 (2015)]

- Pseudogap, charge and spin orders, superconductivity...
⇒ **Pair density wave (PDW):** superconducting (SC) order parameter is oscillatory in space; spatial average = zero

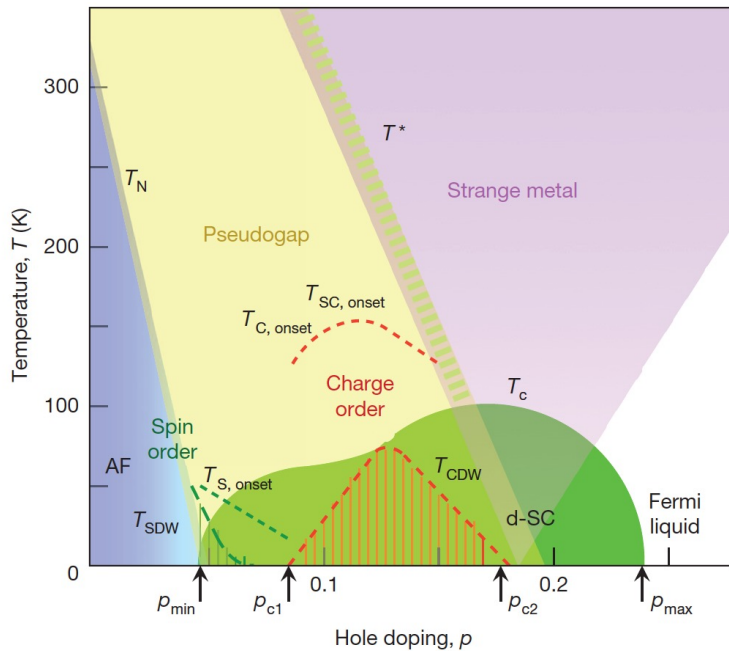
Review on PDW in cuprates and beyond:

D. Agterberg *et al.*, *Annu. Rev. Condens. Matter Phys.* **11**, 231 (2020)

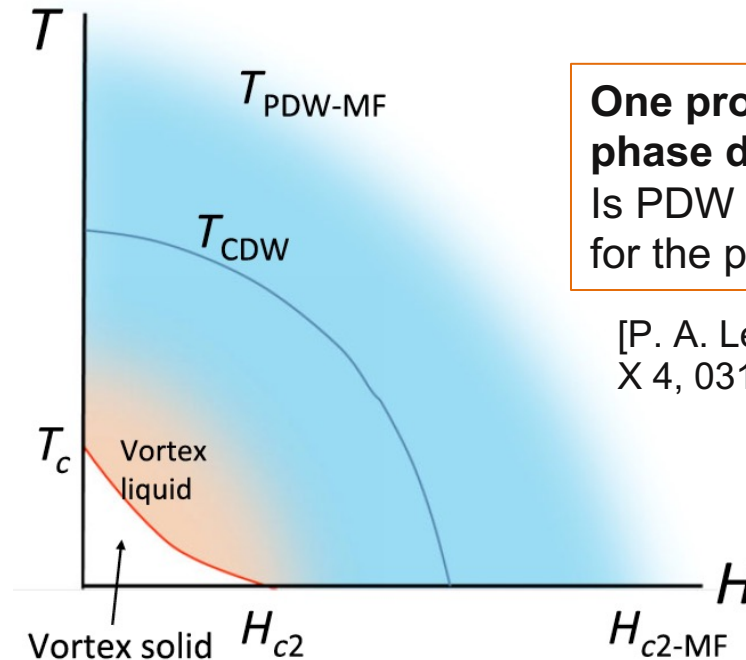
- **Evidence** for PDW has been largely **indirect**
- **Broader relevance** of a PDW state to cuprate physics is an open question



Role of PDW in the physics of copper-oxide high-temperature superconductors?



[Keimer *et al.*, Nature 518, 179 (2015)]



One proposed phase diagram:
Is PDW responsible for the pseudogap?

[P. A. Lee, Phys. Rev. X 4, 031017 (2014)]

- **Needed:** transport signatures of the PDW in the regime where superconductivity is destroyed by quantum phase fluctuations ($T \rightarrow 0$, high H)
- Study **La-214 family**: charge orders with strongest correlations, in the form of charge and spin **stripes**



Outline

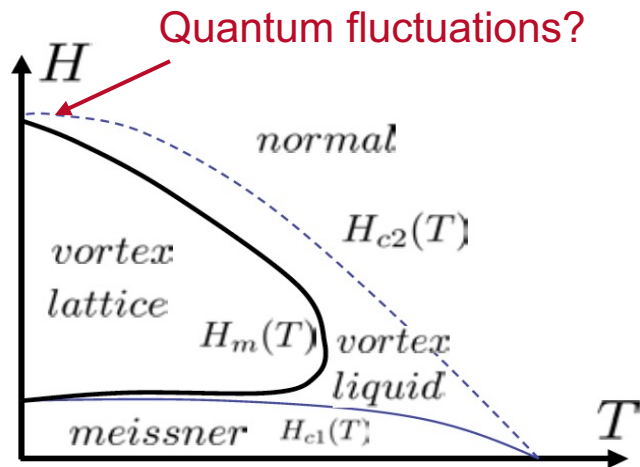
- At what field does the superconductivity vanish?
What is the value of the upper critical field H_{c2} ?
Vortex phase diagram
- Behavior for $H < H_{c2}$ in stripe-ordered cuprates:
Evidence of PDW in the regime of SC phase fluctuations
from $T > T_c^0$ in $H=0$ to $H=H_{c2}$ as $T \rightarrow 0$



Vortex phase diagram

- At what field does the superconductivity vanish?
What is the value of the upper critical field H_{c2} ?

Vortex phase diagram



- **Thermal fluctuations:** Melting of the vortex lattice into a **vortex liquid**
- Vortex lattice suppressed to below the **crossover line $H_{c2}(T)$**
- **Does the vortex liquid survive as $T \rightarrow 0$?**

[Blatter *et al.*, Rev. Mod. Phys. 66, 1125 (1994)]



T - H phase diagram in underdoped cuprates

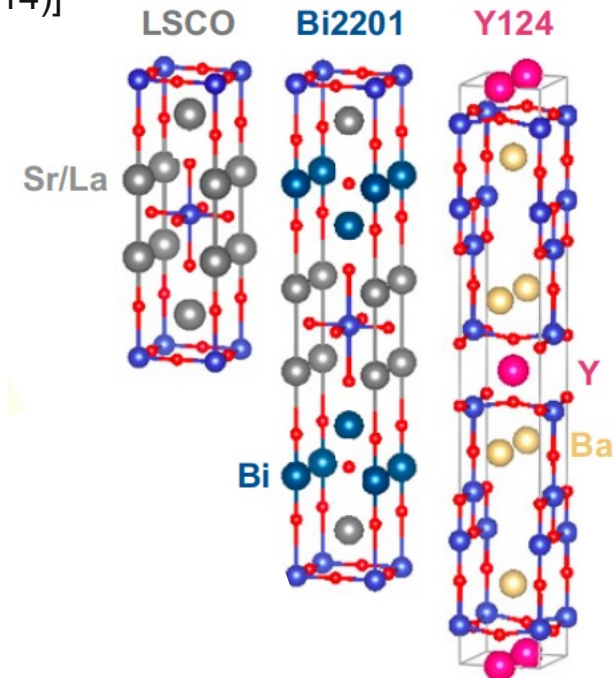
- At what field does the superconductivity vanish? What is the value of H_{c2} ?

Vortex phase diagram

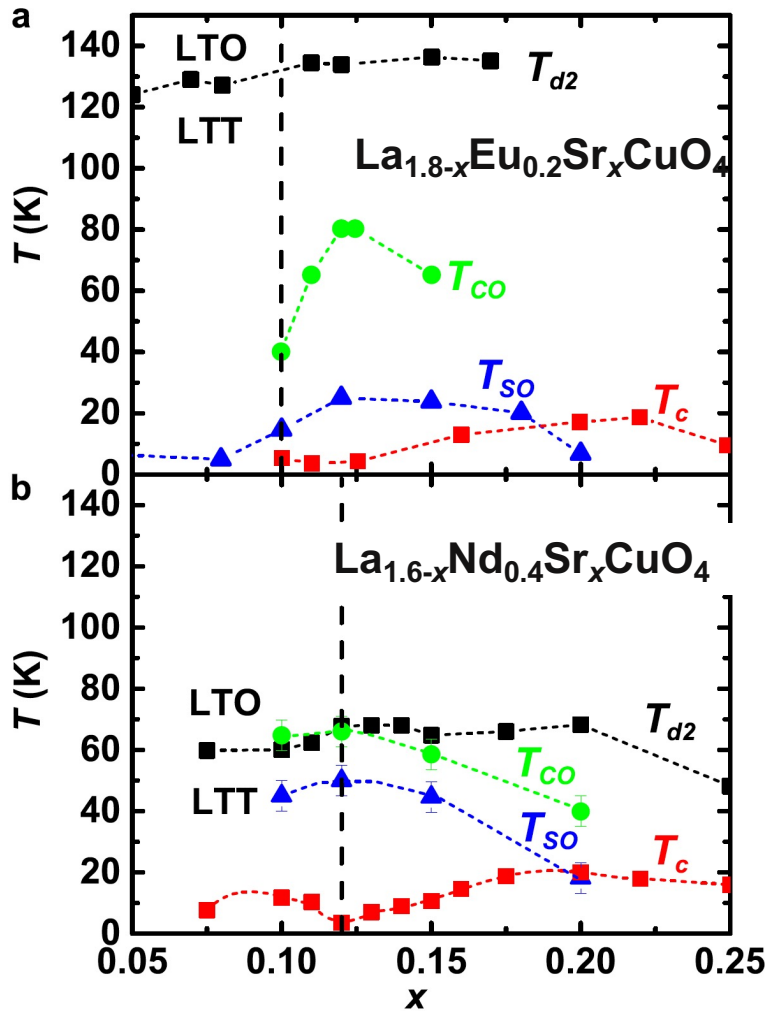
Linear and nonlinear transport:

Qualitatively the same regardless of the presence of charge or spin orders

- **LSCO** (spin order; LTO) [X. Shi *et al.*, Nature Phys. 10, 437 (2014)]
- spin- and charge-stripped **Nd-LSCO** (LTT),
Eu-LSCO (LTT) [Z. Shi *et al.*, Sci. Adv. 6, eaay8946 (2020)]
and **La_{2-x}Ba_xCuO₄** (LBCO) [Y. Li *et al.*, Sci. Adv. 5, eaav7686 (2019)]
- spin- and charge-stripped **Fe-LSCO** (LTO)
[B. K. Pokharel *et al.*, unpublished]
- **Bi-2201** (charge order; tetragonal)
[J. Terzic *et al.*, unpublished]
- **YBCO** (no spin order, static charge order at high H)
[Y.-T. Hsu *et al.*, PNAS 118, e2021216118 (2021);
Y.-T. Hsu *et al.*, PNAS 118, e2016275118 (2021)]



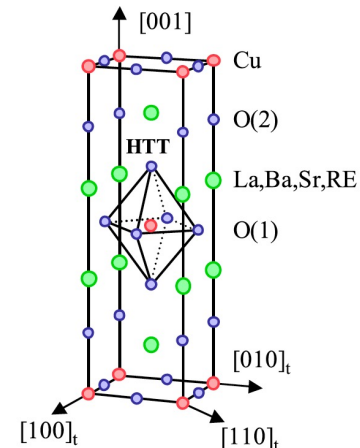
Stripe-ordered Eu-LSCO and Nd-LSCO



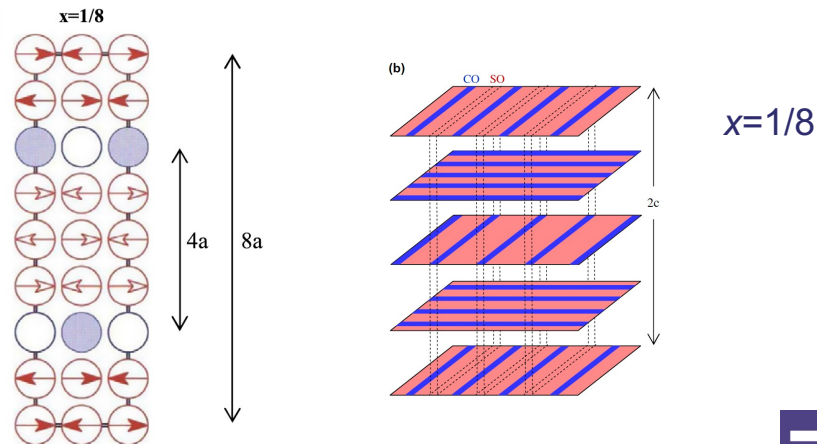
(Data pts from the literature)

- Similar to LBCO

[M. Hücker, Physica C 481, 3 (2012)]



- **Short-range charge and spin stripes** present in $H=0$; both **enhanced** when T_c is suppressed by H

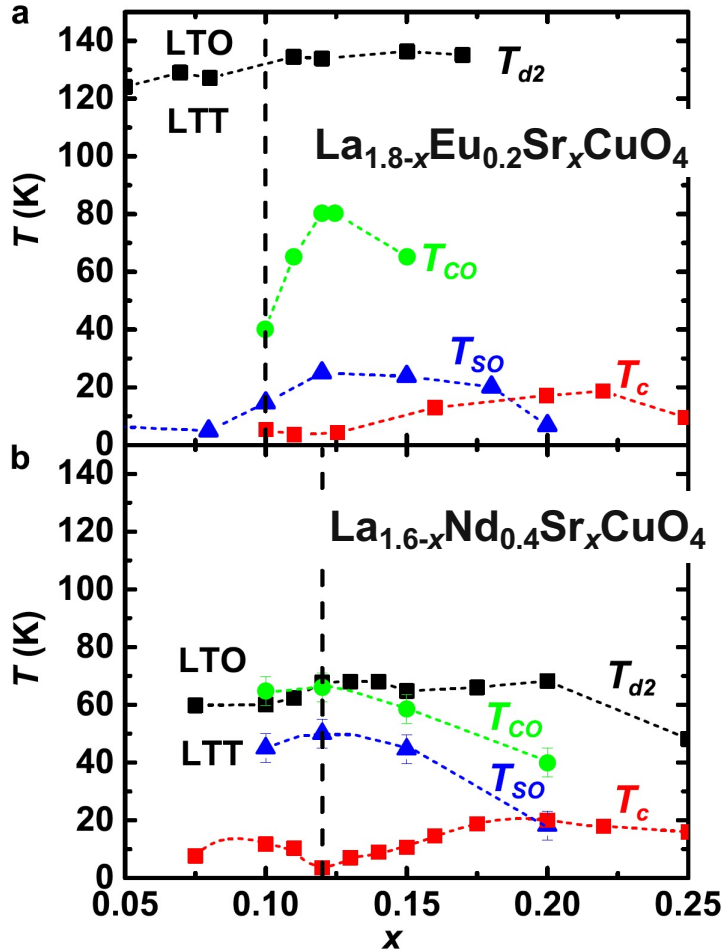


[Tranquada *et al.*, Nature 375, 561 (1995)]

[M. Hücker, Physica C 481, 3 (2012)]



Stripe-ordered Eu-LSCO and Nd-LSCO



(Data pts from the literature)

- $\text{La}_{1.8-x}\text{Eu}_{0.2}\text{Sr}_x\text{CuO}_4$ and $\text{La}_{1.6-x}\text{Nd}_{0.4}\text{Sr}_x\text{CuO}_4$

$\text{La}_{1.8-x}\text{Eu}_{0.2}\text{Sr}_x\text{CuO}_4$ (LESCO): $x=0.10$

$T_c^0 = (5.7 \pm 0.3) \text{ K}$ (where in-plane resistivity ρ_{ab} goes to zero)

$T_{so} \sim 15 \text{ K}$, $T_{co} \sim 40 \text{ K}$, $T_{\text{pseudogap}} \sim 175 \text{ K}$

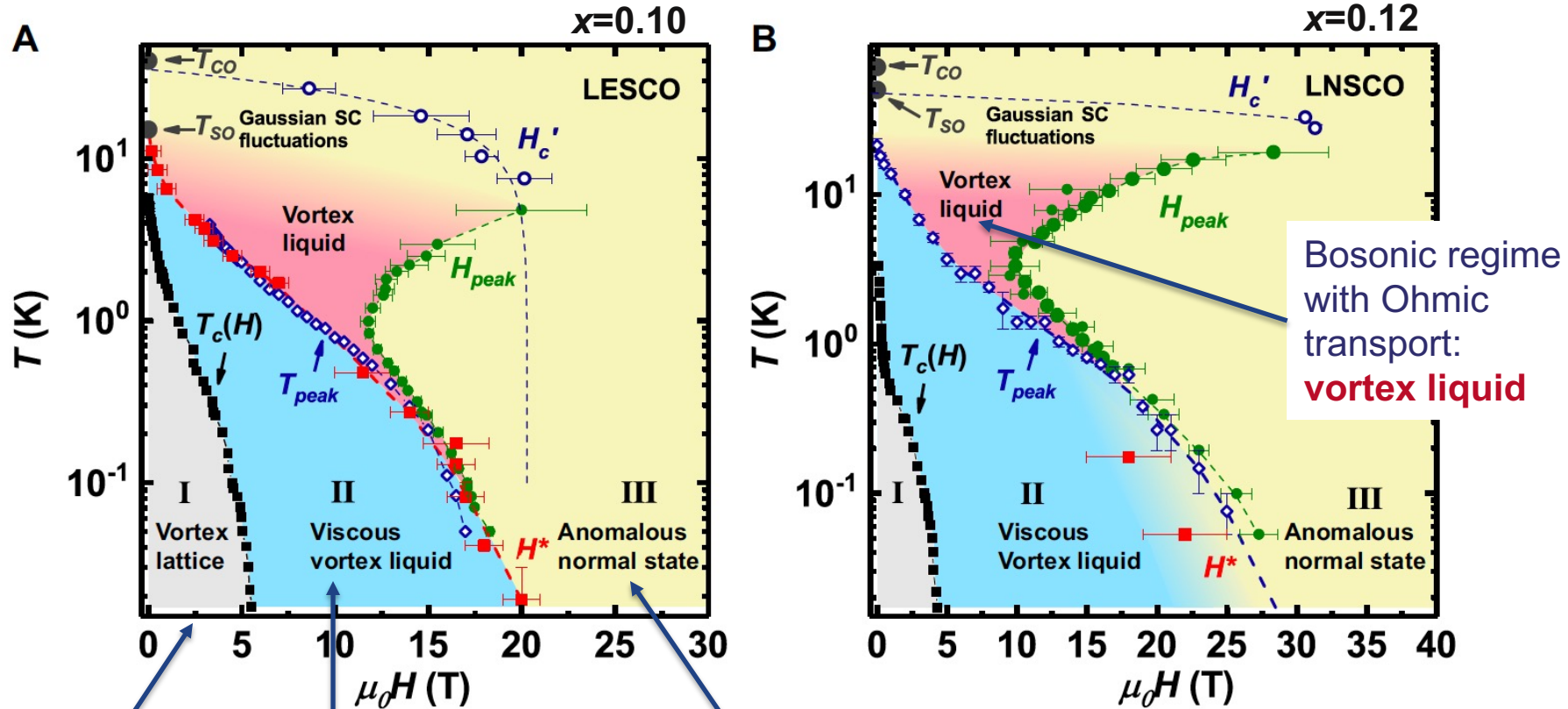
$\text{La}_{1.6-x}\text{Nd}_{0.4}\text{Sr}_x\text{CuO}_4$ (LNSCO): $x=0.12$

$T_c^0 = (3.6 \pm 0.4) \text{ K}$ (where in-plane resistivity ρ_{ab} goes to zero)

$T_{so} \sim 50 \text{ K}$, $T_{co} \sim 70 \text{ K}$, $T_{\text{pseudogap}} \sim 150 \text{ K}$



Vortex phase diagram of stripe-ordered Eu-LSCO and Nd-LSCO



$T_c(H) > 0$
 $\rho_{ab}(T < T_c) = 0$
 $I_c \neq 0$

$T_g = T_c = 0$
 $\rho_{ab}(T > 0) \neq 0$
 $I_c = 0$, non-Ohmic
 (for $I_{dc} \neq 0$)

No SC
 $\rho_{ab}(T > 0) \neq 0$
 Ohmic

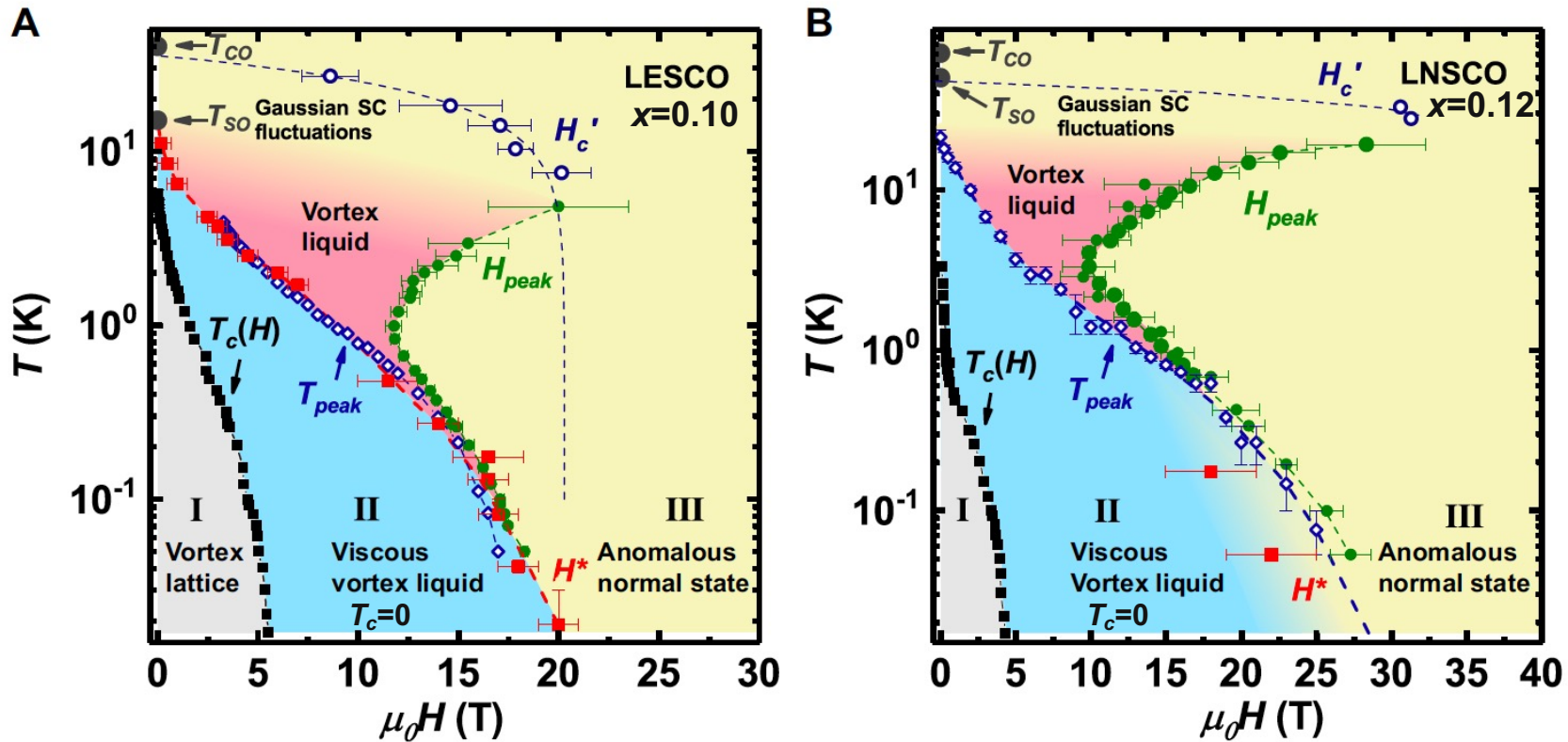
$H_c'(T \rightarrow 0) \approx H^*(T \rightarrow 0)$
 Upper critical field

(False color)



Vortex phase diagram of stripe-ordered Eu-LSCO and Nd-LSCO

Z. Shi *et al.*, *Sci. Adv.* 6, eaay8946 (2020)

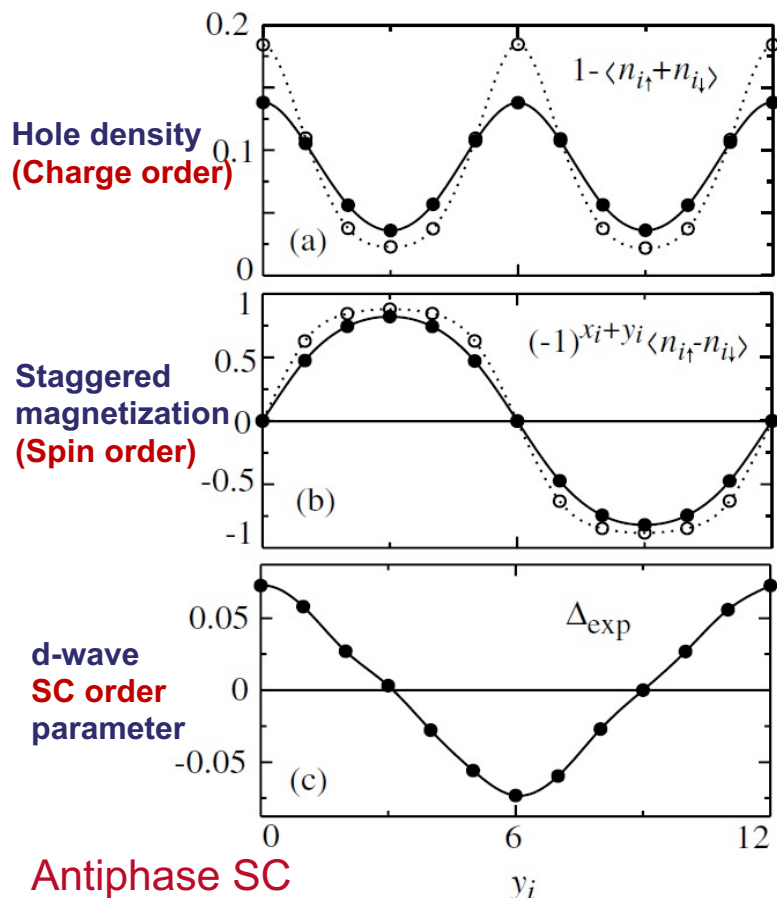
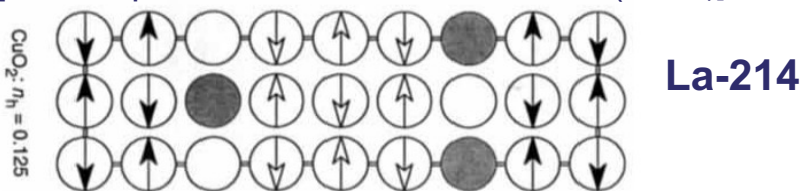


- Superconductivity is destroyed by **quantum phase fluctuations** ($T \rightarrow 0$, high H)
- $H=0$: Onset of phase fluctuations at $T \sim$ a few T_c^0



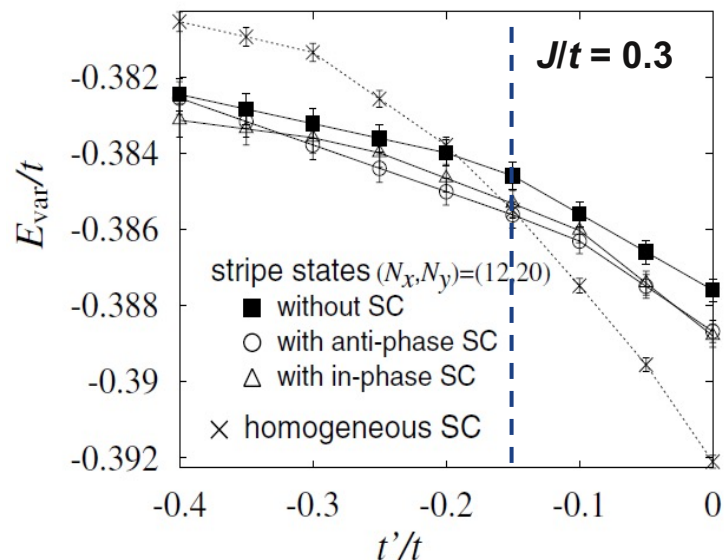
Pair density wave in the presence of stripe order

[J. Tranquada *et al.*, Nature 375, 561 (1995)]



[A. Himeda *et al.*, PRL 88, 117001 (2002)]

Monte Carlo simulation using 2D t-t'-J model



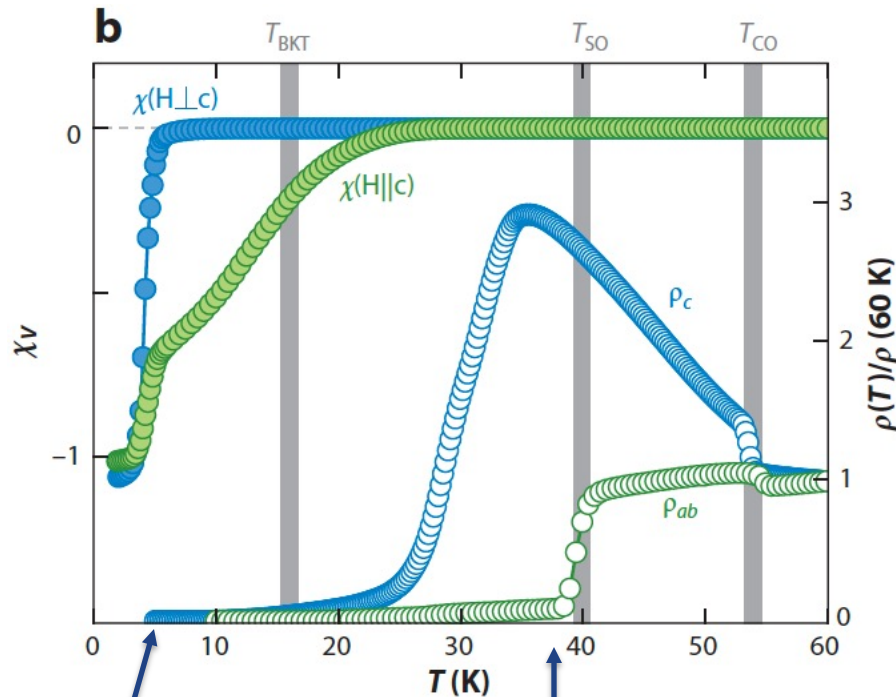
In-phase and antiphase (PDW) SC very close in energy

Effective Josephson coupling between neighboring charge stripes in each plane is mediated by spin stripes



Layer decoupling: Pair density wave scenario

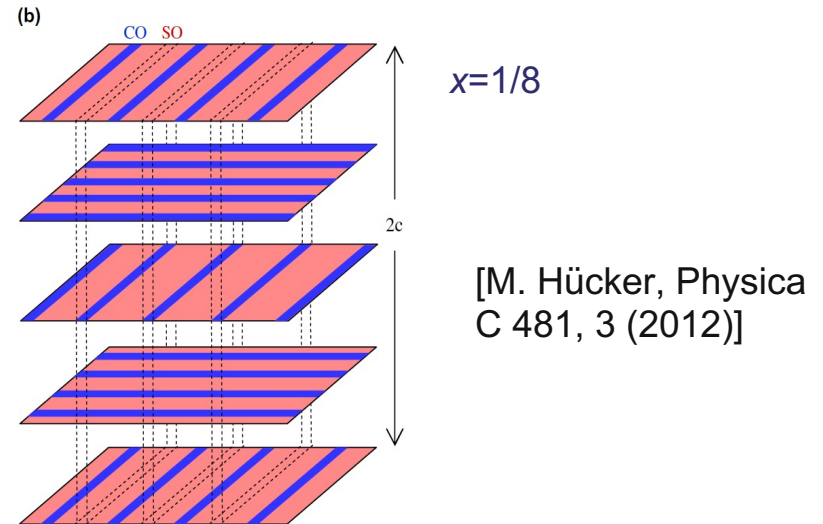
$\text{La}_{2-x}\text{Ba}_x\text{CuO}_4$ ($x=0.125$)



[Q. Li *et al.*, PRL 99, 067001 (2007); J. M. Tranquada *et al.*, PRB 78, 174529 (2008)]

3D, uniform
SC order

Onset of 2D (PDW)
SC correlations



[M. Hücker, Physica C 481, 3 (2012)]

Orthogonally-stacked **antiphase SC**
leads to frustration of interlayer
Josephson coupling and **layer
decoupling**

[E. Berg *et al.*, PRL 99, 127003 (2007)]

Effect reduced for doping away from
 $x=1/8$ and with increasing disorder



Experimental evidence consistent with the PDW in cuprates

Dynamical layer **decoupling in $H=0$ for $x=1/8$:**

- **transport in LBCO:**
Q. Li *et al.*, PRL 99, 067001 (2007)
- **optical measurements in $\text{La}_{1.85-y}\text{Nd}_y\text{Sr}_{0.15}\text{CuO}_4$:**
S. Tajima *et al.*, PRL 86, 500 (2001)

- **$\text{Bi}_2\text{Sr}_2\text{CaCu}_2\text{O}_8$: STM, $H=0$**
[Hamidian *et al.*, Nature 532, 343 (2016);
Du *et al.*, Nature 580, 65 (2020)]

Dynamical layer **decoupling by H** (stabilizes spin stripes) **for x away from $1/8$:**

- **transport in underdoped LBCO:**
Z. Stegen *et al.*, PRB 87, 064509 (2013)
- **optical measurements in underdoped LSCO:**
A. A. Schafgans *et al.*, PRL 104, 157002 (2010)

Testing theoretical predictions - consequences of a PDW SC state:

[E. Fradkin *et al.*, Rev. Mod. Phys. 87, 457 (2015)]

- **Charge order modulation (CDW 1Q order) in vortex halos in $\text{Bi}_2\text{Sr}_2\text{CaCu}_2\text{O}_8$; STM, $H/T_c^0 \lesssim 0.1 \text{ T/K}$ (vortex solid regime)**

[S. D. Edkins *et al.*, Science 364, 976 (2019)]



Probing interlayer frustration

La-214: reorienting spins in spin stripes in every other plane by an in-plane magnetic field

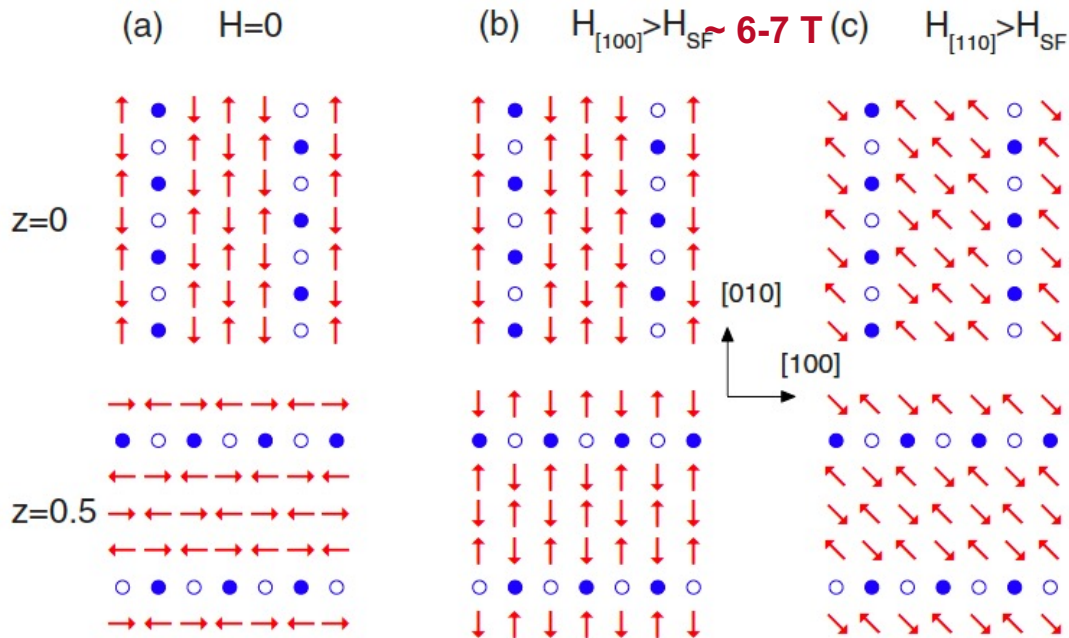


FIG. 5. (Color online) Model for spin structure of site-centered stripes as a function of field. (●,○) Half-filled charge stripes. Stripes in adjacent planes at $z=0$ and 0.5 are perpendicular. (a) Spin structure for $H=0$, (b) $\mathbf{H} \parallel [100]$, and (c) $\mathbf{H} \parallel [110]$.

[M. Hücker *et al.*, Phys. Rev. B 78, 214507 (2008);
M. Hücker *et al.*, Phys. Rev. B 70, 214515 (2004)]

A consequence of the PDW SC state:

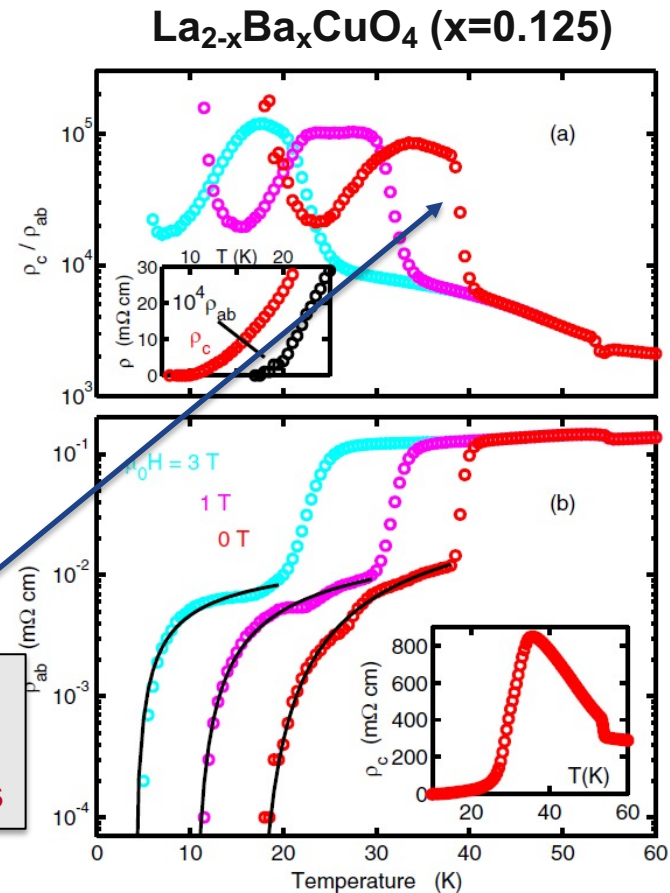
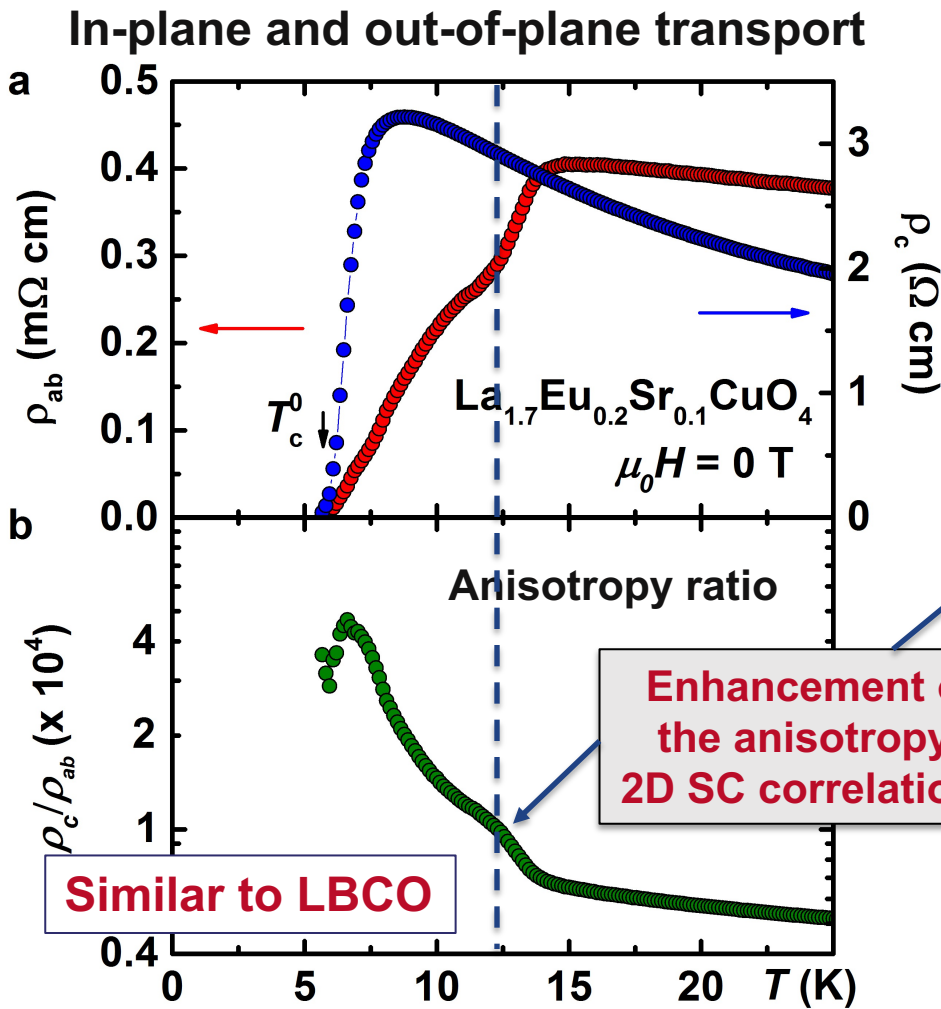
\Rightarrow In-plane H relieves the interlayer frustration, i.e. reduces the anisotropy

[E. Berg *et al.*, PRL 99, 127003 (2007);
E. Fradkin *et al.*, Rev. Mod. Phys. 87, 457 (2015)]

This is what we observed in Eu-LSCO and Nd-LSCO



Eu-LSCO: Anisotropy ratio ρ_c/ρ_{ab} in $H=0$

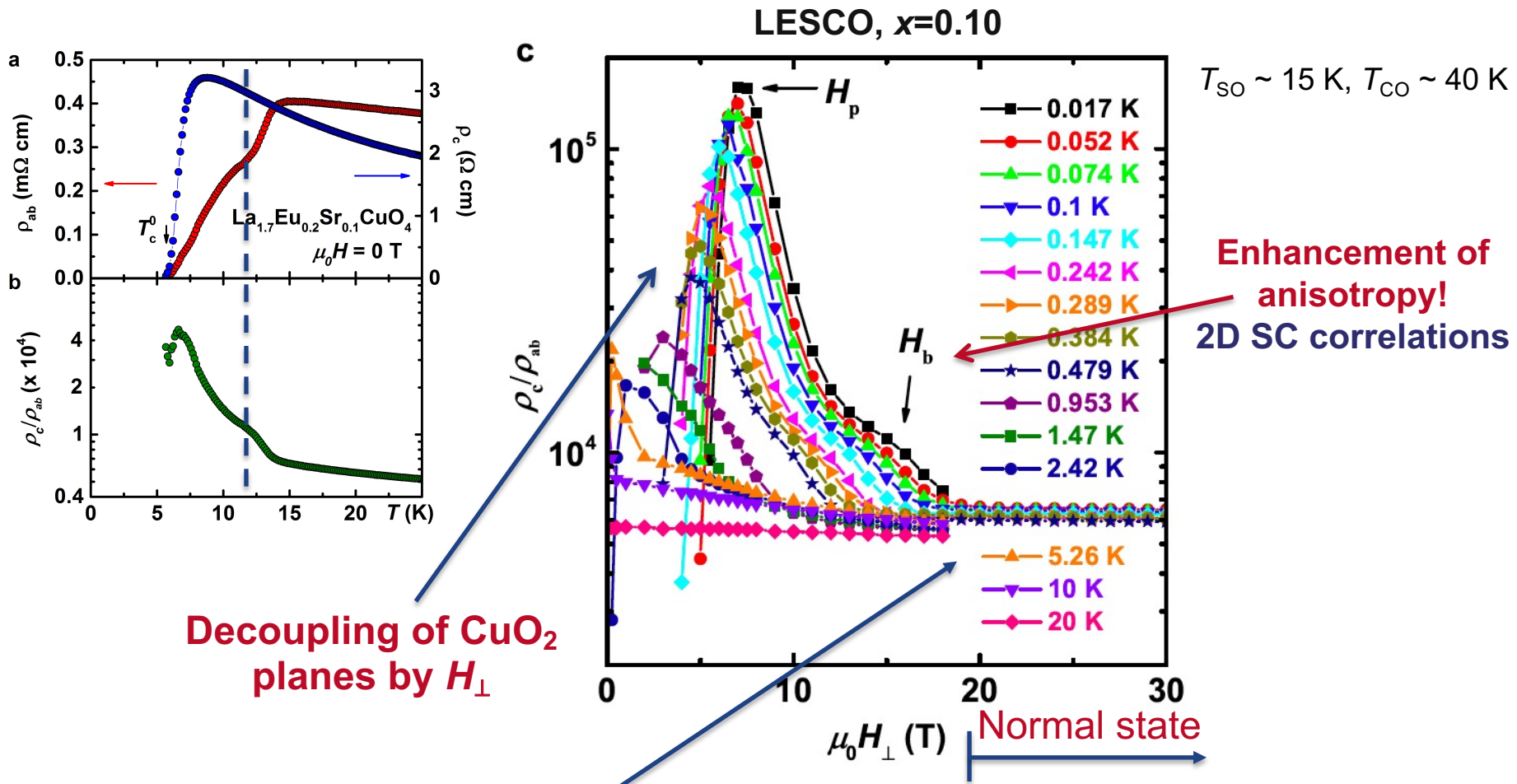


[Q. Li *et al.*, PRL 99, 067001 (2007)]

Same T_c^0 for ρ_{ab} and ρ_c : onset of 3D SC



Evolution of the anisotropy with temperature and perpendicular field

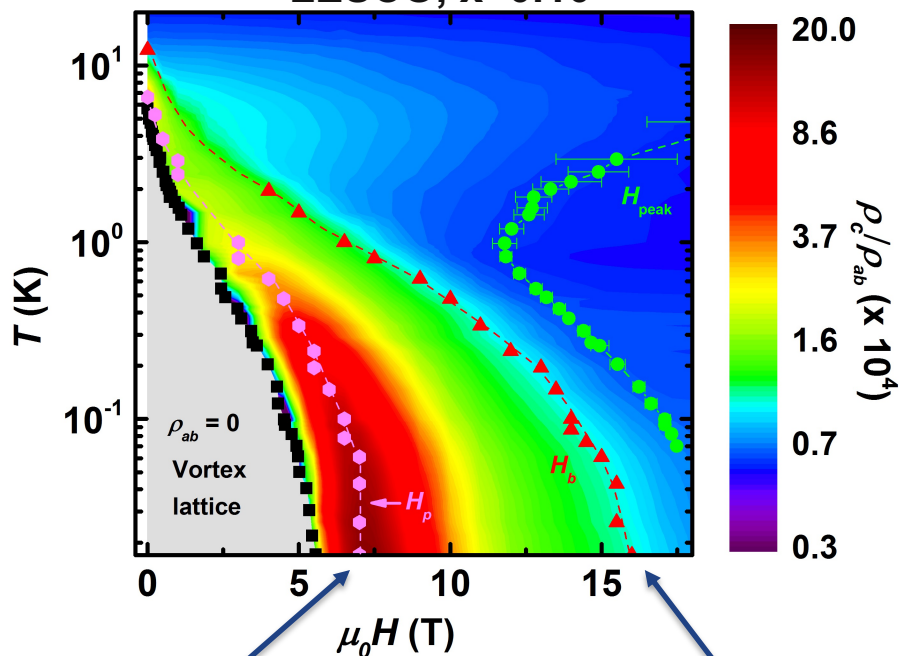


- Field-independent anisotropy ratio ρ_c/ρ_{ab} for $H_{peak} \approx H_{c2} < H$

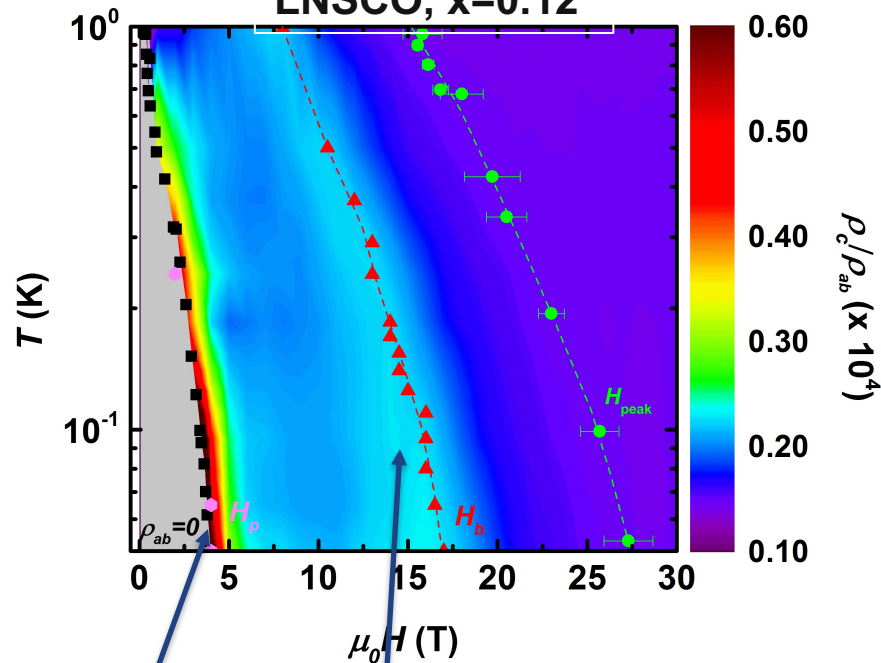


Evolution of the anisotropy with temperature and perpendicular field

LESCO, $x=0.10$



LNSCO, $x=0.12$



$H_p(T)$: layer decoupling field

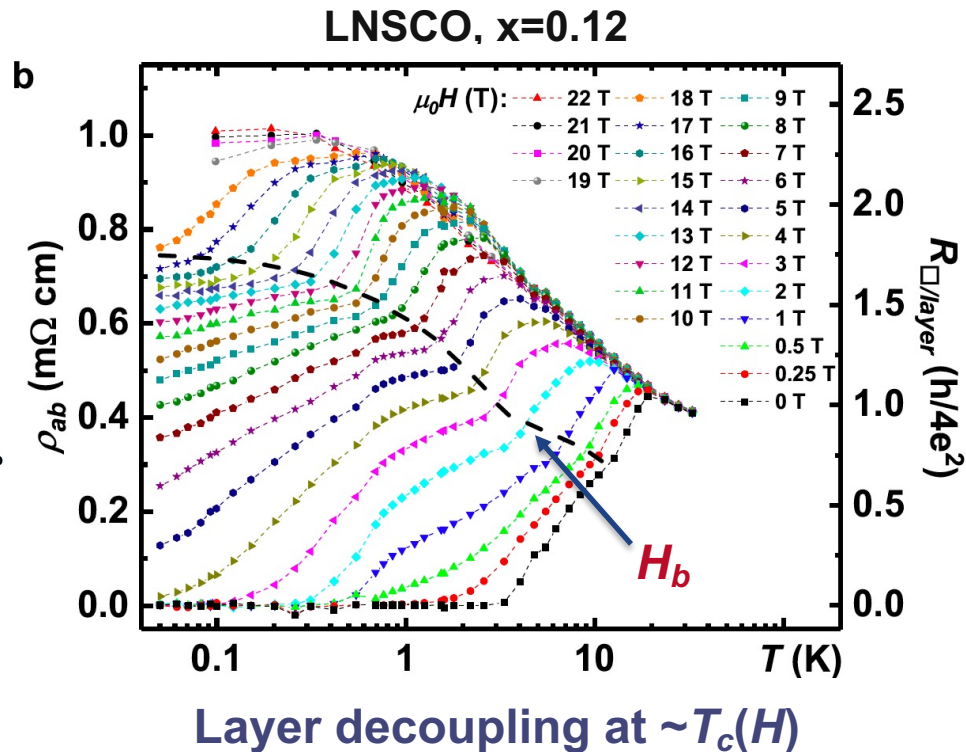
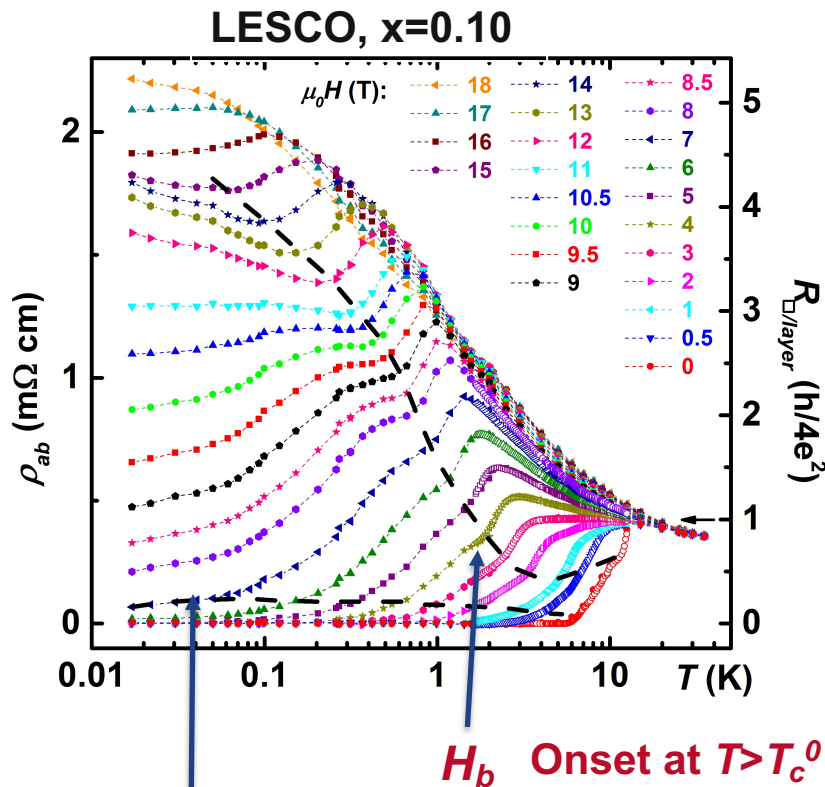
$H_p(T) \approx H_c(T)$ [i.e. $T_c(H)$, as expected]

$H_{\text{peak}} \sim H_{c2}$

H_b : 2D SC correlations



Two-step temperature dependence of the in-plane resistivity ρ_{ab}



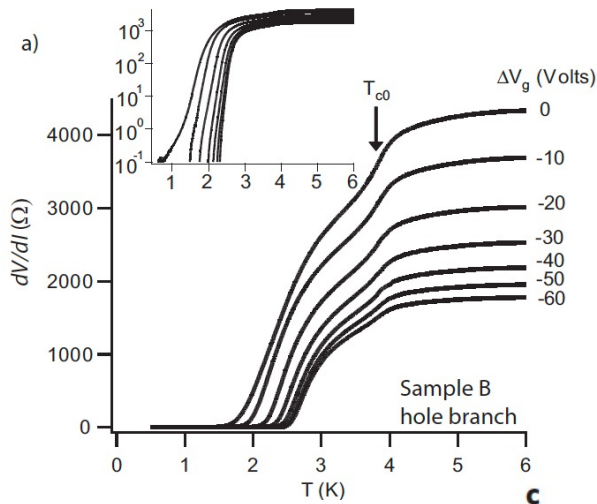
2D Physics



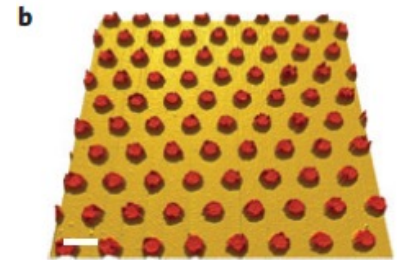
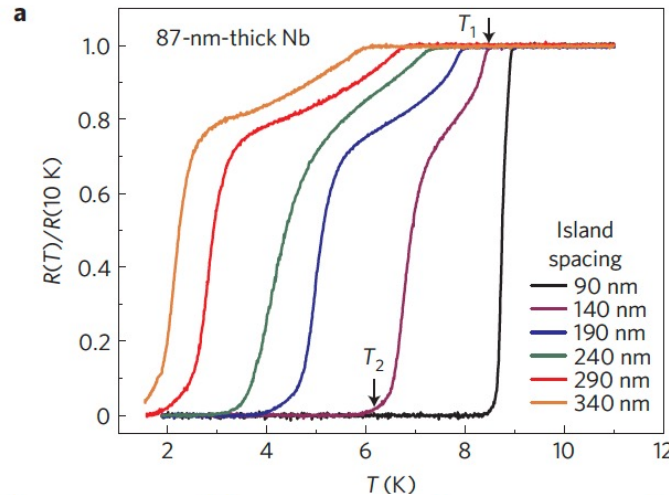
Two-step temperature dependence of the resistivity: Other 2D superconducting systems

Josephson junction (JJ) arrays

Sn islands on graphene sheet

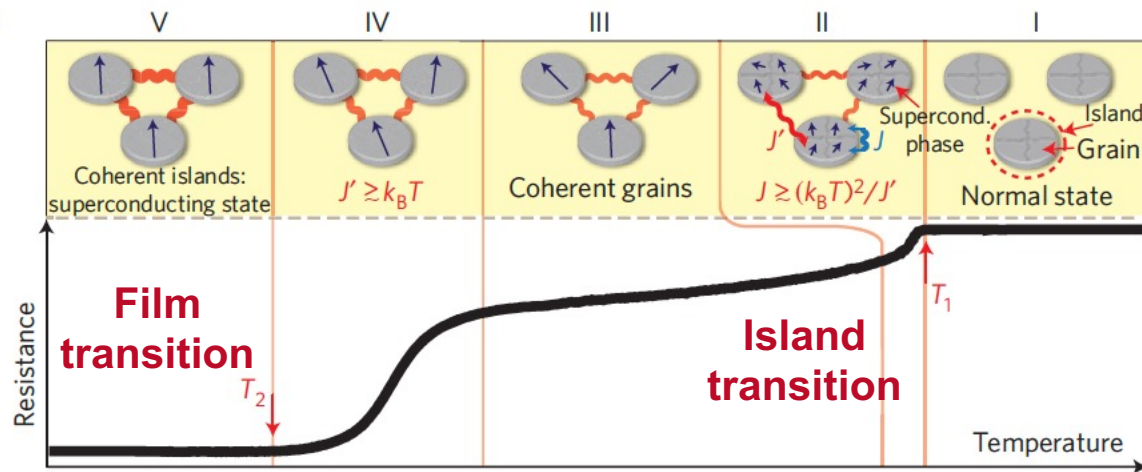


Nb islands on Au



[B. M. Kessler *et al.*, PRL 104, 047001 (2010)]

- **Granular films** of conventional superconductors
- ...



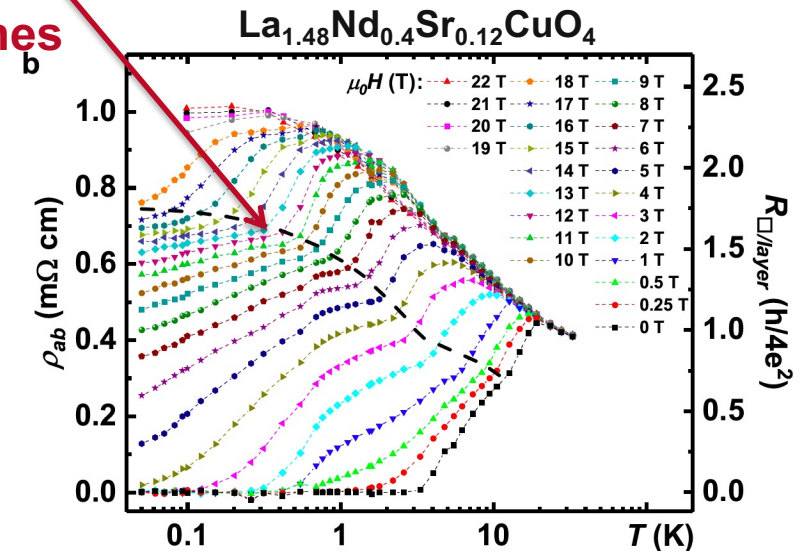
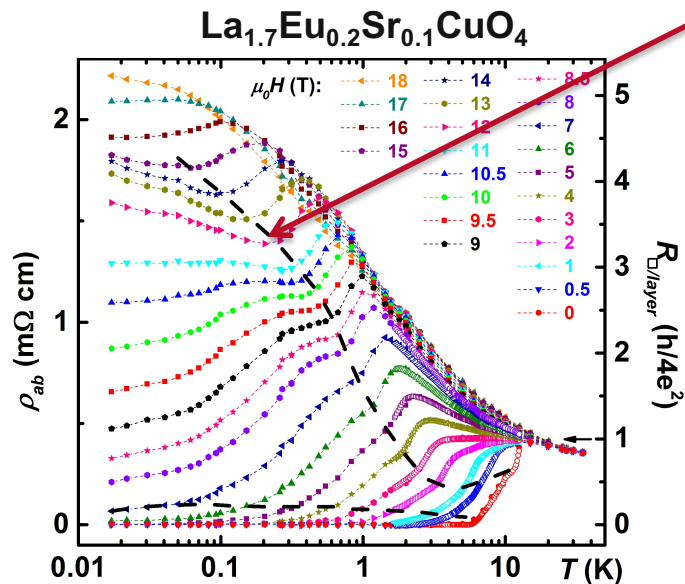
[S. Eley *et al.*, Nature Phys. 8, 59 (2012)]



Two-step temperature dependence of the in-plane resistivity ρ_{ab} : Striped cuprates

- Onset of SC correlations at $T > T_c^0$

Superconducting
“islands”
in the planes



At low T , increasing H_{\perp} destroys superconductivity in planes by quantum phase fluctuations of Josephson-coupled SC islands

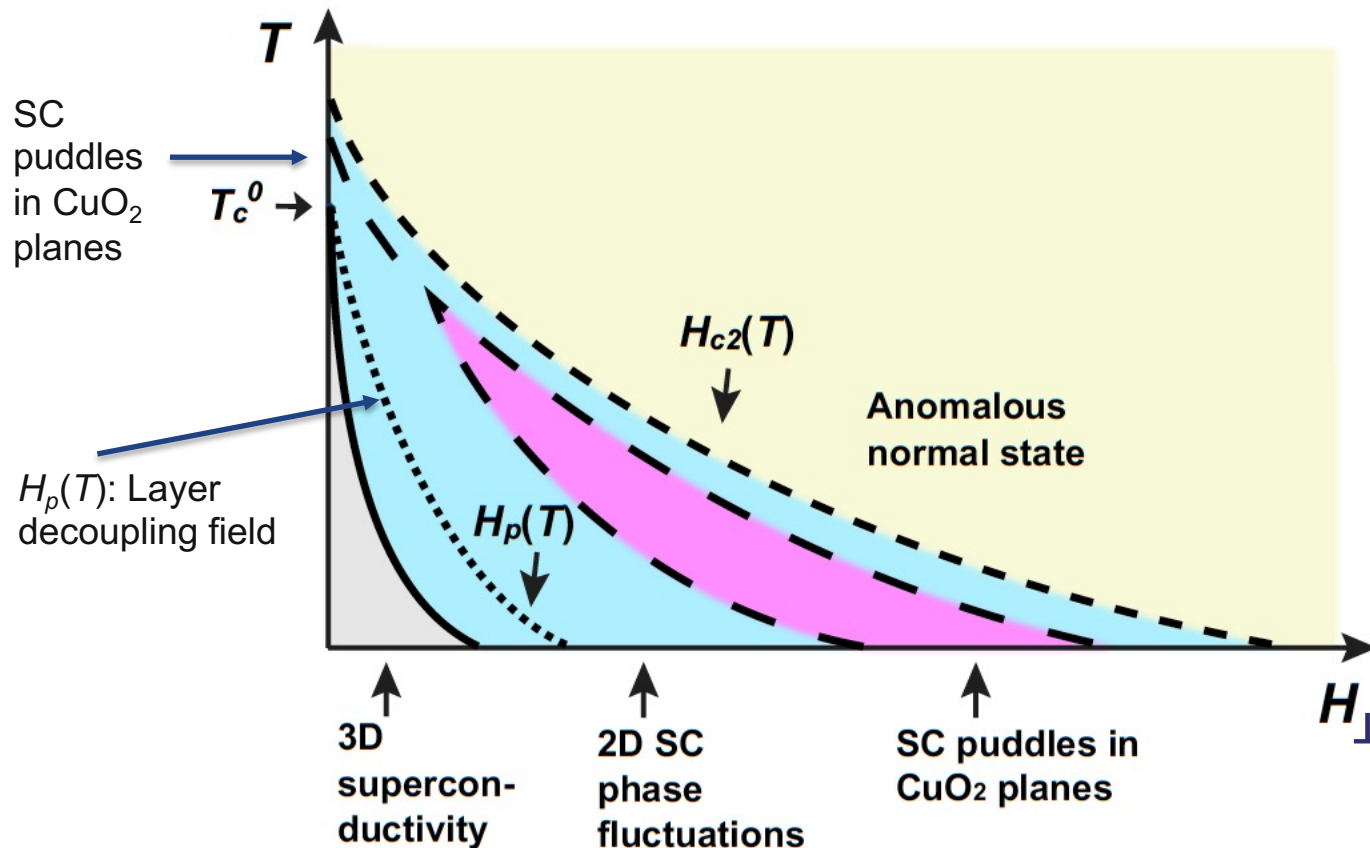
\Rightarrow Intrinsically granular SC state

[A. Kapitulnik *et al.*, Rev. Mod. Phys. 91, 011002 (2019)]



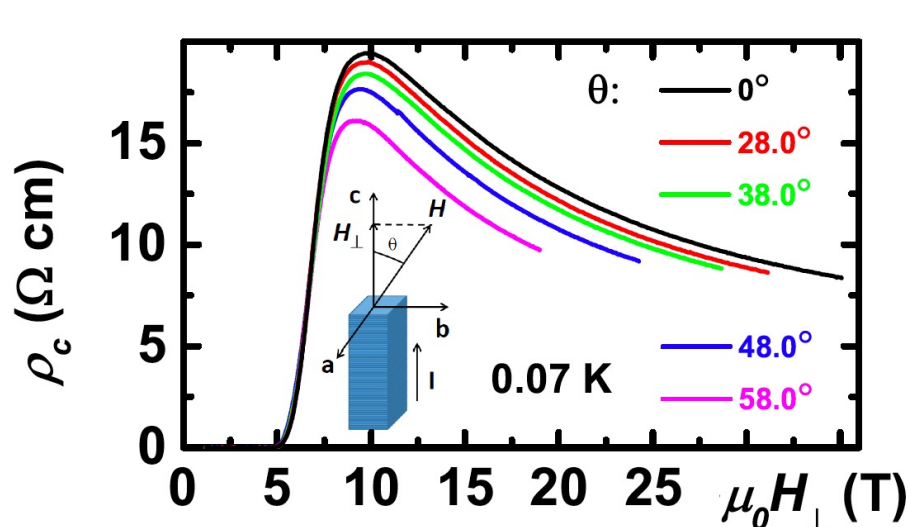
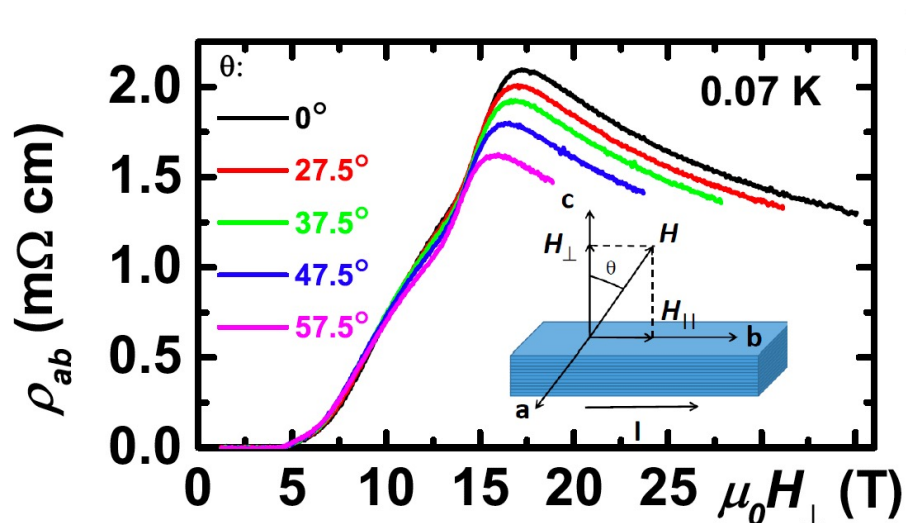
Schematic (T, H_{\perp}) phase diagram of stripe-ordered La-214 cuprates

- Consistent with the presence of **local, PDW correlations** (in puddles) that compete with the uniform SC order at $T_c^0 < T < (2-6)T_c^0$; become **dominant** at high enough $H_{\perp} < H_{c2}$ as $T \rightarrow 0$



Probing interlayer frustration: angle-dependent measurements of $\rho_{ab}(H)$ and $\rho_c(H)$

LESCO, x=0.10



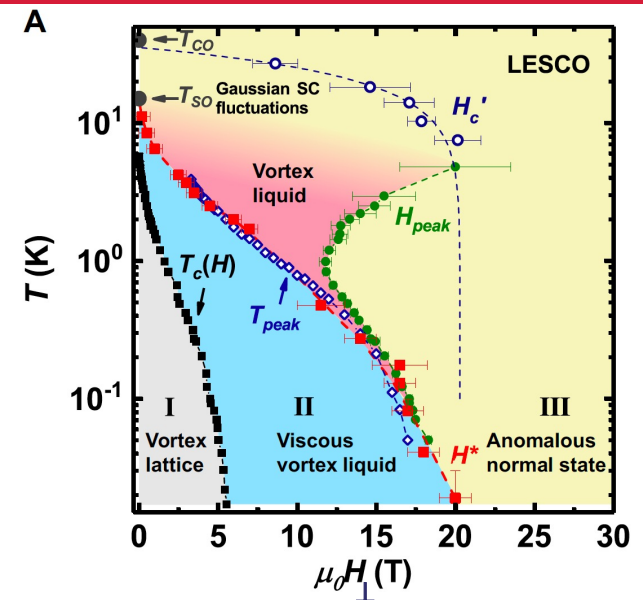
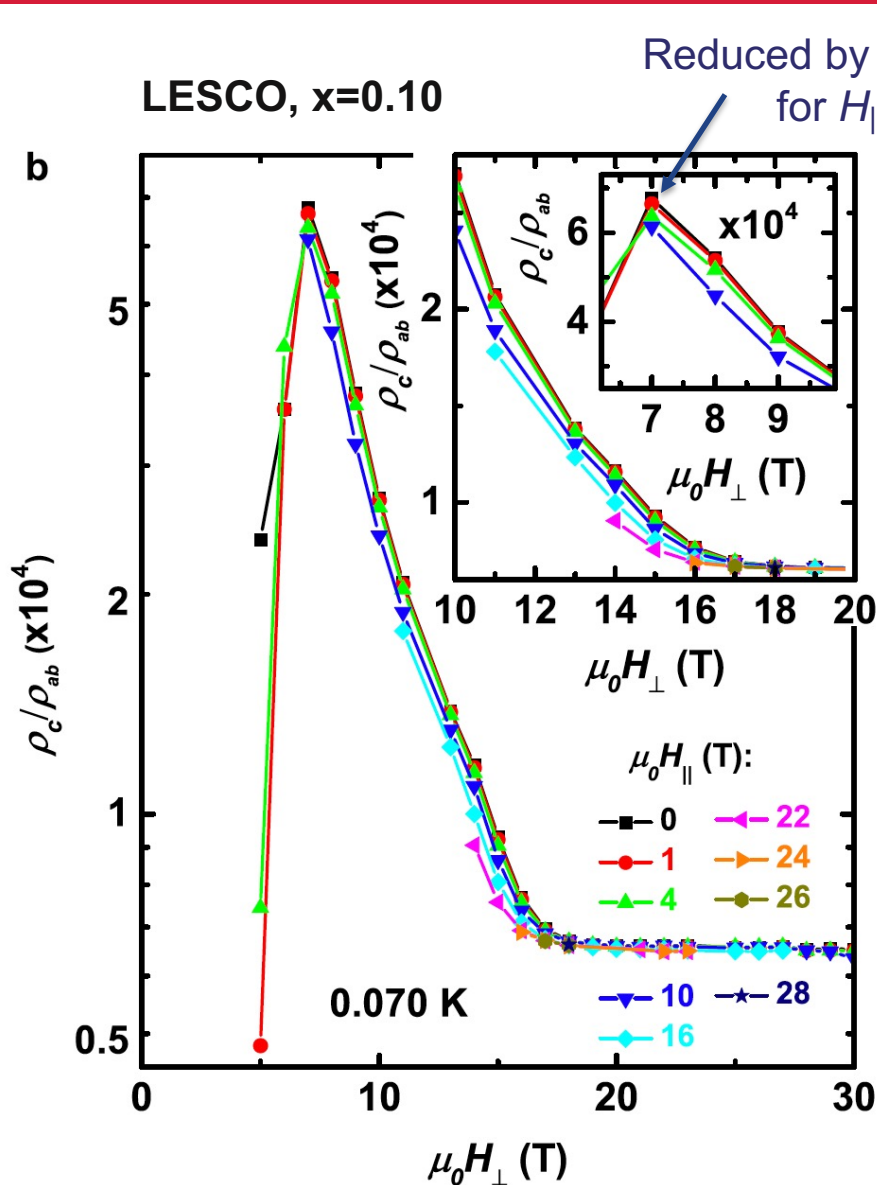
Field perpendicular to the CuO_2 planes: $H_{\perp} = H \cos\theta$

Field parallel to the CuO_2 planes (i.e. to a or b axis): $H_{\parallel} = H \sin\theta$

$H_{\parallel} = H_{\perp} \tan\theta$



Probing interlayer frustration: effect of the in-plane (parallel) magnetic field on ρ_c/ρ_{ab}



H_{\parallel} reduces the anisotropy for $H_p \leq H_{\perp} < H_{c2}$ as predicted in the PDW scenario (reorientation of spins in stripes)

No effect of H_{\parallel} in the normal state: $H_{\perp} > H_{c2}$ ($T=0.070$ K) ≈ 17.5 T

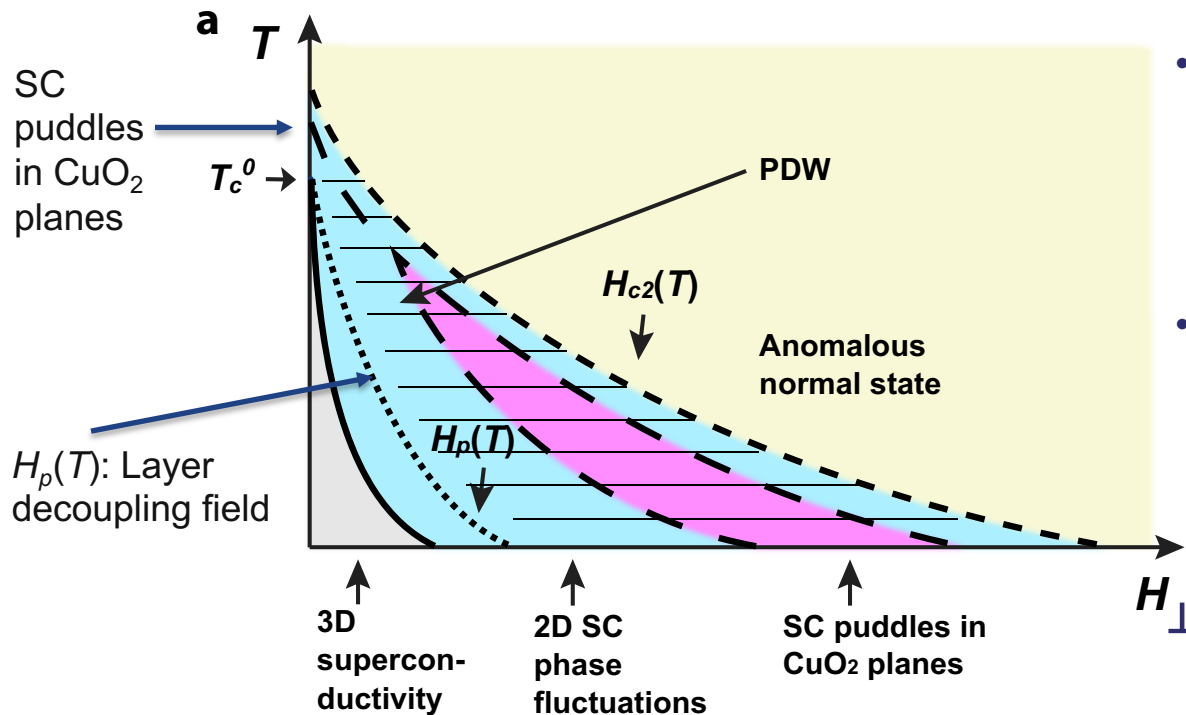


Signatures of a PDW in stripe-ordered Eu-LSCO and Nd-LSCO

[Zhenzhong Shi *et al.*, Nat. Commun. 11, 3323 (2020)]

- Probed the previously inaccessible high H_{\perp}/T_c^0 and $T \rightarrow 0$ regime dominated by **quantum phase fluctuations** and confirmed a theoretical prediction

⇒ Several **signatures of a PDW** for $T_c^0 < T < (2-6)T_c^0 \ll T_{\text{pseudogap}}$ and $H_{\perp} < H_{c2}$



- Results do **not** support a scenario in which the PDW correlations are responsible for the pseudogap
- Observed in the regime with many vortices, **consistent with the STM evidence** for PDW in vortex halos in $\text{Bi}_2\text{Sr}_2\text{CaCu}_2\text{O}_8$ vortex solid

[S. D. Edkins *et al.*, Science 364, 976 (2019)]



Conclusions

- **Robust vortex phase diagram for underdoped cuprates**
 - T - H phase diagram, H_{c2}
 - Key role of quantum phase fluctuations and disorder as $T \rightarrow 0$
 - No qualitative effect of charge and spin orders on the vortex phase diagram

Stripe-ordered cuprates:

- **Signatures of a PDW from $T > T_c^0$ in $H=0$ to $H=H_{c2}$ as $T \rightarrow 0$**

(in the regime of SC phase fluctuations)

- Results do **not** support a scenario in which the PDW correlations are responsible for the pseudogap

